Lecture 3:

# (latency/bandwidth issues)

# Multi-Core Architecture, Part II **Parallel Programming Abstractions**

**Parallel Computing** Stanford CS149, Fall 2023

# **Reviewing last time...**

- Three ideas in throughput computing hardware
  - Multi-core execution
  - SIMD execution
  - Hardware multi-threading
- [Will review by going over slides from the end of lecture 2]

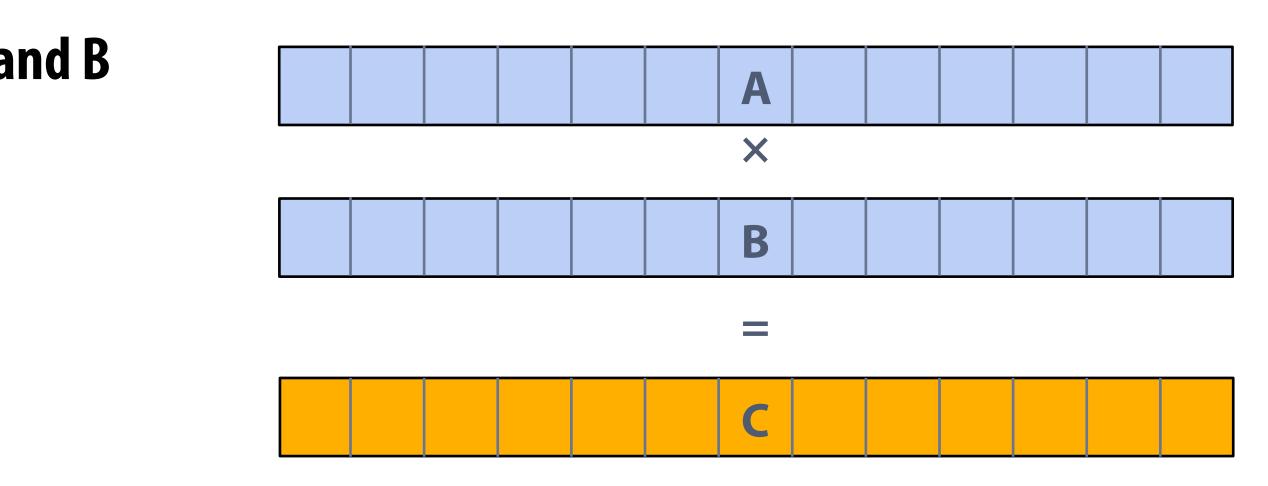


# Thought experiment

Task: element-wise multiplication of two vectors A and B Assume vectors contain millions of elements

- Load input A[i]
- Load input B[i]
- Compute A[i]  $\times$  B[i]
- Store result into C[i]

# Is this a good application to run on a modern throughput-oriented parallel processor?





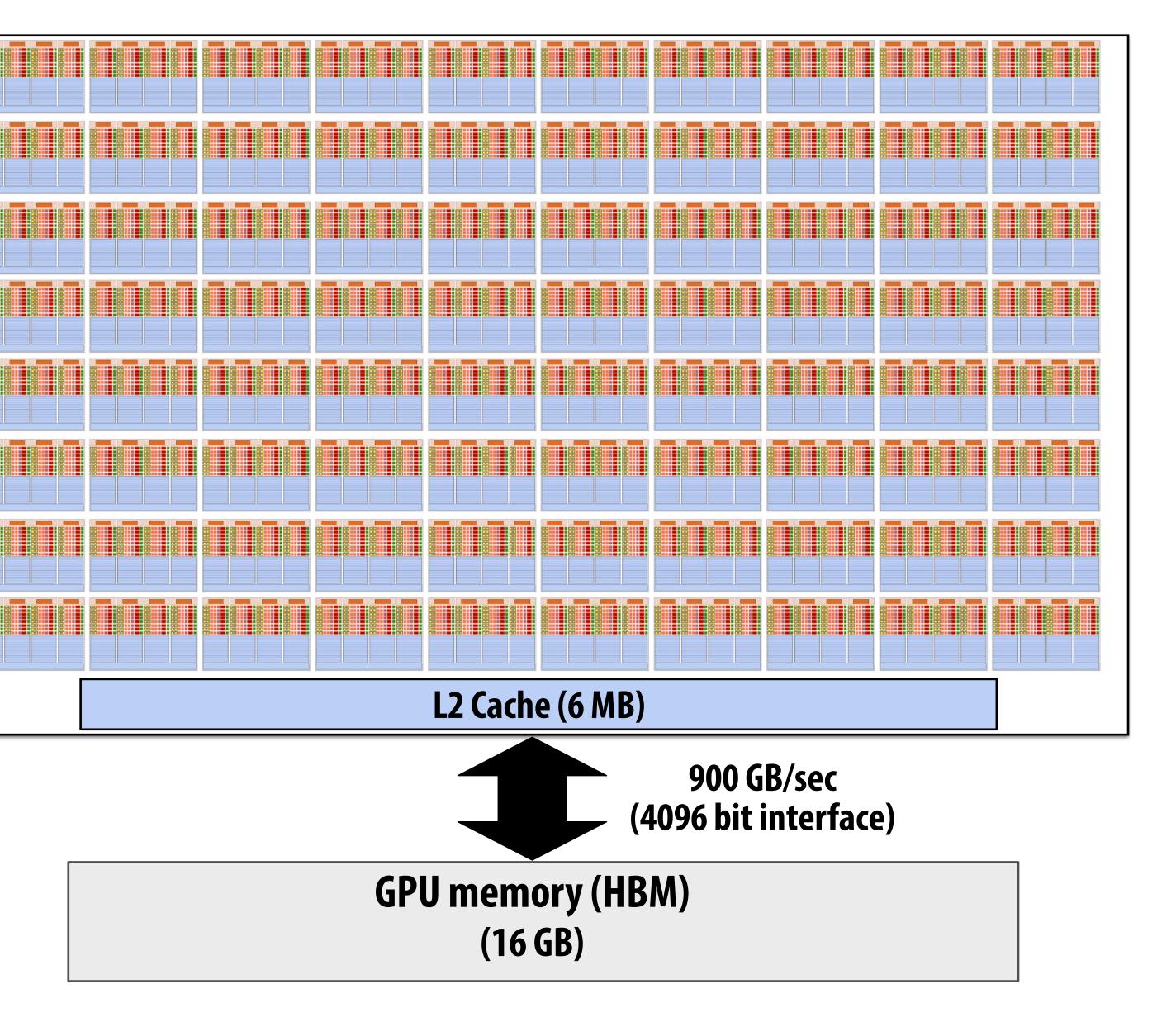
# **NVIDIA V100**

There are 80 SM cores on the V100:

80 SM x 64 fp32 ALUs per SM = 5120 ALUs

# Think about supplying all those ALUs with data each





# Understanding latency and bandwidth



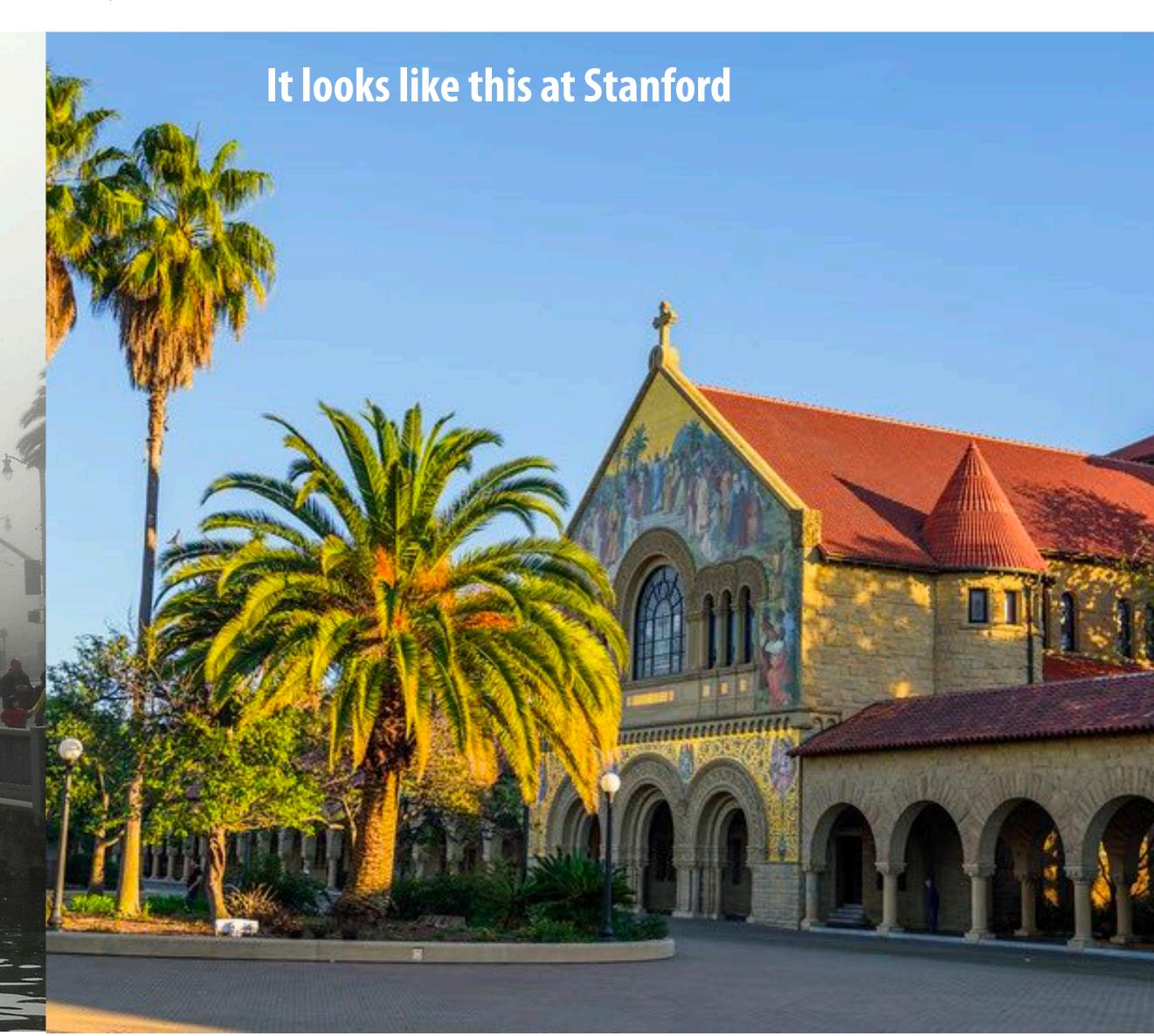
# The school year is starting... gotta get back to Stanford

FFICE



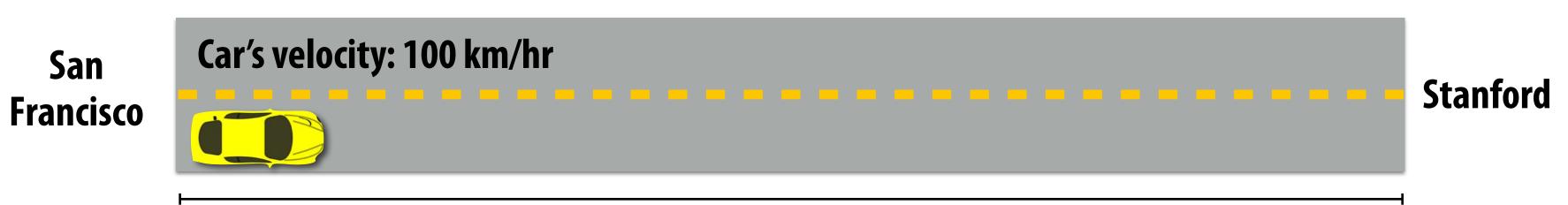
# San Francisco fog vs. South Bay sun

When it looks like this in SF



### **Everyone wants to get to back to the South Bay!**

Assume only one car in a lane of the highway at once. When car on highway reaches Stanford, the next car leaves San Francisco.



Distance: ~ 50 km

**Throughput: 2 cars per hour** 

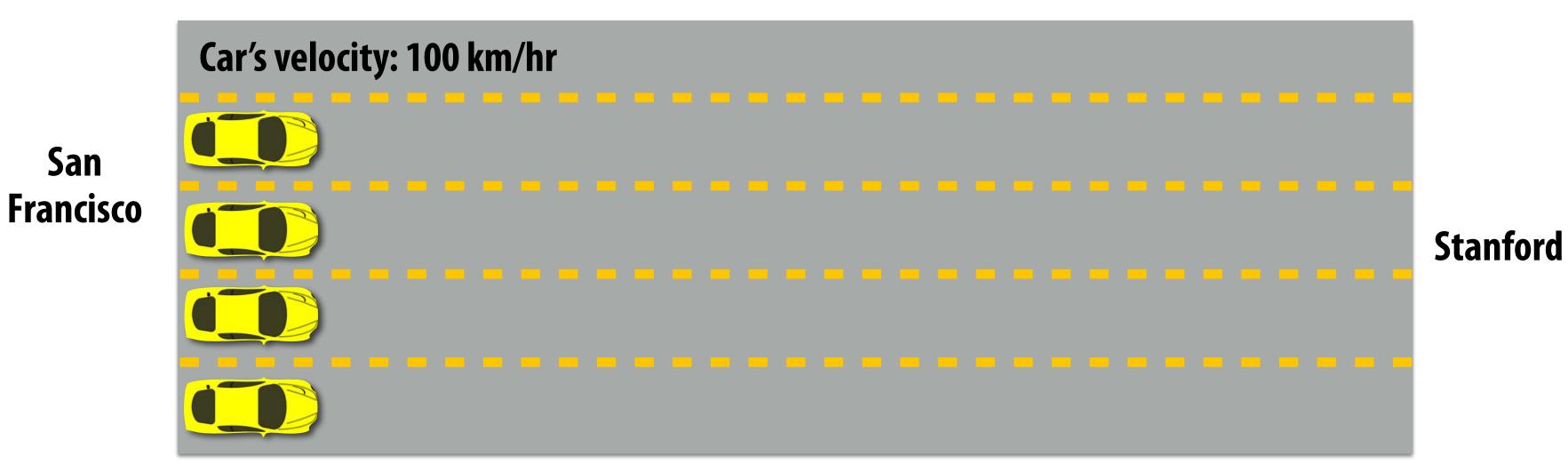
### Latency of driving from San Francisco to Stanford: 0.5 hours



# Improving throughput

San Francisco Car's velocity: 200 km/hr

### **Approach 1: drive faster! Throughput = 4 cars per hour**

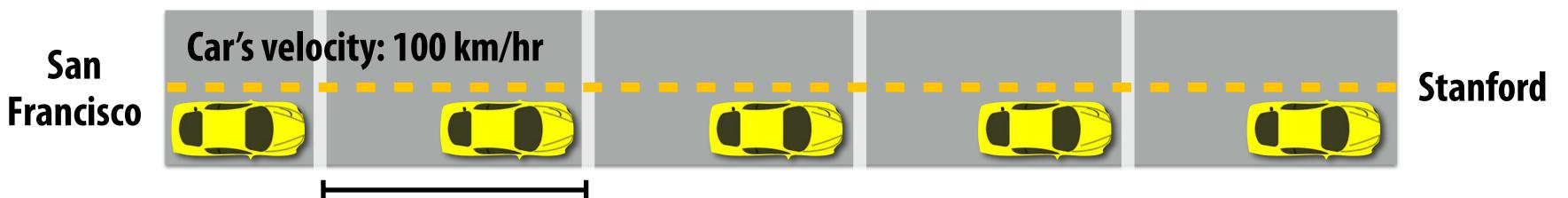


### Stanford

### **Approach 2: build more lanes!** Throughput = 8 cars per hour (2 cars per hour per lane)

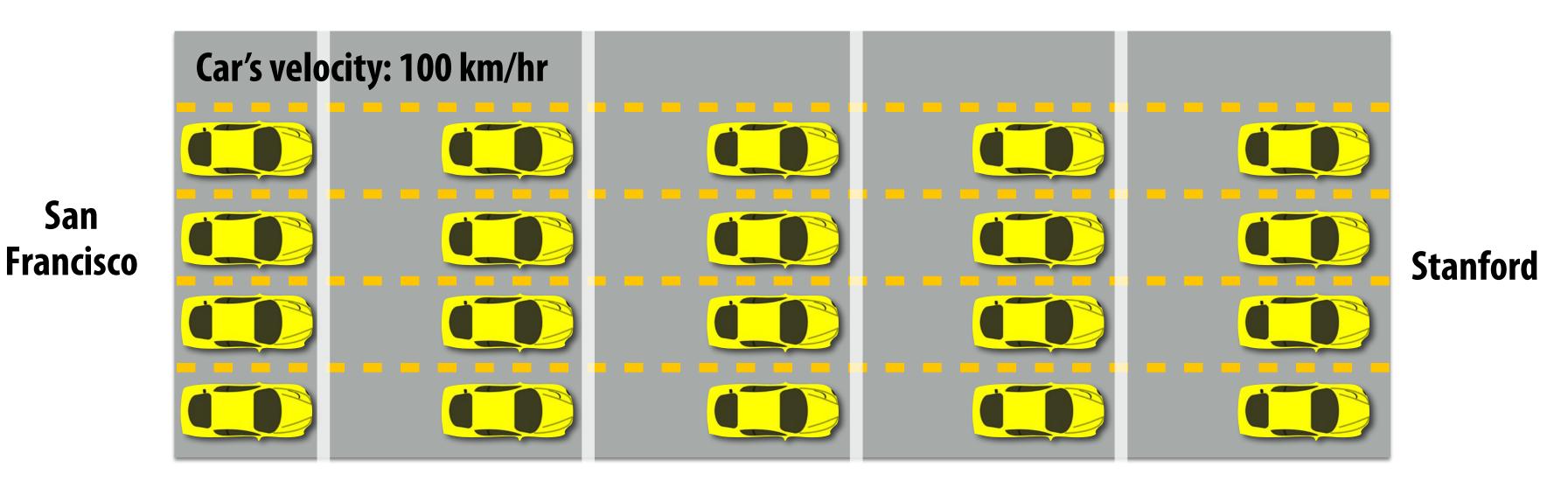


# Using the highway more efficiently



### Cars spaced out by 1 km

### Throughput: 100 cars/hr (1 car every 1/100th of hour)





Throughput: 400 cars/hr (4 cars every 1/100th of hour)



# Terminology

### Memory bandwidth

- The rate at which the memory system can provide data to a processor
- Example: 20 GB/s





Latency of transferring any one item: ~2 sec



# Terminology

### Memory bandwidth

- The rate at which the memory system can provide data to a processor
- Example: 20 GB/s





Latency of transferring any one item: ~2 sec



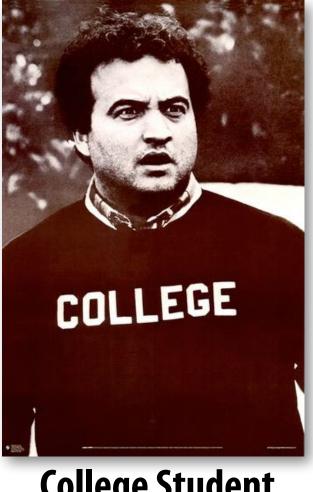
# **Example: doing your laundry Operation: do your laundry**



Washer **45 min** 

000 --

### 1. Wash clothes 2. Dry clothes 3. Fold clothes



Dryer **60 min** 

**College Student 15 min** 

### Latency of completing 1 load of laundry = 2 hours



### **Increasing laundry throughput** Goal: maximize throughput of many loads of laundry

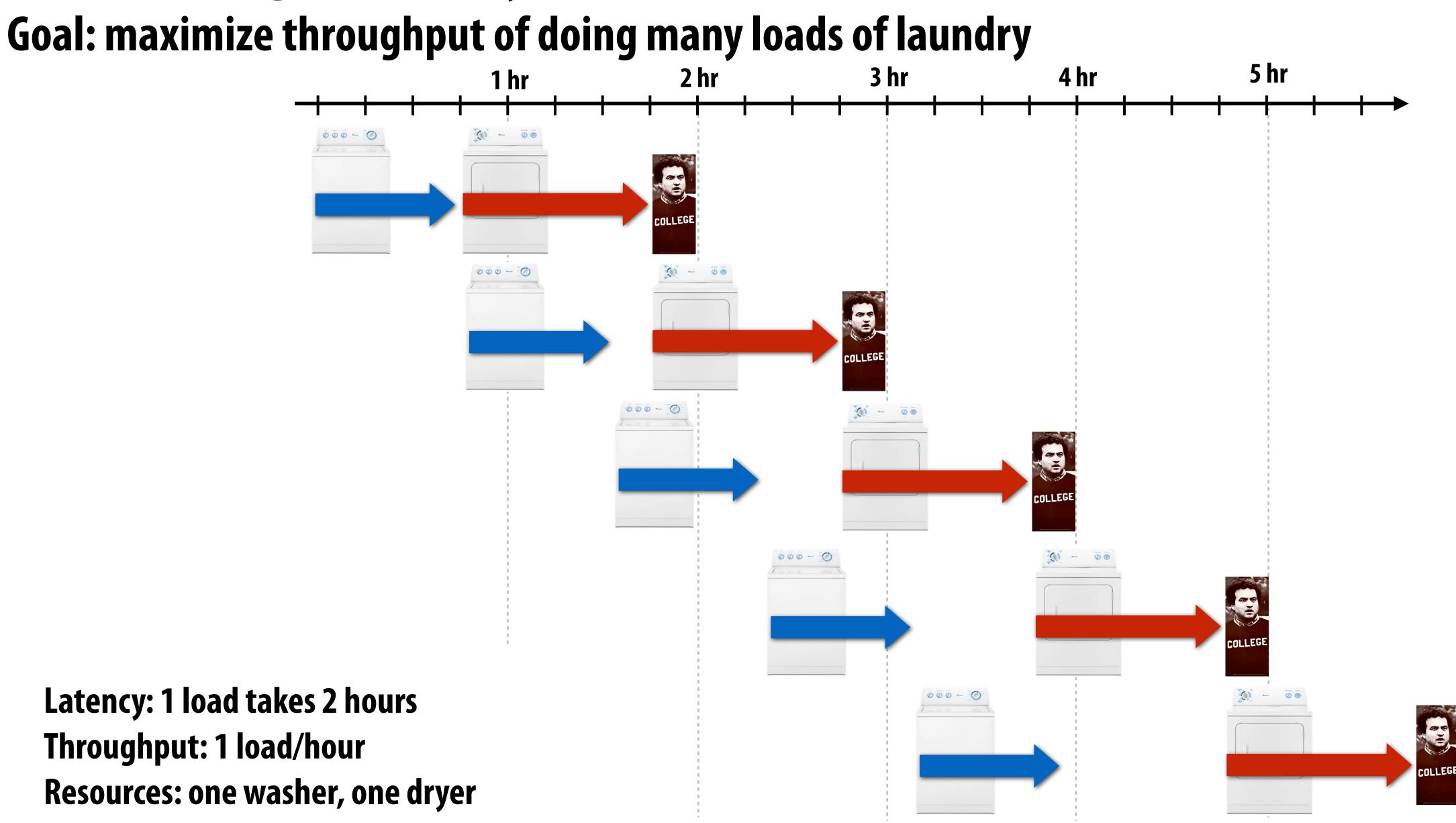


**One approach: duplicate execution resources:** use two washers, two dryers, and call a friend

Latency of completing 2 loads of laundry = 2 hours **Throughput increases by 2x: 1 load/hour** Number of resources increased by 2x: two washers, two dryers



# **Pipelining laundry**

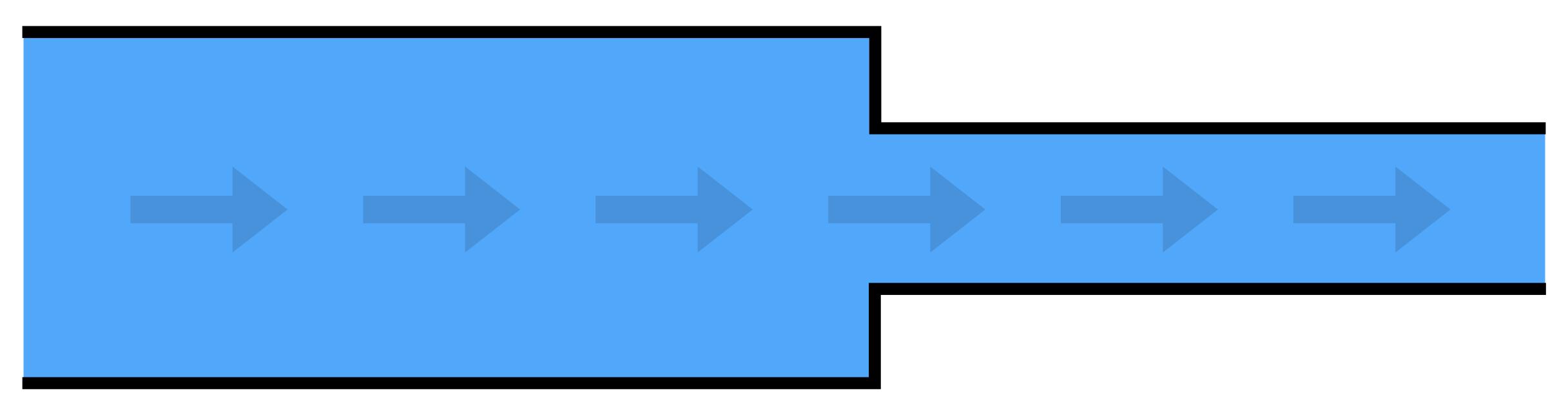


**Throughput: 1 load/hour Resources: one washer, one dryer** 



# Another example: two connected pipes

Pipe 1: max flow 100 liters/sec



### If you connect the pipes, what is the maximum flow you can push through the system? **50 liters/sec**

### Pipe 2: max flow 50 liters/sec

# Applying this concept to a computer...

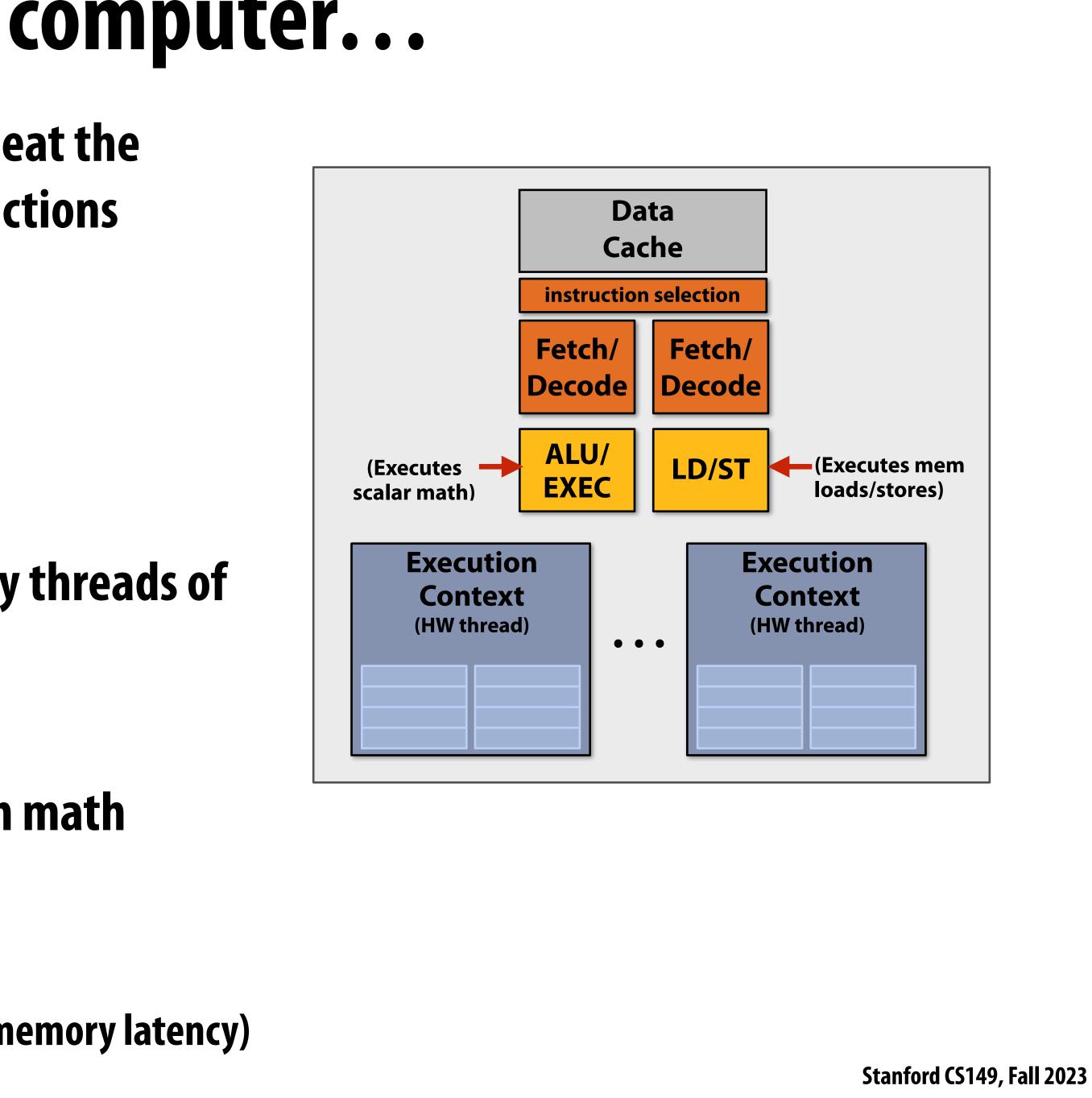
**Consider a program that runs threads that repeat the** following sequence of three dependent instructions

- 1.X = 10ad 64 bytes
- 2. Y = add x + x
- 3. Z = add x + y

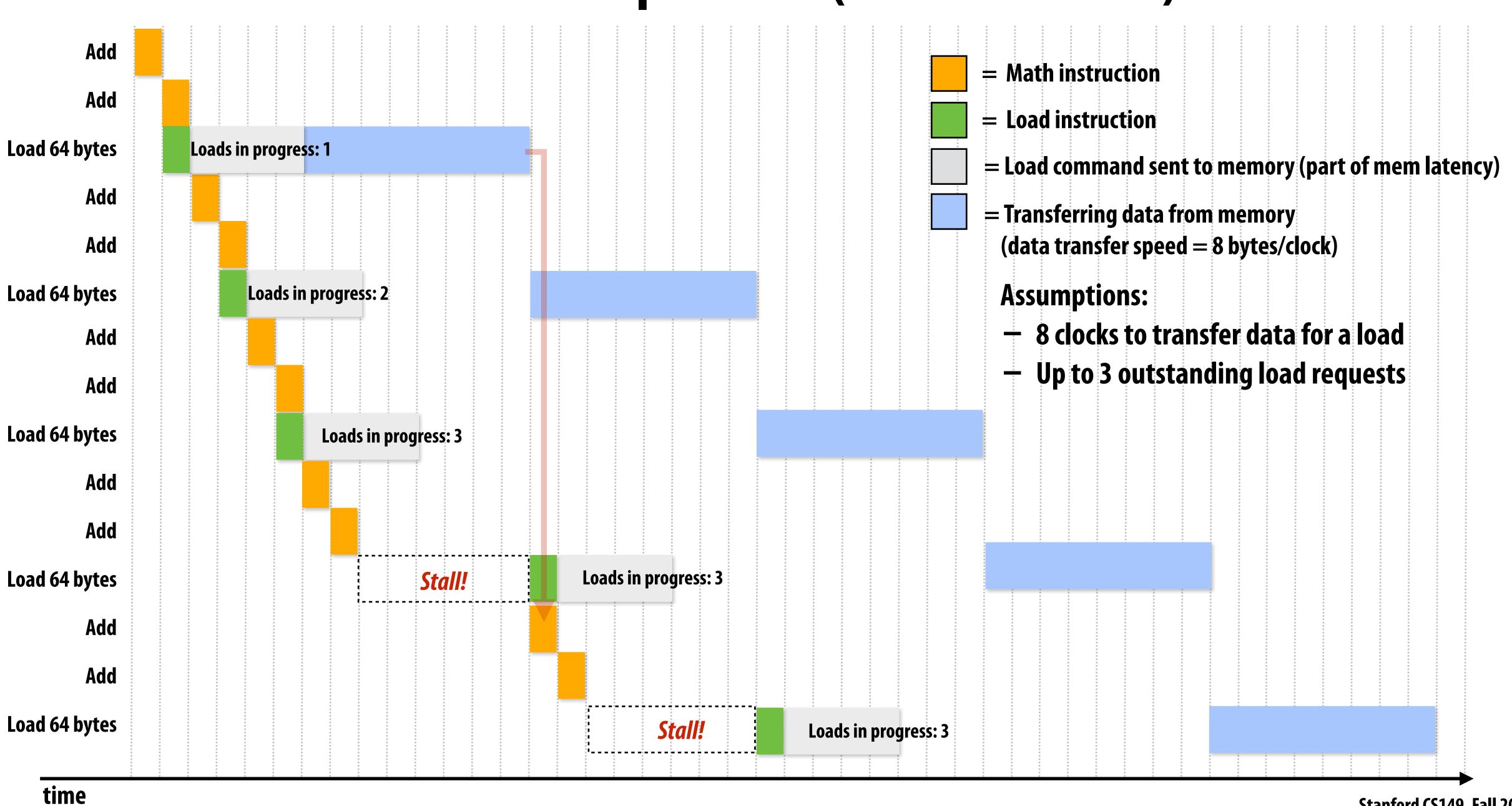
Let's say we're running this sequence on many threads of a multi-threaded\* core that:

- **Executes one math operation per clock**
- Can issue load instructions in parallel with math
- **Receives 8 bytes/clock from memory**

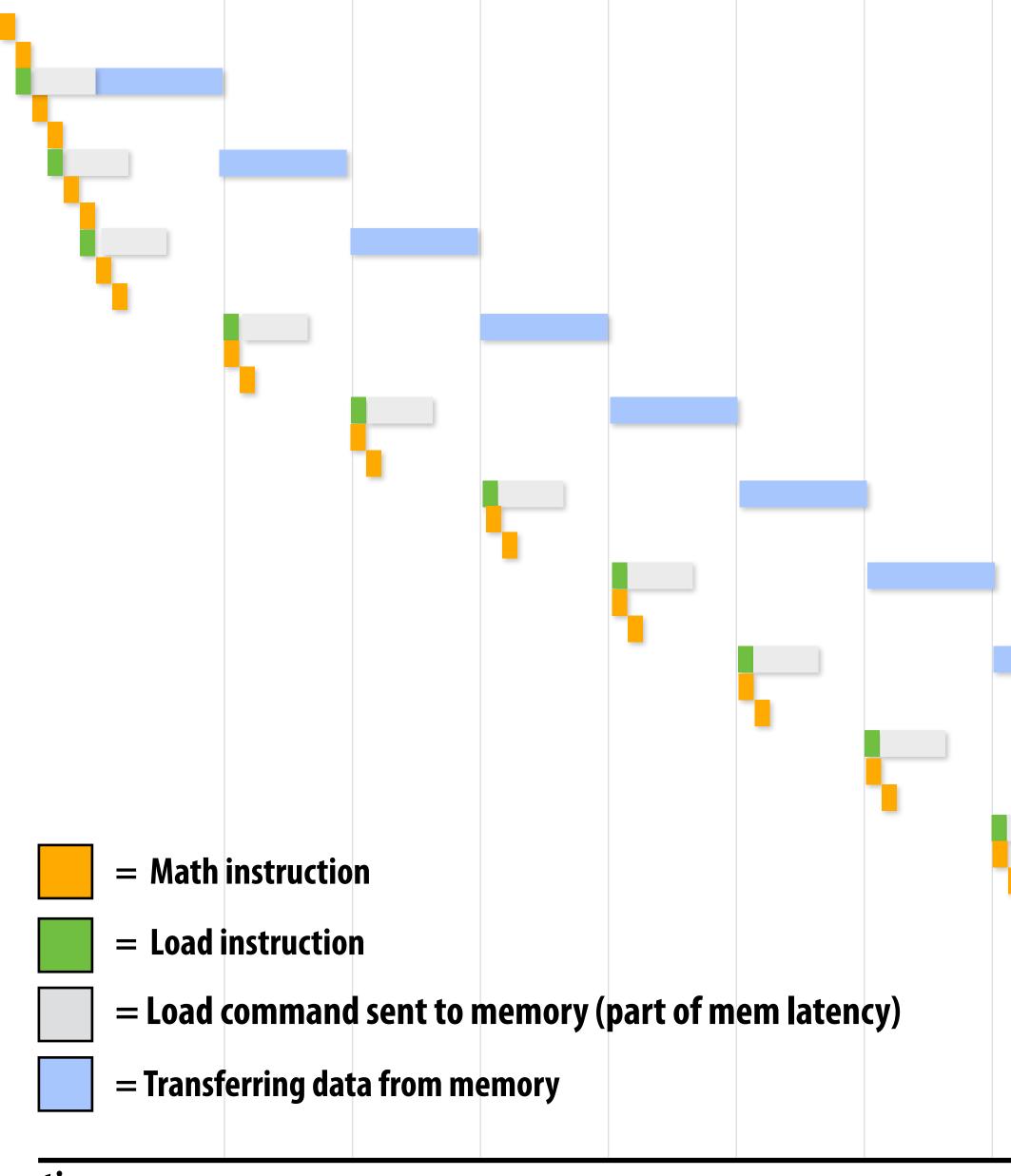
(\* Assume there are plenty of hardware threads to hide memory latency)



### Processor that can do one add per clock (+ co-issues LDs)



### Rate of completing math instructions is limited by memory bandwidth

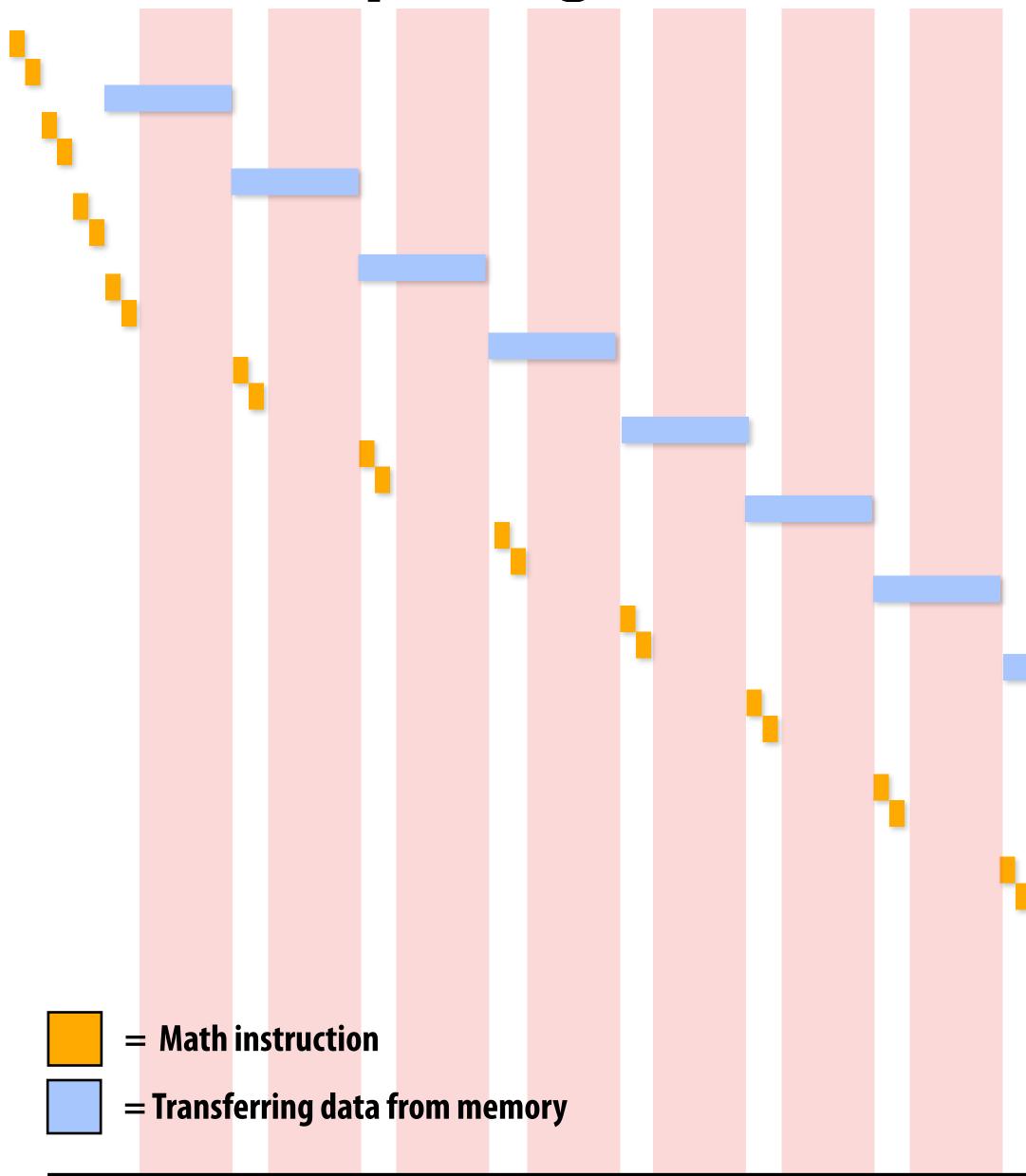


time





### Rate of completing math instructions is limited by memory bandwidth



time

**Memory bandwidth-bound execution!** 

Rate of instructions is determined by the rate at which memory can provide data.

**Red regions: Core is stalled waiting on data for next** instruction

Note that memory is transferring data 100% of time, it can't transfer data faster.

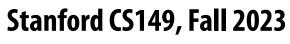
Convince yourself that in steady state core underutilization is only a function of instruction and memory throughput, not a function of memory latency or the number of outstanding memory requests.





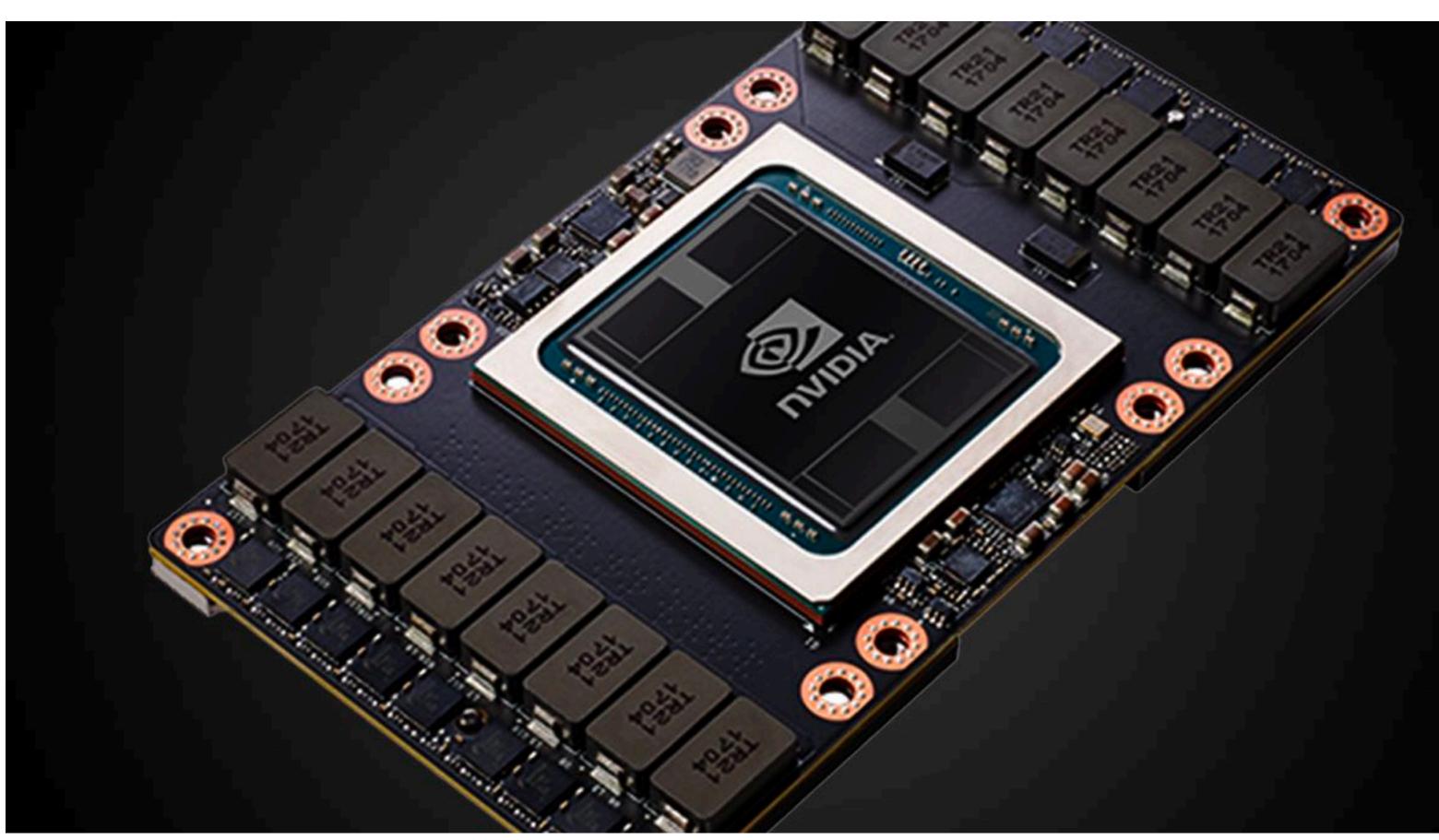






# High bandwidth memories

- Modern GPUs leverage high bandwidth memories located near processor
- **Example:** 
  - V100 uses HBM2
  - 900 GB/s







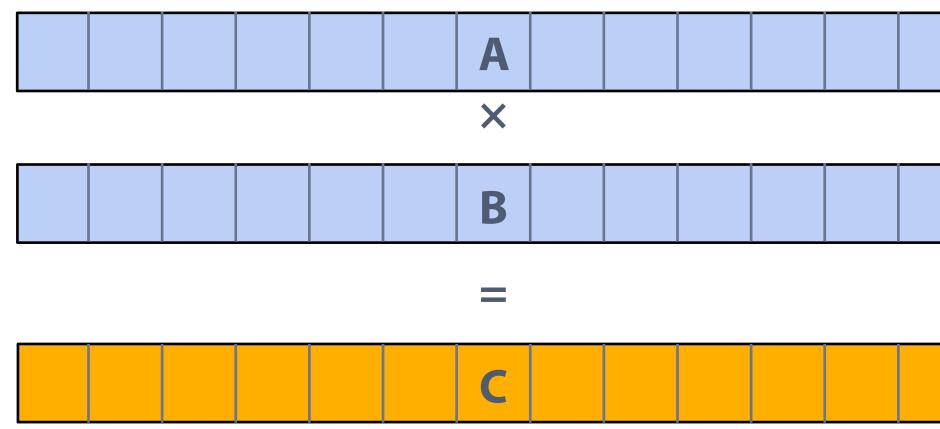
# Back to our thought experiment

Task: element-wise multiplication of two vectors A and B **Assume vectors contain millions of elements** 

- Load input A[i]
- Load input B[i]
- Compute  $A[i] \times B[i]$
- **Store result into C[i]**

Three memory operations (12 bytes) for every MUL NVIDIA V100 GPU can do 5120 fp32 MULs per clock (@ 1.6 GHz) Need ~98 TB/sec of bandwidth to keep functional units busy

### <1% GPU efficiency... but still must faster than an eight-core CPU! (3.2 GHz Xeon E5v4 eight-core CPU connected to 76 GB/sec memory bus: ~3% efficiency on this computation)





# This computation is bandwidth limited!

If processors request data at too high a rate, the memory system cannot keep up.

**Overcoming bandwidth limits is often the most important** challenge facing software developers targeting modern throughput-optimized systems.



# In modern computing, bandwidth is the <u>critical</u> resource

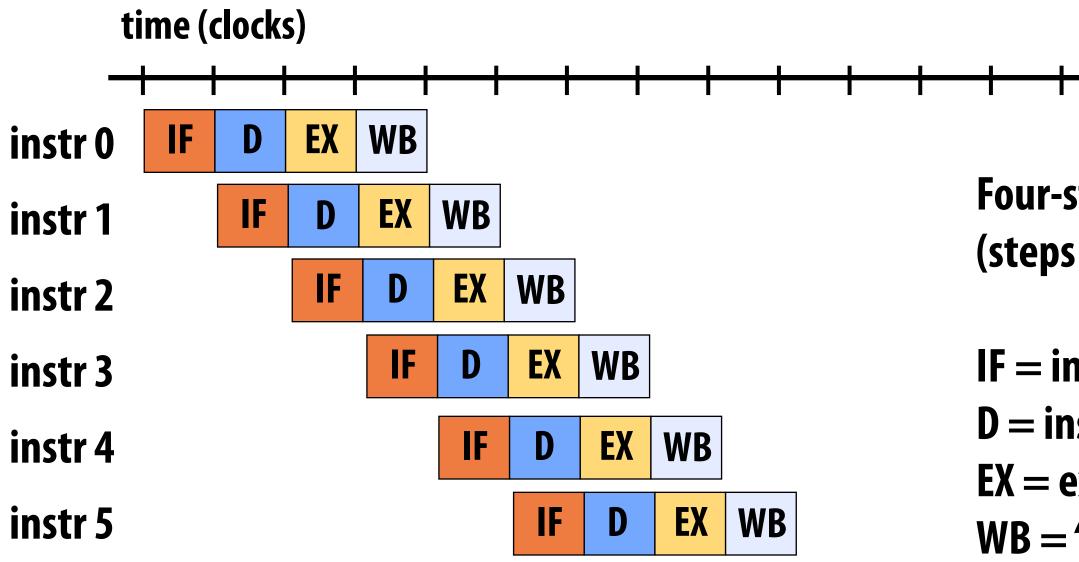
### Performant parallel programs will:

- **Organize computation to fetch data from <u>memory</u> less often** 
  - Reuse data previously loaded by the same thread (temporal locality optimizations)
  - Share data across threads (inter-thread cooperation)
- Favor performing additional arithmetic to storing/reloading values (the math is "free")
- Main point: programs must access memory infrequently to utilize modern processors efficiently



# Another pipelining example: an instruction pipeline

Many students often ask how a processor can complete a multiply operation in a clock. When we say a core does one operation per clock, we are referring to INSTRUCTION THROUGHPUT, NOT LATENCY.



Latency: 1 instruction takes 4 cycles **Throughput: 1 instruction per cycle** (Yes, care must be taken to ensure program correctness when back-to-back instructions are dependent.)

Actual instruction pipelines can be variable length (depending on the instruction) deep as  $\sim$ 20 stages in modern CPUs

Four-stage instruction pipeline (steps required to complete and instruction):

IF = instruction fetch **D** = instruction decode + register read **EX** = execute operation WB = "write back" results to registers



# The theme of the second half of today's lecture is: Abstraction vs. implementation

**Conflating semantics (meaning) of an abstraction with details of its** implementation is a common cause for confusion in this course.

# Part 2:



# Abstraction vs. implementation

**Semantics:** what do the operations provided by a programming model mean?

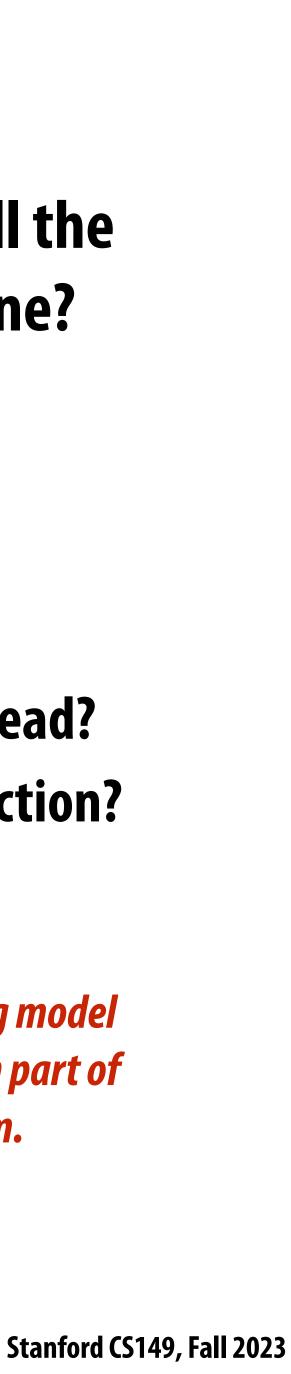
Given a program, and given the semantics (meaning) of the operations used, what is the answer that the program will compute?

### **Implementation** (aka scheduling): how will the answer be computed on a parallel machine?

### In what (potentially parallel) order will be a program's operations be executed? Which operations will be computed by each thread? Each execution unit? Each lane of a vector instruction?

Your goal as a student:

Given a program and knowledge of how a parallel programming model is implemented, in your head can you "trace" through what each part of the parallel computer is doing during each step of program.



# An example: **Programming with ISPC**



# ISPC

- Intel SPMD Program Compiler (ISPC)
- SPMD: single program multiple data

### http://ispc.github.com/

- A great read: "The Story of ISPC" (by Matt Pharr)
  - https://pharr.org/matt/blog/2018/04/30/ispc-all.html
  - Go read it!



# **Recall: example program from last class**

### **Compute** sin(x) **using Taylor expansion:** $sin(x) = x - \frac{x^3}{3!} + \frac{x^5}{5!} - \frac{x^7}{7!} + ...$ for each element of an array of N floating-point numbers

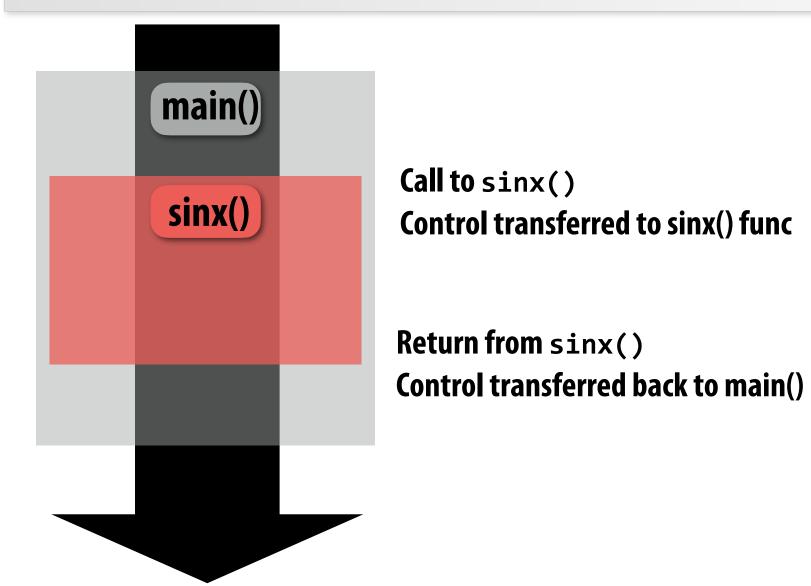
```
void sinx(int N, int terms, float* x, float* result)
   for (int i=0; i<N; i++)</pre>
   {
      float value = x[i];
      float numer = x[i] * x[i] * x[i];
      int denom = 6; // 3!
      int sign = -1;
      for (int j=1; j<=terms; j++)</pre>
      {
         value += sign * numer / denom;
         numer *= x[i] * x[i];
         denom *= (2*j+2) * (2*j+3);
         sign *= -1;
      }
      result[i] = value;
```



# **Invoking sinx()**

### C++ code: main.cpp

```
#include "sinx.h"
int main(int argc, void** argv) {
  int N = 1024;
  int terms = 5;
  float* x = new float[N];
  float* result = new float[N];
  // initialize x here
  sinx(N, terms, x, result);
  return 0;
}
```



### **C++ code:** sinx.cpp

```
void sinx(int N, int terms, float* x, float* result)
  for (int i=0; i<N; i++)</pre>
   {
      float value = x[i];
      float numer = x[i] * x[i] * x[i];
      int denom = 6; // 3!
      int sign = -1;
      for (int j=1; j<=terms; j++)</pre>
      {
         value += sign * numer / denom;
         numer *= x[i] * x[i];
         denom *= (2*j+2) * (2*j+3);
         sign *= -1;
      }
      result[i] = value;
```



# sinx() in ISPC

### C++ code: main.cpp

```
#include "sinx_ispc.h"
int main(int argc, void** argv) {
  int N = 1024;
  int terms = 5;
  float* x = new float[N];
  float* result = new float[N];
  // initialize x here
  // execute ISPC code
  ispc_sinx(N, terms, x, result);
  return 0;
```

### **SPMD programming abstraction:**

Call to ISPC function spawns "gang" of ISPC "program instances"

All instances run ISPC code concurrently

Each instance has its own copy of local variables (blue variables in code, we'll talk about "uniform" later)

Upon return, all instances have completed

### **ISPC code:** sinx.ispc

```
export void ispc_sinx(
   uniform int N,
   uniform int terms,
   uniform float* x,
   uniform float* result)
   // assume N % programCount = 0
   for (uniform int i=0; i<N; i+=programCount)</pre>
      int idx = i + programIndex;
      float value = x[idx];
      float numer = x[idx] * x[idx] * x[idx];
      uniform int denom = 6; // 3!
      uniform int sign = -1;
      for (uniform int j=1; j<=terms; j++)</pre>
         value += sign * numer / denom
         numer *= x[idx] * x[idx];
         denom *= (2*j+2) * (2*j+3);
         sign *= -1;
      result[idx] = value;
```



# **Invoking sinx() in ISPC**

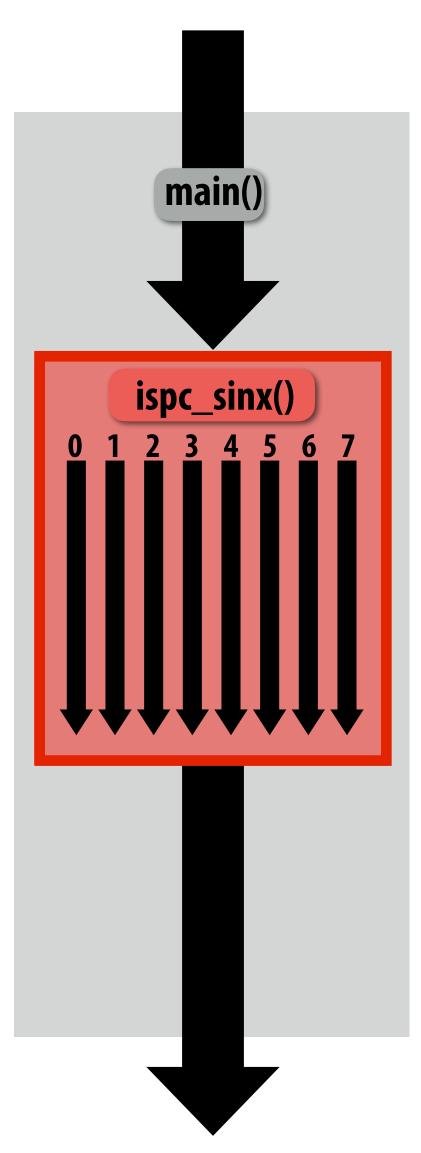
### C++ code: main.cpp

```
#include "sinx_ispc.h"
int main(int argc, void** argv) {
  int N = 1024;
  int terms = 5;
  float* x = new float[N];
  float* result = new float[N];
  // initialize x here
  // execute ISPC code
  ispc_sinx(N, terms, x, result);
  return 0;
```

### **SPMD programming abstraction:**

Call to ISPC function spawns "gang" of ISPC "program instances" All instances run ISPC code concurrently Each instance has its own copy of local variables Upon return, all instances have completed

In this illustration programCount = 8



### Sequential execution (C code)

Call to ispc\_sinx() **Begin executing** programCount instances of ispc\_sinx() (ISPC code)

ispc\_sinx() returns. **Completion of ISPC program instances Resume sequential execution** 

Sequential execution (C code)



# sinx() in ISPC

### "Interleaved" assignment of array elements to program instances

### C++ code: main.cpp

```
#include "sinx_ispc.h"
int main(int argc, void** argv) {
    int N = 1024;
    int terms = 5;
    float* x = new float[N];
    float* result = new float[N];
    // initialize x here
    // execute ISPC code
    ispc_sinx(N, terms, x, result);
    return 0;
}
```

### ISPC language keywords:

programCount: number of simultaneously executing instances in the gang (uniform value)

programIndex: id of the current instance in the gang.
(a non-uniform value: "varying")

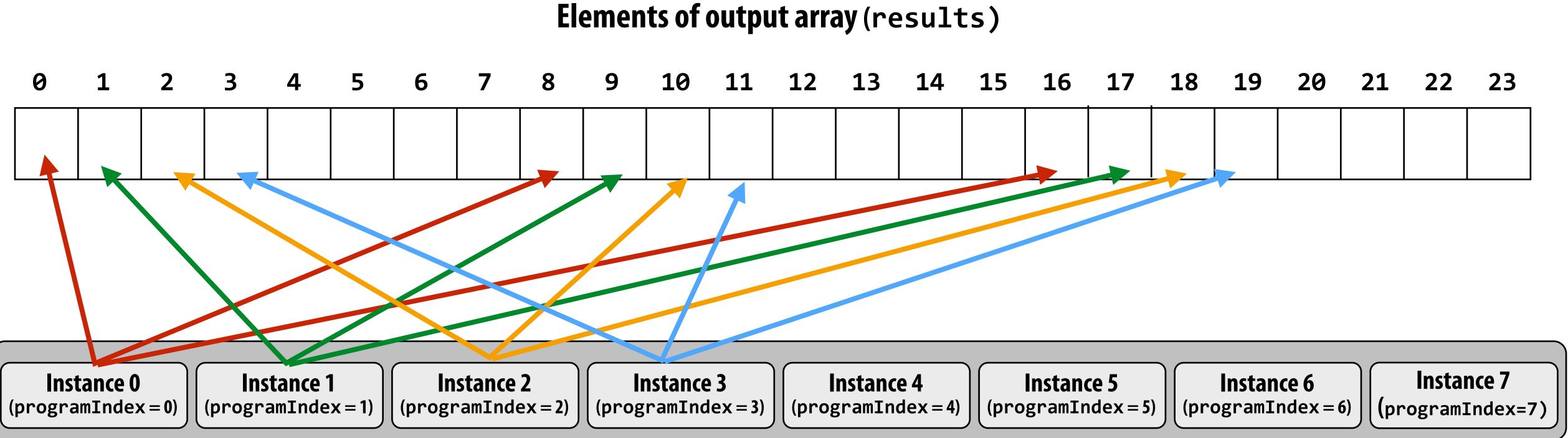
uniform: A type modifier. All instances have the same value for this variable. Its use is purely an optimization. Not needed for correctness.

```
ISPC code: sinx.ispc
```

```
export void ispc_sinx(
   uniform int N,
   uniform int terms,
   uniform float* x,
   uniform float* result)
   // assumes N % programCount = 0
   for (uniform int i=0; i<N; i+=programCount)</pre>
   {
      int idx = i + programIndex;
      float value = x[idx];
      float numer = x[idx] * x[idx] * x[idx];
      uniform int denom = 6; // 3!
      uniform int sign = -1;
      for (uniform int j=1; j<=terms; j++)</pre>
         value += sign * numer / denom
         numer *= x[idx] * x[idx];
         denom *= (2*j+2) * (2*j+3);
         sign *= -1;
      result[idx] = value;
```



## Interleaved assignment of program instances to loop iterations



In this illustration: gang contains eight instances: programCount = 8

### "Gang" of ISPC program instances





### ISPC <u>implements</u> the gang abstraction using SIMD instructions

### C++ code: main.cpp

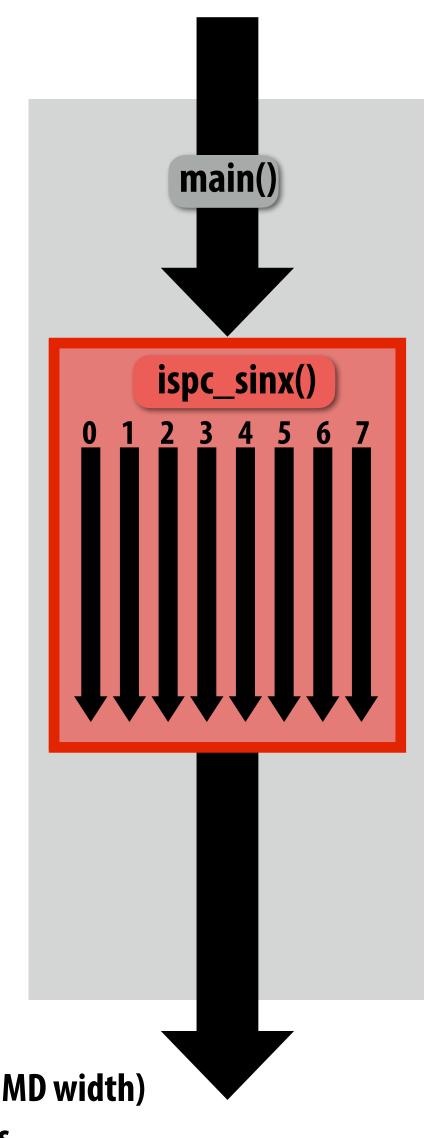
```
#include "sinx_ispc.h"
int main(int argc, void** argv) {
  int N = 1024;
  int terms = 5;
  float* x = new float[N];
  float* result = new float[N];
  // initialize x here
  // execute ISPC code
  ispc sinx(N, terms, x, result);
  return 0;
```

### **SPMD programming abstraction:**

Call to ISPC function spawns "gang" of ISPC "program instances" All instances run ISPC code simultaneously Upon return, all instances have completed

### ISPC compiler generates SIMD implementation:

Number of instances in a gang is the SIMD width of the hardware (or a small multiple of SIMD width) ISPC compiler generates a C++ function binary (.o) whose body contains SIMD instructions C++ code links against generated object file as usual



Sequential execution (C code)

Callto ispc\_sinx() Begin executing programCount instances of ispc\_sinx() (ISPC code)

ispc\_sinx() returns. **Completion of ISPC program instances Resume sequential execution** 

Sequential execution (C code)



### sinx() in ISPC: version 2

### "Blocked" assignment of array elements to program instances

C++ code: main.cpp

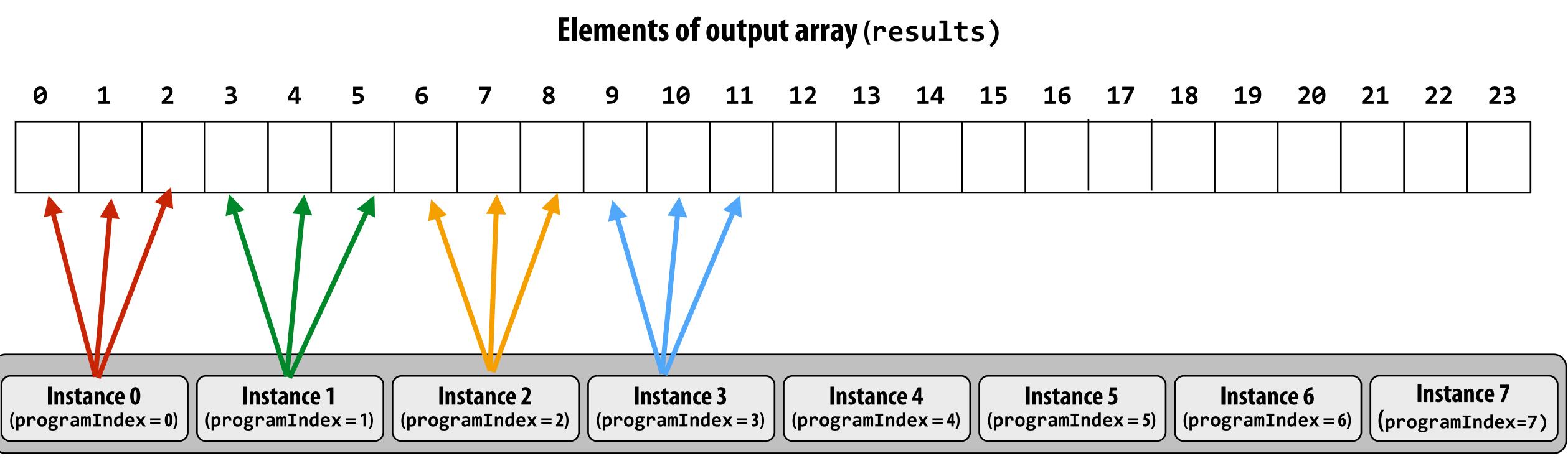
```
#include "sinx_ispc.h"
int main(int argc, void** argv) {
  int N = 1024;
  int terms = 5;
  float* x = new float[N];
  float* result = new float[N];
  // initialize x here
  // execute ISPC code
  ispc_sinx_v2(N, terms, x, result);
  return 0;
```

#### **ISPC code:** sinx.ispc

```
export void ispc_sinx_v2(
   uniform int N,
   uniform int terms,
   uniform float* x,
   uniform float* result)
   // assume N % programCount = 0
   uniform int count = N / programCount;
   int start = programIndex * count;
  for (uniform int i=0; i<count; i++)</pre>
      int idx = start + i;
      float value = x[idx];
      float numer = x[idx] * x[idx] * x[idx];
      uniform int denom = 6; // 3!
      uniform int sign = -1;
      for (uniform int j=1; j<=terms; j++)</pre>
         value += sign * numer / denom
         numer *= x[idx] * x[idx];
         denom *= (j+3) * (j+4);
         sign *= -1;
      result[idx] = value;
```



### Blocked assignment of program instances to loop iterations



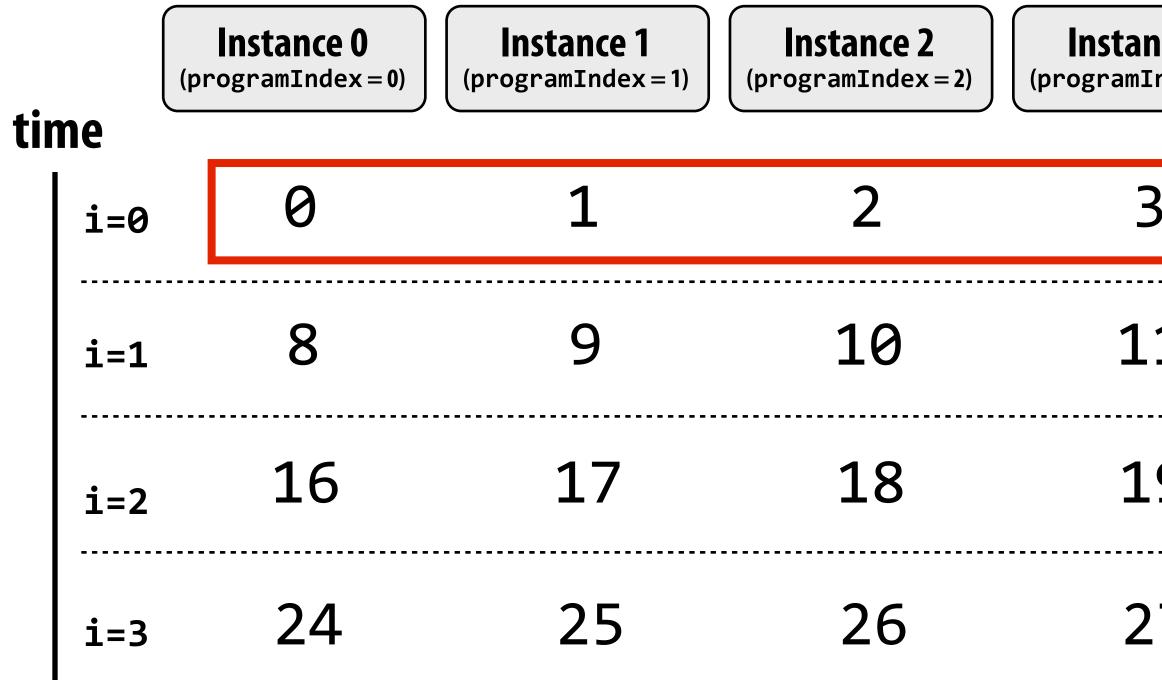
In this illustration: gang contains eight instances: programCount = 8

### "Gang" of ISPC program instances



## Schedule: interleaved assignment

### **Gang contains four instances:** programCount = 8



A single "packed vector load" instruction (vmovaps \*) efficiently float value = x[idx]; for all program instances, since the eight values are contiguous

\* see \_\_mm256\_load\_ps() intrinsic function

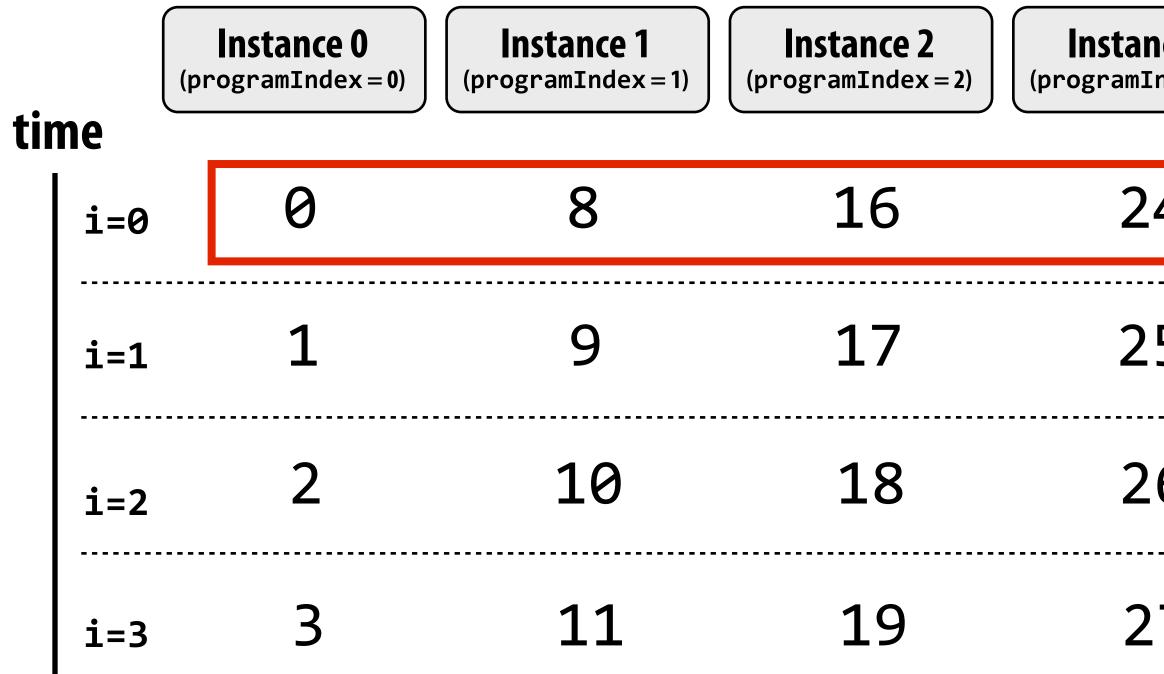
### "Gang" of ISPC program instances

nce 3 Index = 3)	<b>Instance 4</b> programIndex = 4)	<b>Instance 5</b> (programIndex = 5)	<b>Instance 6</b> (programIndex = 6)	<b>Instance 7</b> (programIndex =
3	4	5	6	7
1	12	13	14	15
9	20	21	22	23
.7	28	29	30	31
<pre>y implements: // assumes N % programCount = 0 for (uniform int i=0; i<n; i+="programCount)&lt;/td"></n;></pre>				



### Schedule: blocked assignment "Gang" of ISPC program instances

### **Gang contains four instances:** programCount = 8



float value = x[idx];
For all program instances now touches eight non-contiguous v
memory. Need "gather" instruction (vgatherdps \*) to impleme
a more complex, and more costly SIMD instruction...)

\* see \_mm256\_i32gather\_ps() intrinsic function

<b>1ce 3</b> (index = 3)	<b>Instance 4</b> (programIndex = 4)	<b>Instance 5</b> (programIndex = 5)	<b>Instance 6</b> (programIndex = 6)	<b>Instance 7</b> (programIndex =
4	32	40	48	56
5	33	41	49	57
6	34	42	50	58
7	35	43	51	59
values in ent (gath	eris int s	<pre>uniform int count = N / programCount; int start = programIndex * count; for (uniform int i=0; i<count; i++)="" {<br="">int idx = start + i; float value = x[idx]; </count;></pre>		



## **Raising level of abstraction with foreach**

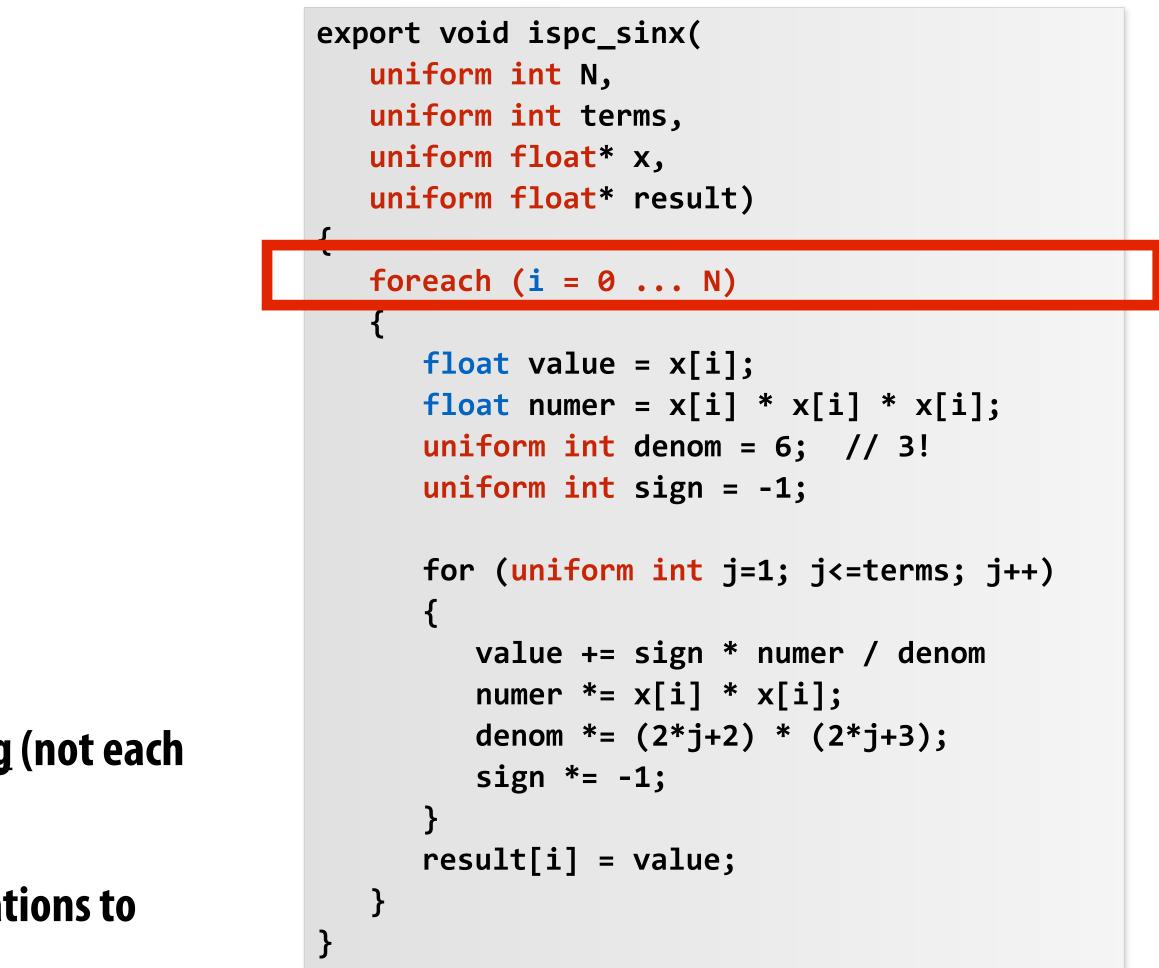
#### C++ code: main.cpp

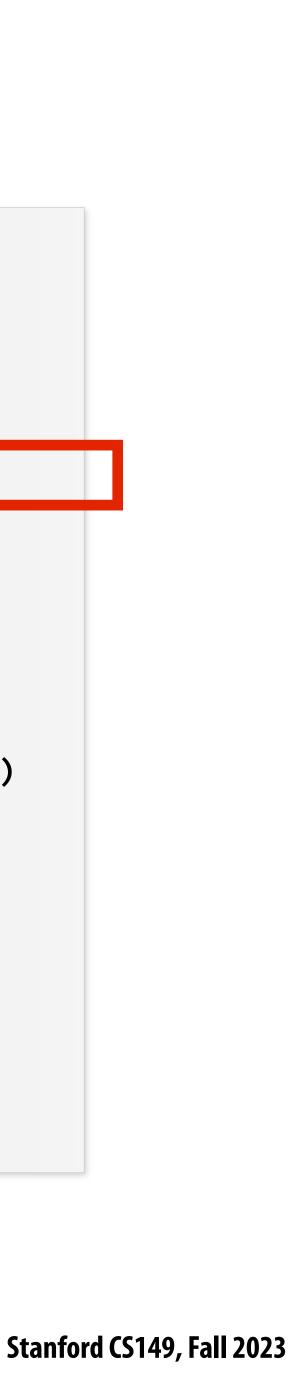
```
#include "sinx_ispc.h"
int N = 1024;
int terms = 5;
float* x = new float[N];
float* result = new float[N];
// initialize x here
// execute ISPC code
sinx(N, terms, x, result);
```

#### foreach: key ISPC language construct

- foreach declares parallel loop iterations
  - Programmer says: these are the iterations <u>the entire gang</u> (not each instance) must perform
- ISPC implementation takes responsibility for assigning iterations to program instances in the gang

#### **ISPC code:** sinx.ispc





## How might foreach be implemented?

**Code written using foreach abstraction:** 

```
foreach (i = 0 ... N)
{
    // do work for iteration i here...
}
```

Implementation 1: program instance 0 executes all iterations

```
if (programCount == 0) {
   for (int i=0; i<N; i++) {
        // do work for iteration i here...
   }
}</pre>
```

#### Implementation 2: interleave iterations onto program instances

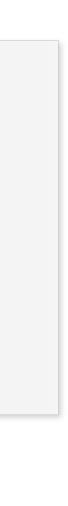
```
// assume N % programCount = 0
for (uniform int loop_i=0; loop_i<N; loop_i+=programCount)
{
    int i = loop_i + programIndex;
    // do work for iteration i here...
}</pre>
```

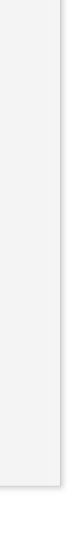
#### Implementation 3: block iterations onto program instances

```
// assume N % programCount = 0
uniform int count = N / programCount;
int start = programIndex * count;
for (uniform int loop_i=0; loop_i<count; loop_i++)
{
    int i = start + loop_i;
    // do work for iteration i here...
}</pre>
```

#### Implementation 4: dynamic assignment of iterations to instances

```
uniform int nextIter;
if (programCount == 0)
nextIter = 0;
int i = atomic_add_local(&nextIter, 1);
while (i < N) {
   // do work for iteration i here...
   i = atomic_add_local(&nextIter, 1);
}
```





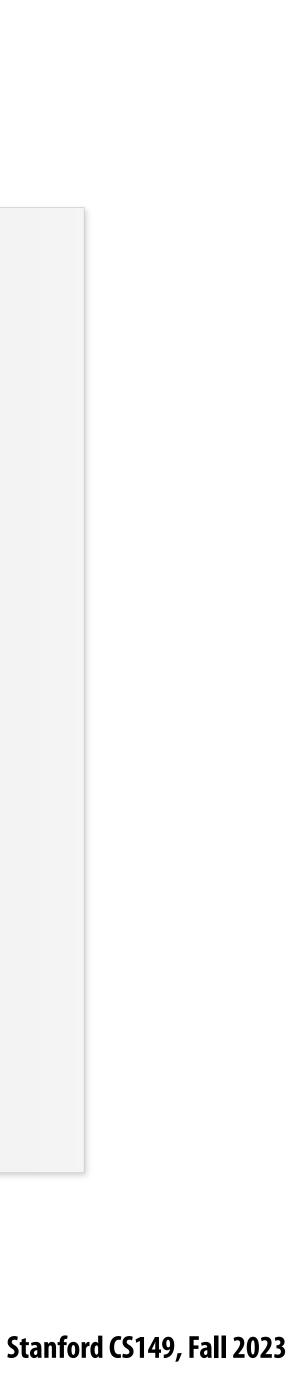


## Thinking about iterations, not parallel execution

In many simple cases, using foreach allows the programmer to express their program almost as if it was a sequential program

```
uniform int N,
uniform float* x,
uniform float* y)
foreach (i = 0 \dots N)
  float val = x[I];
  float result;
  // do work here to compute
  // result from val
 y[i] = result;
```

export void ispc\_function(

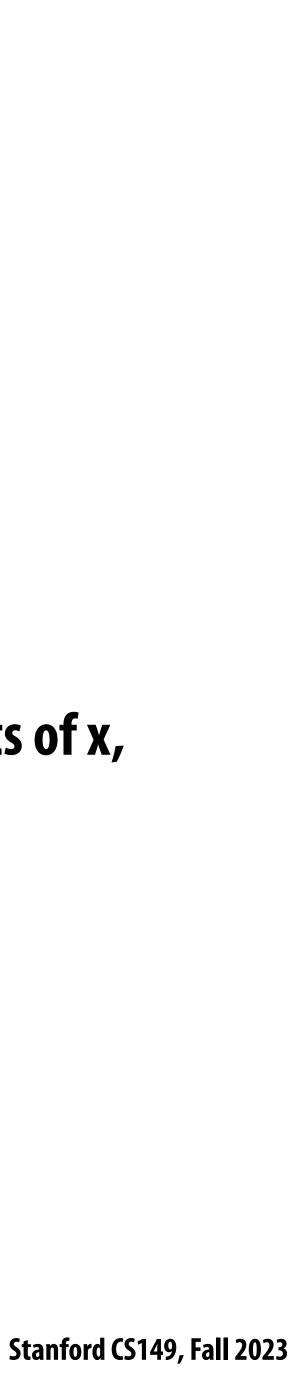


### What does this program do?

```
// main C++ code:
const int N = 1024;
float* x = new float[N/2];
float* y = new float[N];
// initialize N/2 elements of x here
// call ISPC function
absolute_repeat(N/2, x, y);
```

```
// ISPC code:
export void absolute_repeat(
  uniform int N,
  uniform float* x,
  uniform float* y)
{
  foreach (i = 0 \dots N)
   {
       if (x[i] < 0)
         y[2*i] = -x[i];
       else
         y[2*i] = x[i];
      y[2*i+1] = y[2*i];
```

### This ISPC program computes the absolute value of elements of x, then repeats it twice in the output array y



### What does this program do?

```
// main C++ code:
const int N = 1024;
float* x = new float[N];
float* y = new float[N];
// initialize N elements of x
// call ISPC function
shift_negative(N, x, y);
```

```
// ISPC code:
export void shift_negative(
   uniform int N,
  uniform float* x,
  uniform float* y)
{
  foreach (i = 0 \dots N)
   {
       if (i \ge 1 \&\& x[i] < 0)
        y[i-1] = x[i];
       else
         y[i] = x[i];
```

- The output of this program is undefined!
- Possible for multiple iterations of the loop body to write to same memory location



### **Computing the sum of all elements in an array (incorrectly)**

### What's the error in this program?

```
export uniform float sum_incorrect_1(
   uniform int N,
   uniform float* x)
{
   float sum = 0.0f;
   foreach (i = 0 \dots N)
      sum += x[i];
   return sum;
```

### sum is of type float (different variable for all program instances)

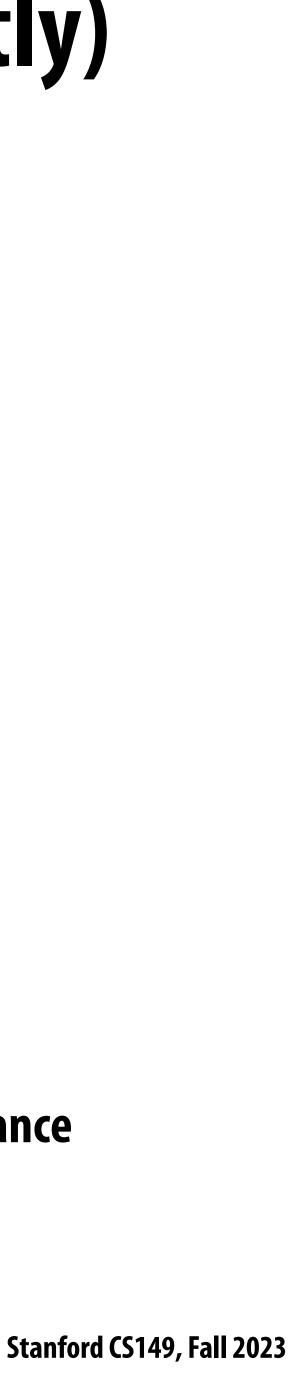
Cannot return many copies of a varianble to the calling C code, which expects one return value of type float **Result: compile-time type error** 

### What's the error in this program?

```
export uniform float sum_incorrect_2(
   uniform int N,
   uniform float* x)
   uniform float sum = 0.0f;
   foreach (i = 0 \dots N)
      sum += x[i];
   return sum;
```

#### sum is of type uniform float (one copy of variable for all program instances)

x[i] has a different value for each program instance So what gets copied into sum? **Result: compile-time type error** 



## **Computing the sum of all elements in an array (correctly)**

```
export uniform float sum_array(
   uniform int N,
   uniform float* x)
{
   uniform float sum;
   float partial = 0.0f;
   foreach (i = 0 \dots N)
   {
      partial += x[i];
   // reduce_add() is part of ISPC's cross
   // program instance standard library
   sum = reduce_add(partial);
   return sum;
```

\* Self-test: If you understand why this implementation correctly implements the semantics of the ISPC gang abstraction, then you've got a good command of ISPC

}

Each instance accumulates a private partial sum (no communication)

Partial sums are added together using the reduce\_add() cross-instance communication primitive. The result is the same total sum for all program instances (reduce\_add() returns a uniform float)

The ISPC code at left will execute in a manner similar to the C code with AVX intrinsics implemented below. \*

```
float sum_summary_AVX(int N, float* x) {
  float tmp[8]; // assume 16-byte alignment
  __mm256 partial = _mm256_broadcast_ss(0.0f);
  for (int i=0; i<N; i+=8)</pre>
    partial = _mm256_add_ps(partial, _mm256_load_ps(&x[i]));
  _mm256_store_ps(tmp, partial);
  float sum = 0.f;
  for (int i=0; i<8; i++)</pre>
    sum += tmp[i];
  return sum;
```



Stanford CS149, Fall 2023

## **ISPC's cross program instance operations**

**Compute sum of a variable's value in all program instances in a gang:** 

uniform int64 reduce\_add(int32 x);

**Compute the min of all values in a gang:** uniform int32 reduce\_min(int32 a);

**Broadcast a value from one instance to all instances in a gang:** int32 broadcast(int32 value, uniform int index);

For all i, pass value from instance i to the instance i+offset % programCount: int32 rotate(int32 value, uniform int offset);



## **ISPC:** abstraction vs. implementation

### Single program, multiple data (SPMD) programming model

- different value of programIndex)
- This is the programming <u>abstraction</u>
- **Program is written in terms of this abstraction**

### Single instruction, multiple data (SIMD) <u>implementation</u>

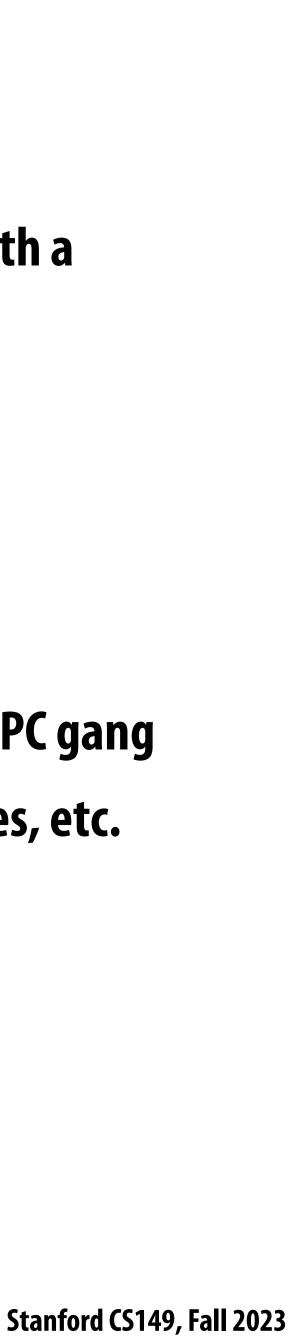
- like you do manually in assignment 1)

### Semantics of ISPC can be tricky

SPMD abstraction + uniform values (allows implementation details to peek through abstraction a bit)

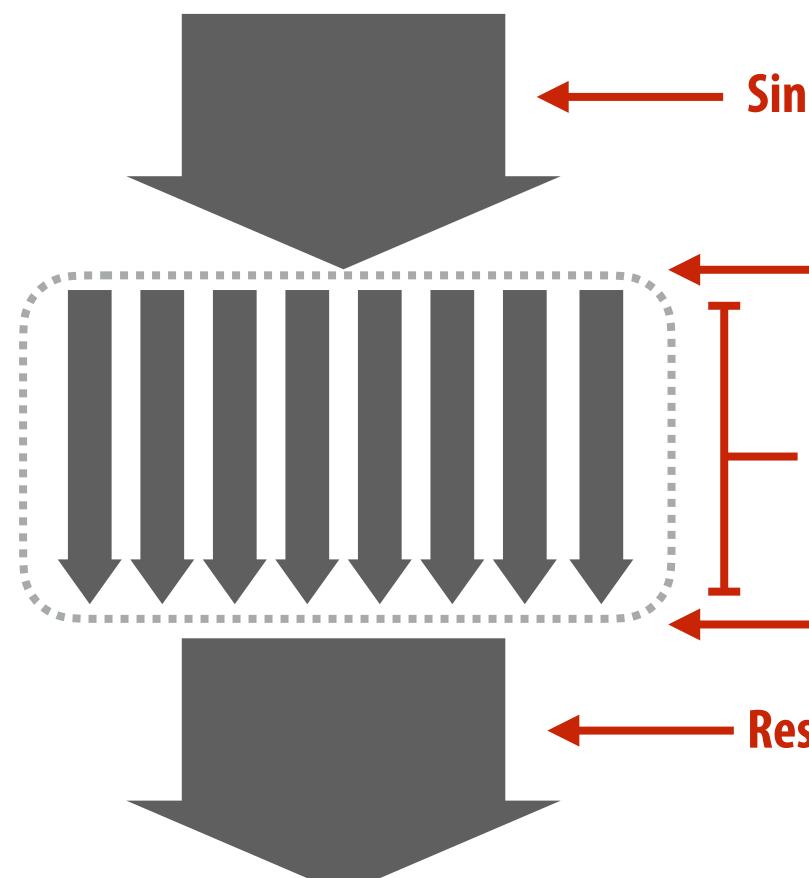
Programmer "thinks": running a gang is spawning programCount logical instruction streams (each with a

ISPC compiler emits vector instructions (e.g., AVX2, ARM NEON) that carry out the logic performed by a ISPC gang ISPC compiler handles mapping of conditional control flow to vector instructions (by masking vector lanes, etc.



## SPMD programming model summary

- SPMD = "single program, multiple data"



Define one function, run multiple instances of that function in parallel on different input arguments

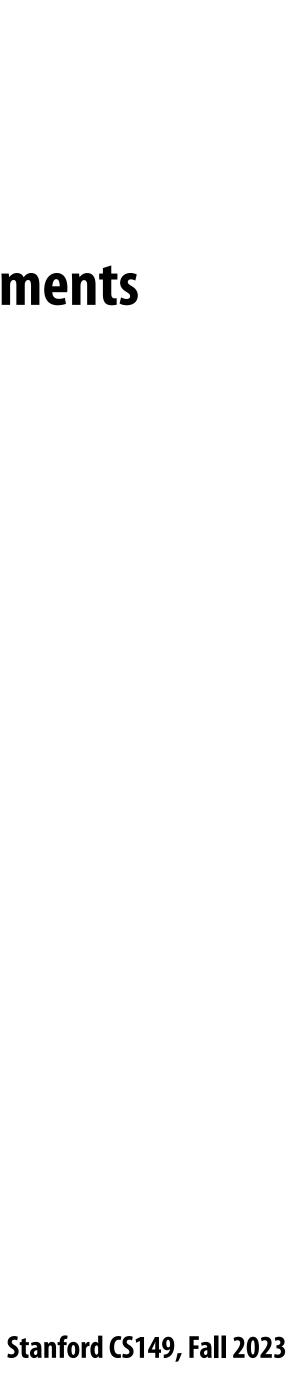
**Single thread of control** 

**Call SPMD function** 

**SPMD execution: multiple instances of function** run in parallel (multiple logical threads of control)

**SPMD function returns** 

**Resume single thread of control** 



### **ISPC** tasks

- on thread running on one x86 core of a CPU.
- of the four cores of the myth machines.
- ISPC contains another abstraction: a "task" that is used to achieve multi-core execution. I'll let you read up about that as you do assignment 1.

# The ISPC gang abstraction is implemented by SIMD instructions that execute within

So all the code I've shown you in the previous slides would have executed on only one



## Thinking about operating on data in parallel?

- In many simple cases, using ISPC foreach allows the programmer to express their program almost as if it was a sequential program
  - Almost want to explain code as: "independently, for each element in the input array... do this..."
- **Exceptions:** 
  - **Uniform variables**
  - **Cross-instance operations (in standard library, like reduceAdd)**
- But ISPC is a low-level programming language: by exposing programIndex and programCount, it allows programmer to define what work each program instance does and what data each instance accesses
  - Can implement programs with undefined output
  - Can implement programs that are correct only for a specific programCount

```
export void ispc_function(
   uniform int
                  Ν,
   uniform float* x,
   uniform float* y)
{
   foreach (i = 0 ... N)
     float val = x[i];
     float result;
     // do work here to compute
     // result from val
     y[i] = result;
```



### But can express very advanced cooperation

```
// compute the product of all eight elements in the
// input array. Assumes the gang size is 8.
export void vec8product(
   uniform float* x,
  uniform float* result)
  float val1 = x[programIndex];
   float val2 = shift(val1, -1);
  if (programIndex % 2 == 0)
     val1 = val1 * val2;
   val2 = shift(val1, -2);
   if (programIndex % 4 == 0)
      val1 = val1 * val2;
   }
   val2 = shift(val1, -4);
   if (programIndex % 8 == 0) {
      *result = val1 * val2
```

Here's a program that computes the product of all elements of an array in lg(8) = 3 steps

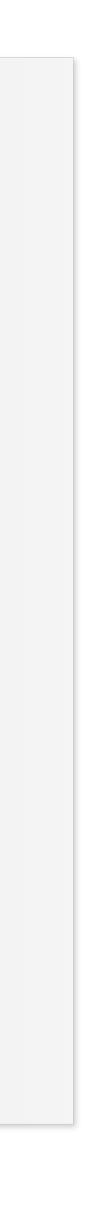


## But what if ISPC was not trying to be a low-level language?

- Example: change language so there is no access to programIndex, programCount
- Expect programmer to just use foreach
- Now there's very little need to think about program instances at all.
  - **Everything outside a foreach must be uniform** values and uniform logic. Why?

```
export void ispc_function(
   int
          N,
  float* x,
  float* y)
  int twoN = 2 * N;
   foreach (i = 0 \dots twoN)
     float val = x[i];
     float result;
     // do work here to compute
     // result from val
     y[i] = result;
```



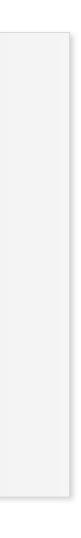


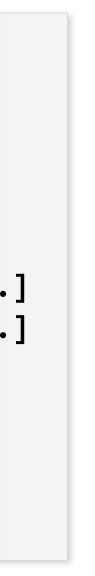
### **Another alternative**

- Don't even allow array indexing!
- Invoke computation once per element of a "collection" data structure
- Programmer writes no loops, performs no data indexing
- This model should be very family to NumPy, PyTorch, etc. programmers, right?
- Much more on this to come

```
float dowork(float x) {
  // do work here to compute
  // result from x
Collection x; // data structure of N
// invoke doWork for all elements of x,
// placing results in collection y
Collection y = map(doWork, x, y);
```

```
import numpy as np
def addOne(i):
    return i+1
mapAddOne = np.vectorize(addOne);
X = np.arange(15) # create numPy array [0, 1, 2, 3, ...]
Y = np.arange(15) \# create numPy array [0, 1, 2, 3, ...]
                        \# Z = [0, 2, 4, 6, ...]
Z = X + Y;
Zplus1 = mapAddOne(Z); # Zplus1 = [1, 3, 5, 7, ...]
```







## Summary

Programming models provide a way to think about the organization of parallel programs.

They provide <u>abstractions</u> that permit multiple valid <u>implementations</u>.

I want you to always be thinking about abstraction vs. implementation for the remainder of this course.

