Lecture 14: Image Compression and Basic Image Processing

Interactive Computer Graphics Stanford CS248, Winter 2021

A few words on color

Recall from last time: RGB color space

Color defined by 3D point in space defined by red, green, and blue primaries.

blue = (0,0,1)

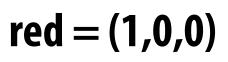
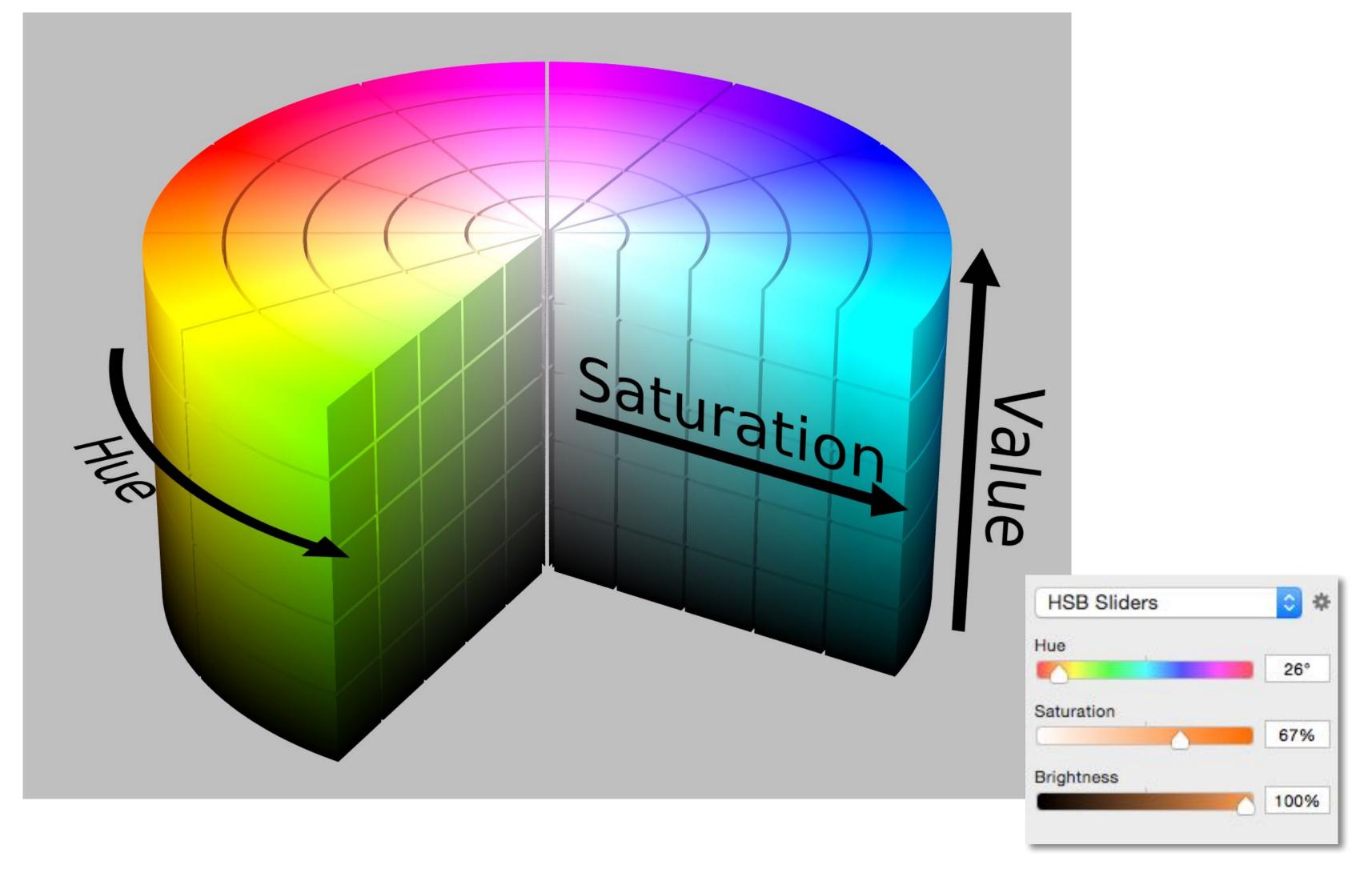


Image credit: https://forum.luminous-landscape.com/index.php?topic=37695

green = (0,1,0)

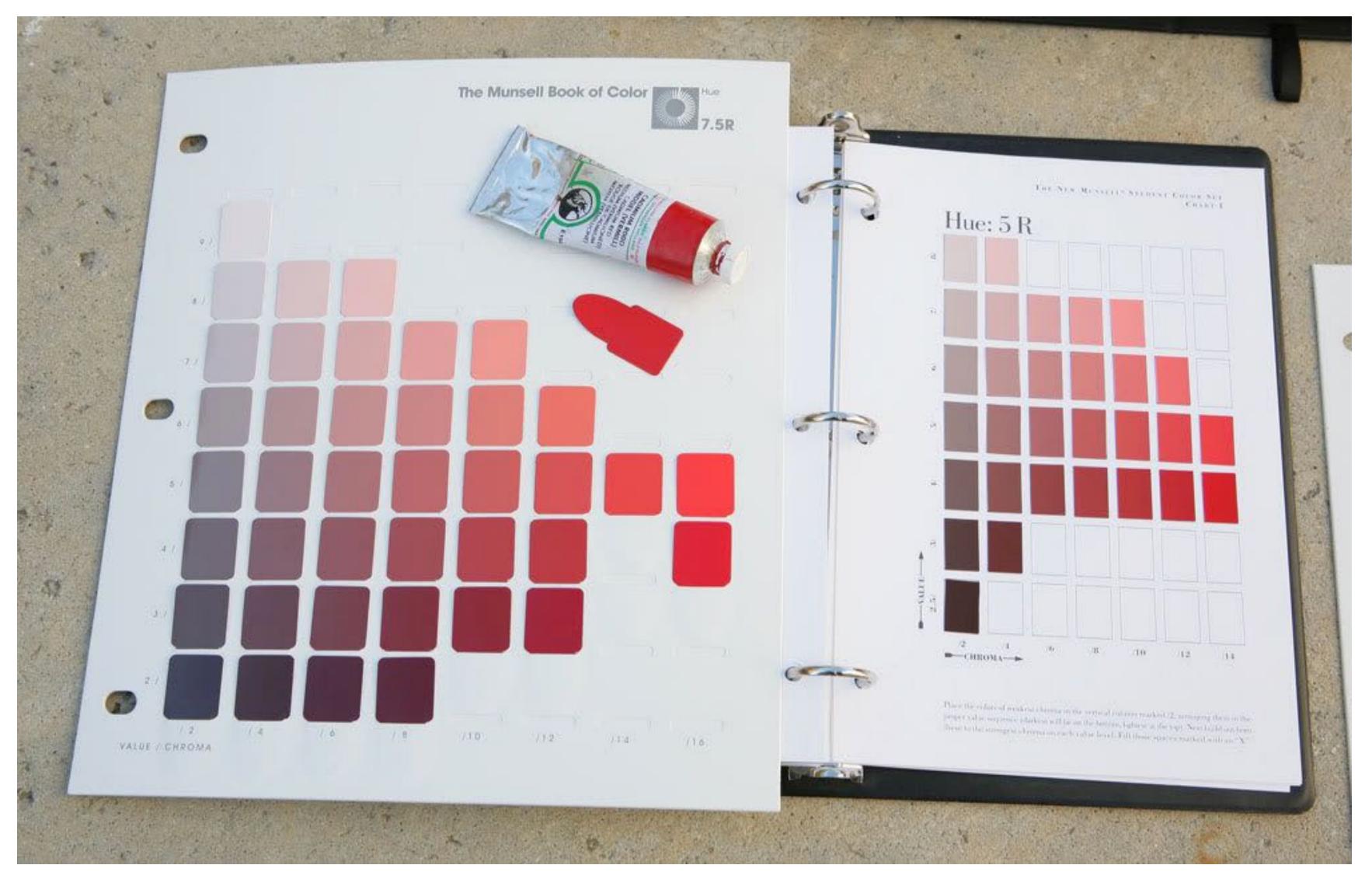
Another color space: HSV (hue-saturation-value)

Axes of space correspond to natural notions of "characteristics" of color



Stanford CS248, Winter 2021

Munsell book of color



Swatch identified by three numbers: hue, value (lightness), and chroma (color purity)

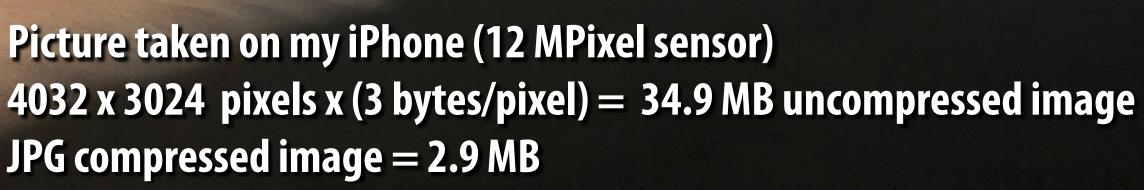
Recurring themes in the course Choosing the right representation for a task

- - e.g., choosing the right basis
- **Exploiting human perception for computational efficiency**
 - Errors/approximations in algorithms can be tolerable if humans do not notice
- Convolution as a useful operator
 - To remove high frequency content from images
 - What else can we do with convolution?

Image Compression

A recent sunset in Half Moon Bay

Picture taken on my iPhone (12 MPixel sensor) JPG compressed image = 2.9 MB



Review from last time

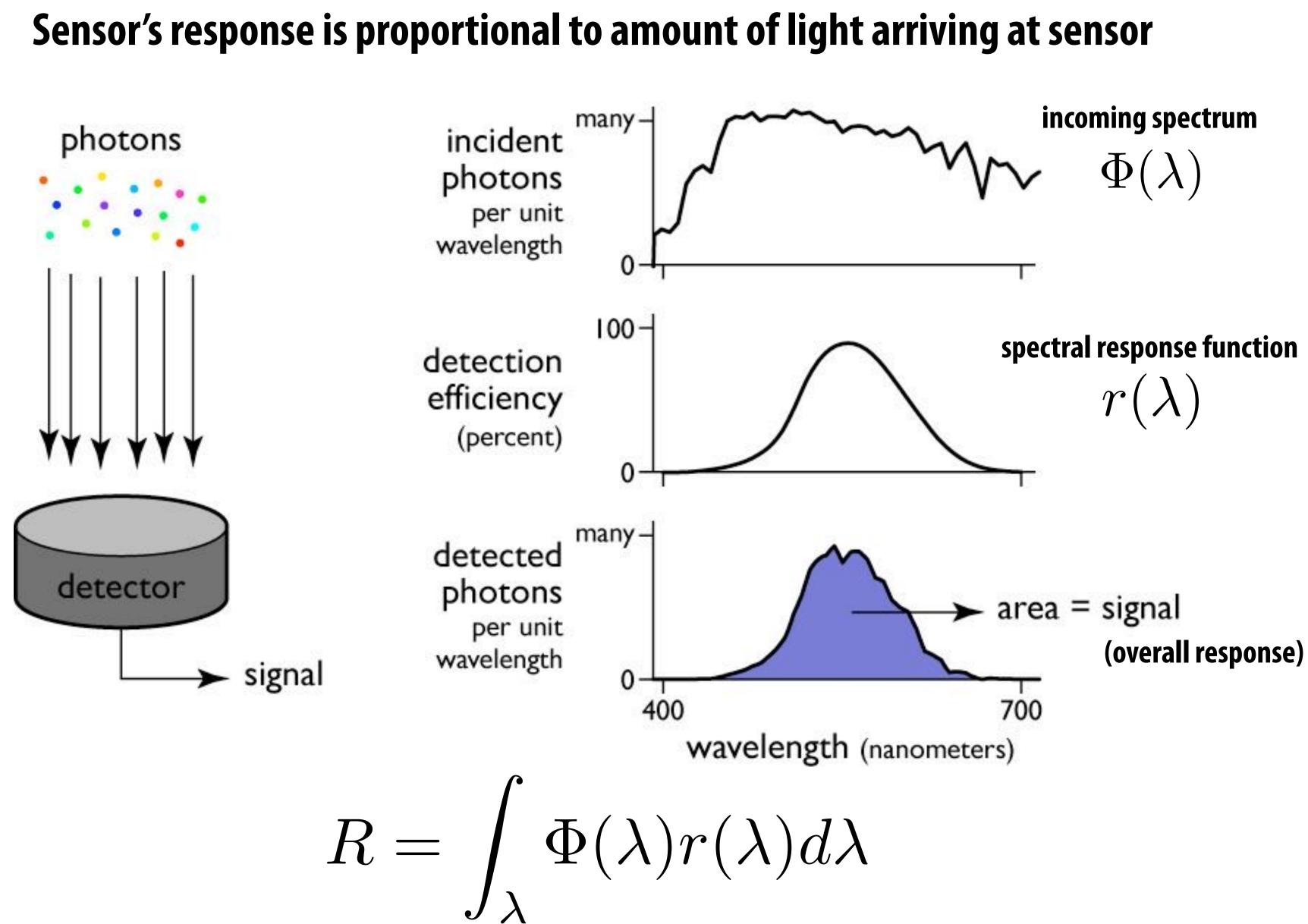


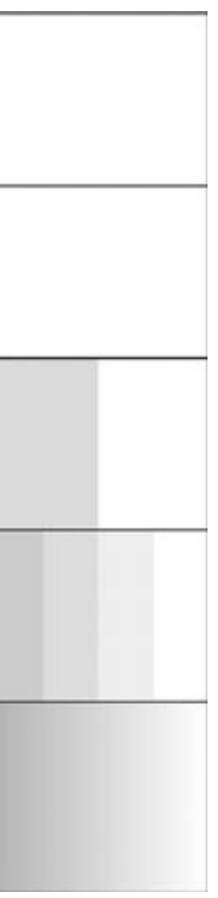
Figure credit: Steve Marschner

Encoding numbers

- More bits \rightarrow can represent more unique numbers
- 8 bits \rightarrow 256 unique numbers (0-255)

1 bit	
2 bit	
3 bit	
4 bit	
8 bit	

[Credit: lambert and waters]



Idea 1:

- What is the most efficient way to encode intensity values as a byte?
- Idea: encode based on how the brain *perceived brightness*, not based on the response of eye

Luminance (brightness)

Product of radiance and the eye's luminous efficiency

$$Y = \int \Phi(\lambda) V(\lambda) \, \mathrm{d}\lambda$$

Luminous efficiency is measure of how bright light at a given wavelength is perceived by a human (due to the eye's response to light at that wavelength)



Adjust power of monochromatic light source of wavelength λ until it matches the brightness of reference 555 nm source (photopic case)

0.9

0.8

0.7

0.6

0.5

0.4

0.3

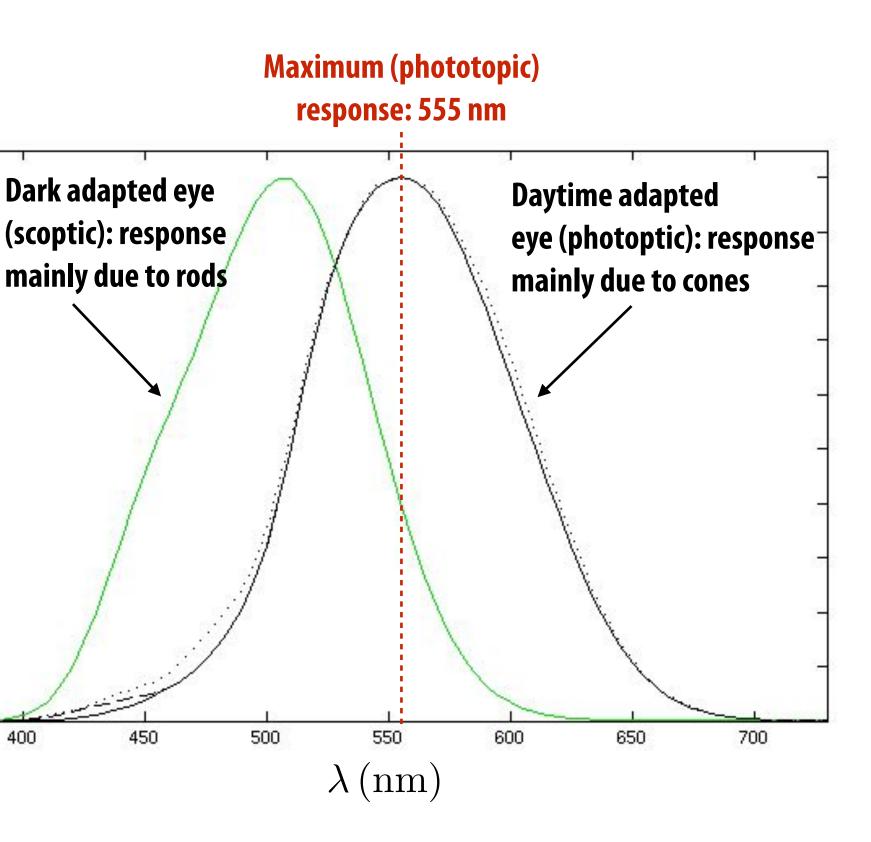
0.2

0.1

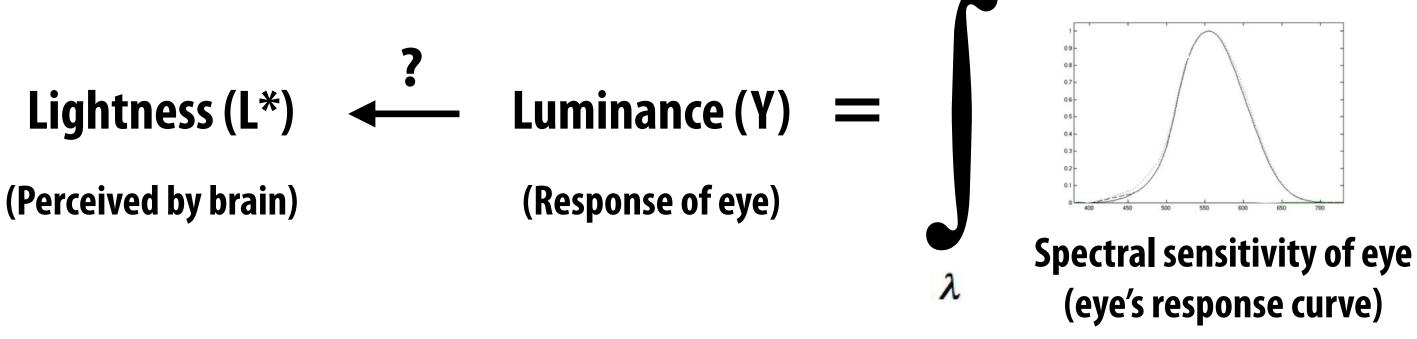
400

 $V(\lambda)$

Notice: the sensitivity of photopic eye is maximized at ~ 555 nm



Lightness (<u>perceived</u> brightness) aka luma



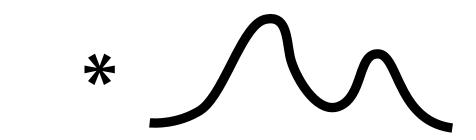
Dark adapted eye: $L^* \propto Y^{0.4}$

Bright adapted eye: $L^{*} \propto Y^{0.5}$

In a dark room, you turn on a light with luminance: Y_1 You turn on a second light that is identical to the first. Total output is now: $Y_2 = 2Y_1$

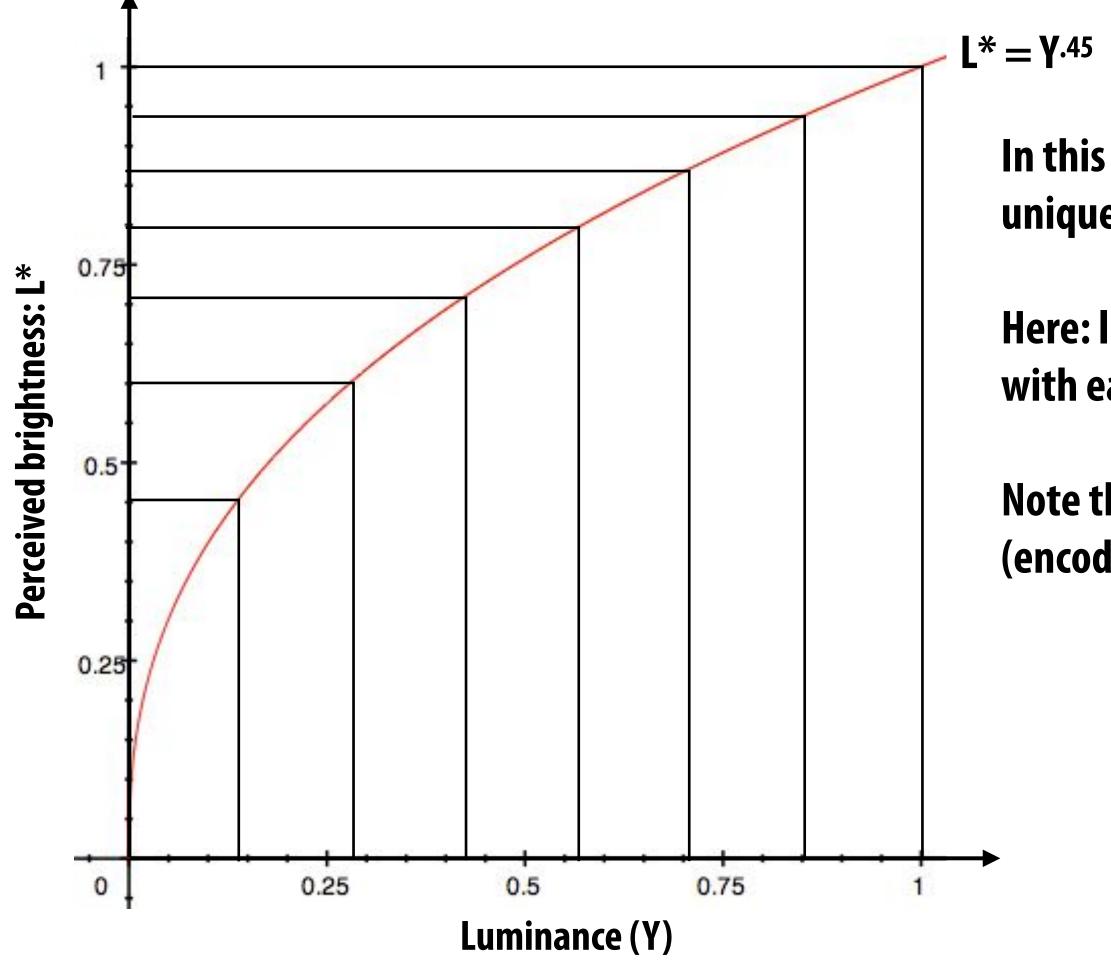
Total output appears $2^{0.4} = 1.319$ times brighter to dark-adapted human

Note: Lightness (L*) is often referred to as luma (Y')



Radiance (energy spectrum from scene)

Consider an image with pixel values encoding luminance (linear in energy hitting sensor)



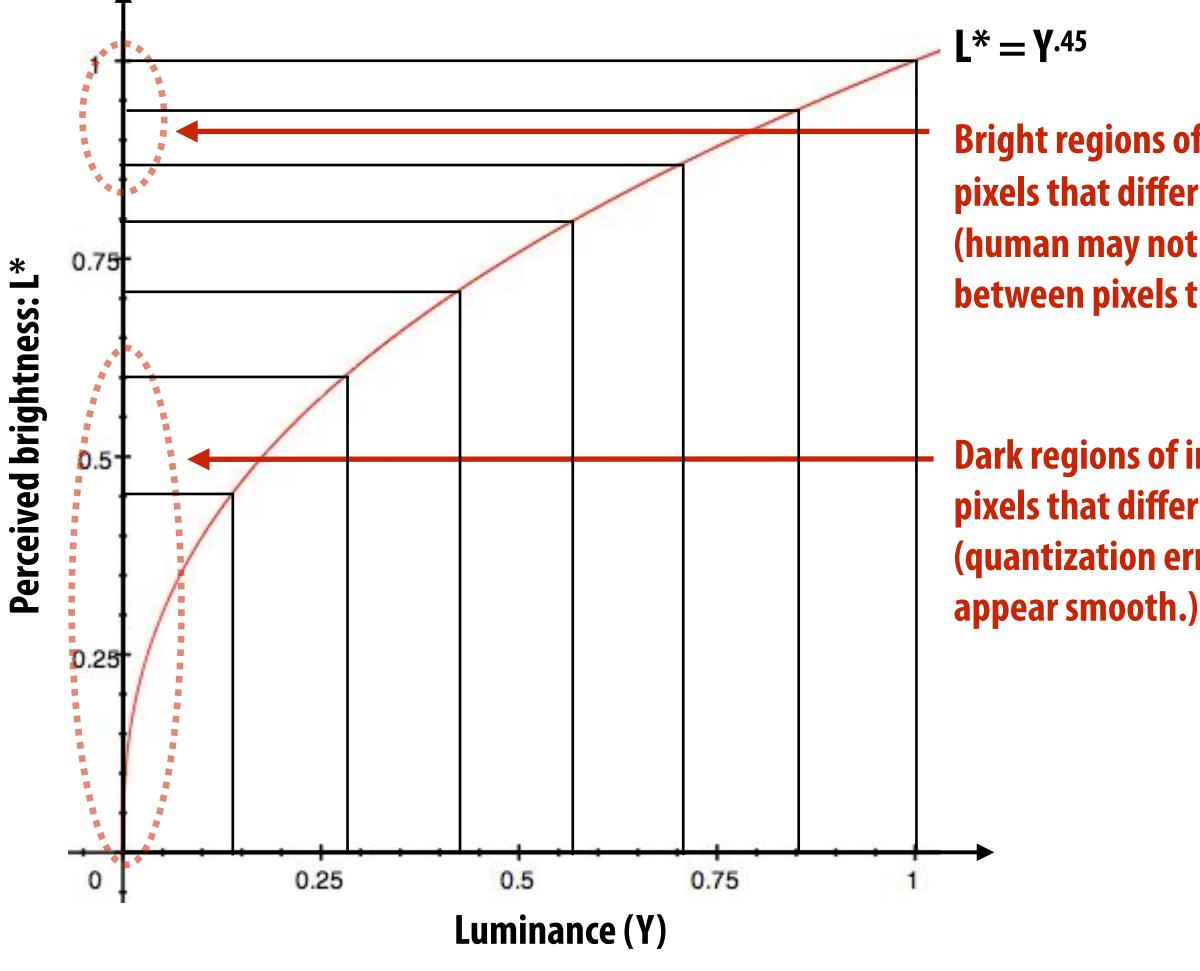
In this visualization: Pixel can represent 8 unique luminance values (3-bits/pixel)

Here: lines indicate luminance associated with each unique pixel value

Note that pixels are linear in luminance (encode equally spaced sensor responses)

Problem: quantization error

Many common image formats store 8 bits per channel (256 unique values) Insufficient precision to represent brightness in darker regions of image



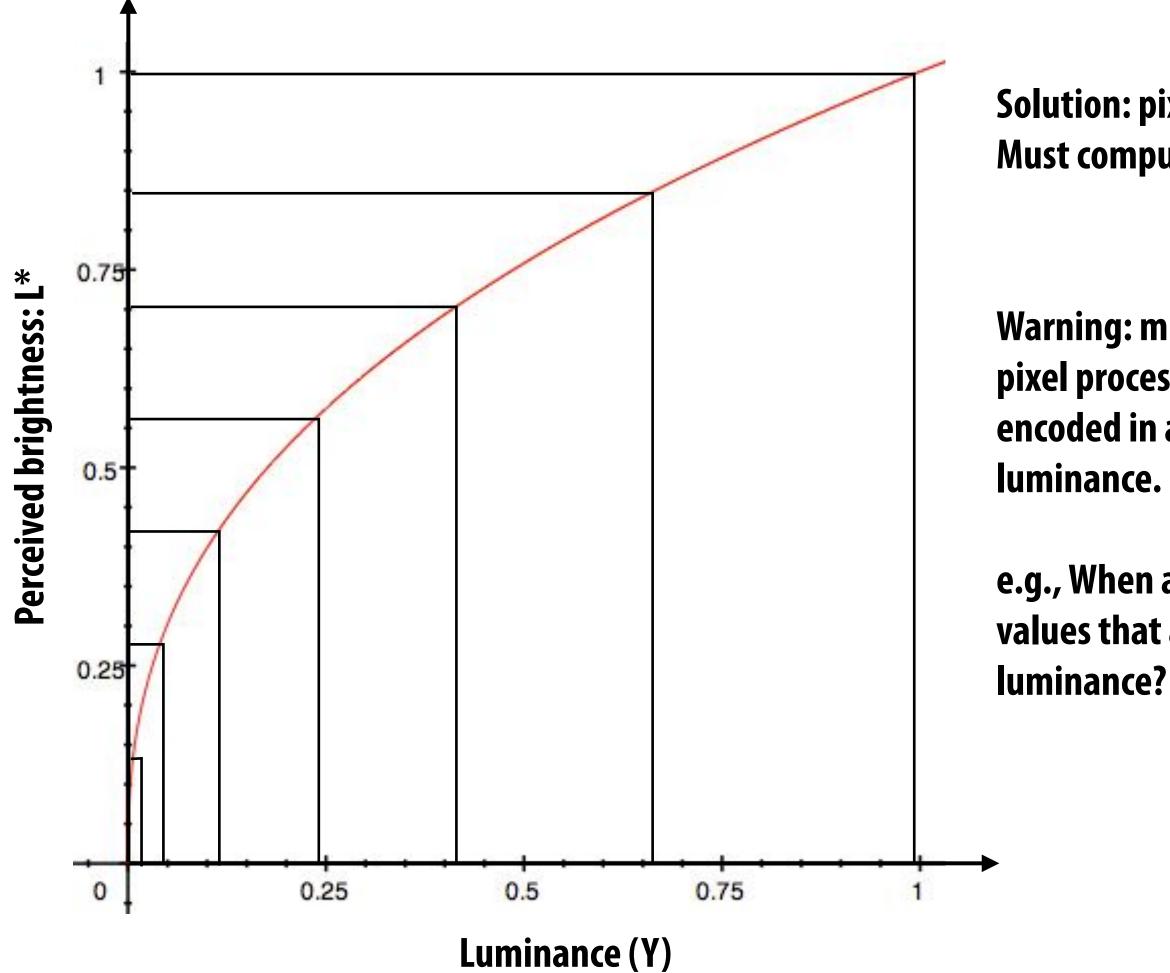
Rule of thumb: human eye cannot differentiate <1% differences in luminance

Bright regions of image: perceived difference between pixels that differ by one step in luminance is small! (human may not even be able to perceive difference between pixels that differ by one step in luminance!)

Dark regions of image: perceived difference between pixels that differ by one step in luminance is large! (quantization error: gradients in luminance will not

Store lightness, not luminance

Idea: distribute representable pixel values evenly with respect to lightness (perceived brightness), not evenly in luminance (make more efficient use of available bits)



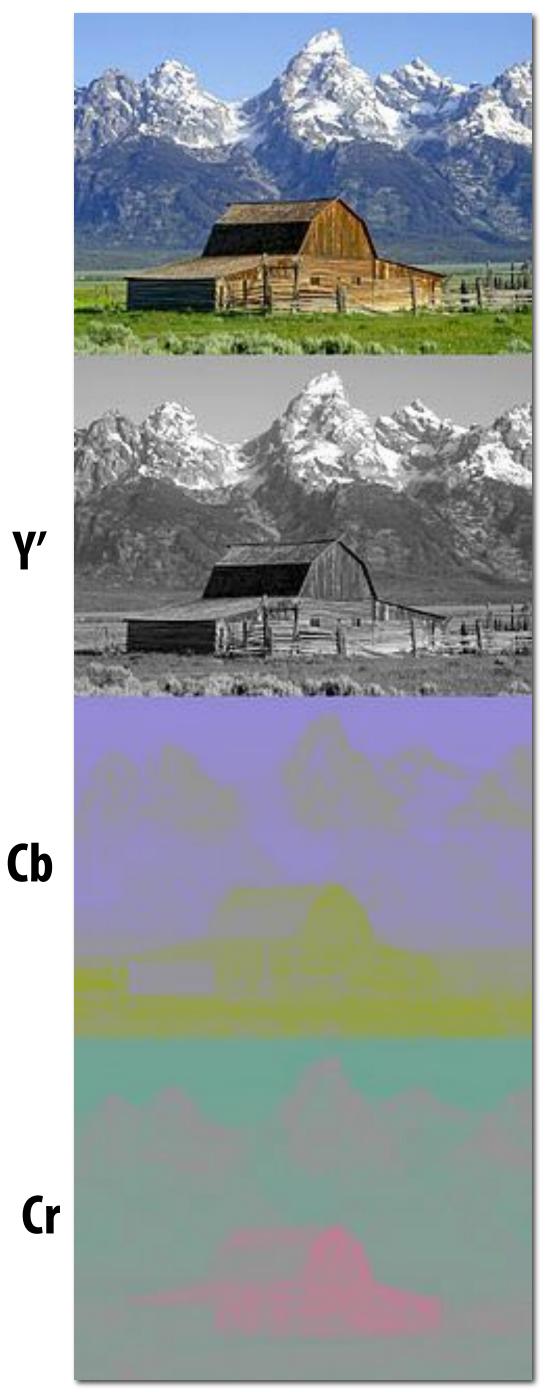
Solution: pixel stores Y^{0.45} Must compute (pixel_value)^{2,2} prior to display on LCD

Warning: must take caution with subsequent pixel processing operations once pixels are encoded in a space that is not linear in

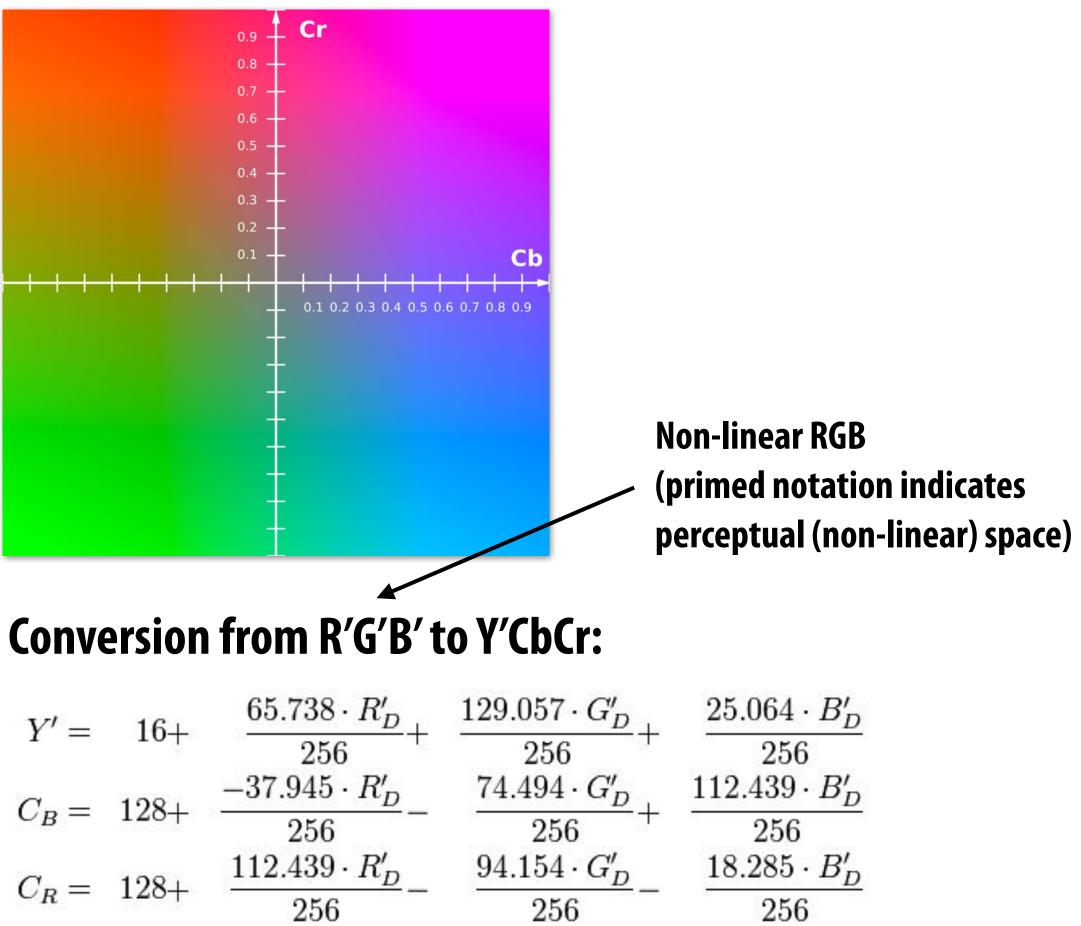
e.g., When adding images should you add pixel values that are encoded as lightness or as

Idea 2:

- Chrominance ("chroma") subsampling
- The human visual system is less sensitive to detail in chromaticity than in luminance
 - So it is sufficient to sample chroma more sparsely in space



Y'CbCr color space Y' = luma: perceived luminance (non-linear) **Cb** = **blue-yellow deviation from gray** Cr = red-cyan deviation from gray



Y' =	16 +	$\frac{65.738\cdot R_I'}{256}$
$C_B =$	128 +	$\frac{-37.945 \cdot R_I'}{256}$
$C_R =$	128 +	$\frac{112.439\cdot R_I'}{256}$

Image credit: Wikipedia



Original picture of Kayvon



Contents of CbCr color channels downsampled by a factor of 20 in each dimension (400x reduction in number of samples)



Full resolution sampling of luma (Y')



Reconstructed result (looks pretty good)

Chroma subsampling

Y'CbCr is an efficient representation for storage (and transmission) because Y' can be stored at higher resolution than CbCr without significant loss in perceived visual quality

Y' ₀₀ Cb ₀₀ Cr ₀₀	Y' ₁₀	Y' ₂₀ Cb ₂₀ Cr ₂₀	Y′ ₃₀
Y′ ₀₁ Cb ₀₁ Cr ₀₁	Υ′ ₁₁	Y' ₂₁ Cb ₂₁ Cr ₂₁	Y′ 31

Y'00 **Cb**₀₀ **Cr**₀₀ **Y**'₀₁

4:2:2 representation:

Store Y' at full resolution Store Cb, Cr at full vertical resolution, but only half horizontal resolution

X:Y:Z notation:

- X = width of block
- Y = number of chroma samples in first row
- Z = number of chroma samples in second row

dimensions

Real-world 4:2:0 examples:

most JPG images and H.264 video

Y′ ₁₀	Y' ₂₀ Cb ₂₀ Cr ₂₀	Y′ ₃₀
Y′ ₁₁	Υ′ ₂₁	Y′ ₃₁

4:2:0 representation:

Store Y' at full resolution Store Cb, Cr at half resolution in both

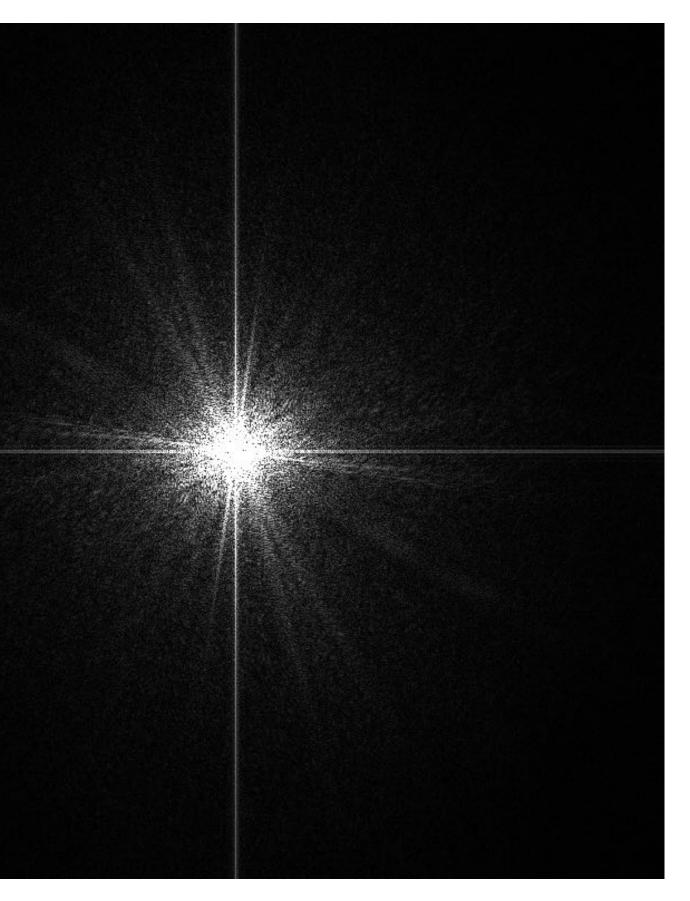
Idea 3:

- Low frequency content is predominant in the real world
- The human visual system is less sensitive to high frequency sources of error in images
- So a good compression scheme needs to accurately represent lower frequencies, but it can be acceptable to sacrifice accuracy in representing higher frequencies

Recall: frequency content of images



Spatial domain result

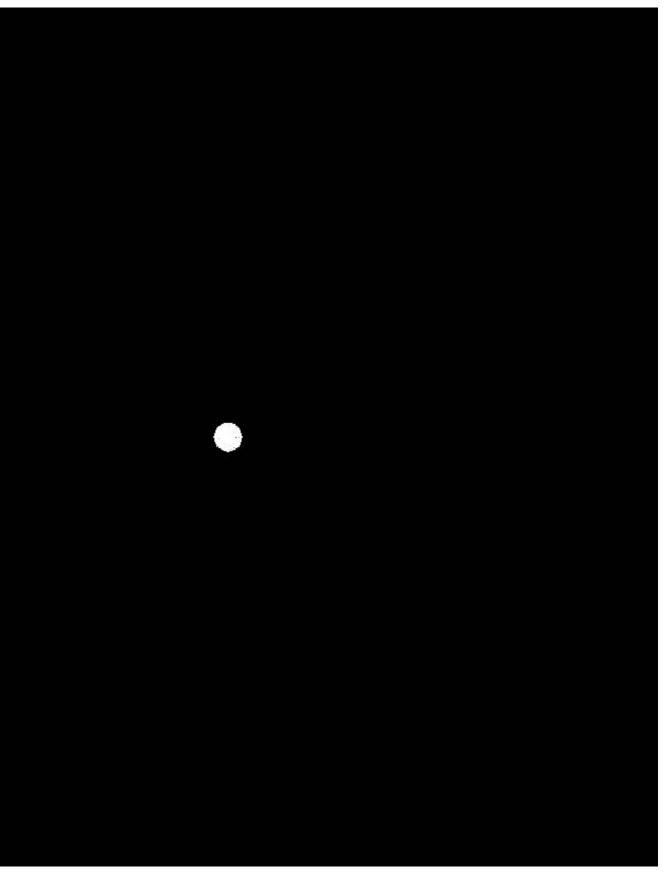


Spectrum

Recall: frequency content of images

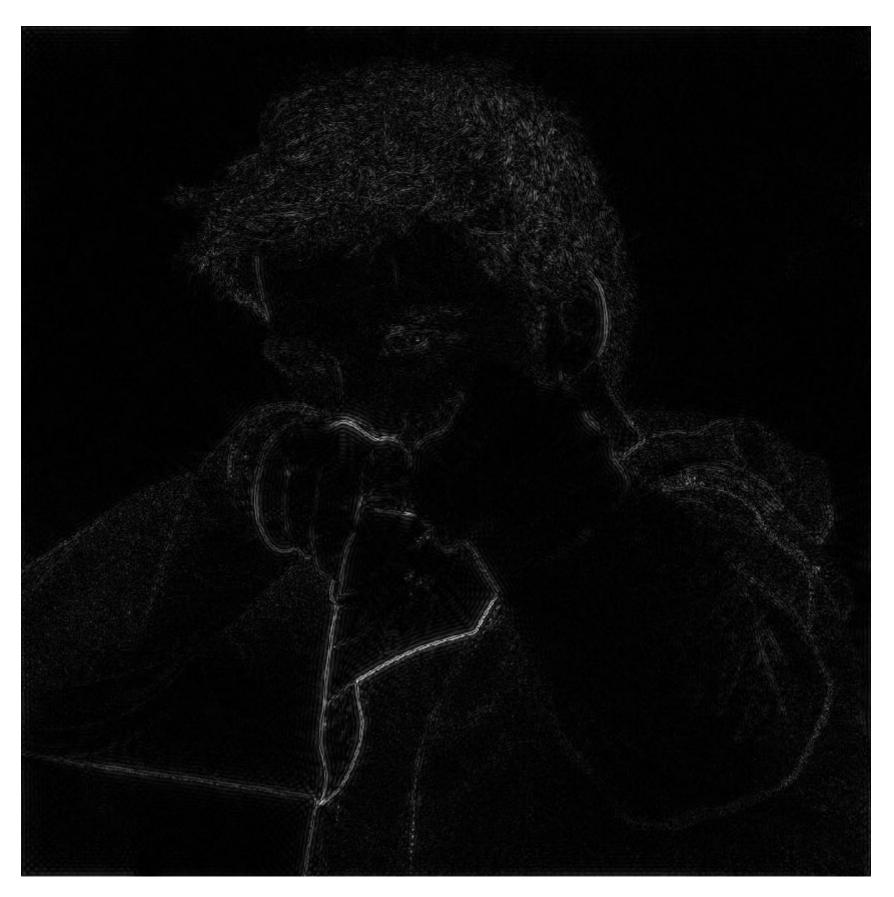


Spatial domain result

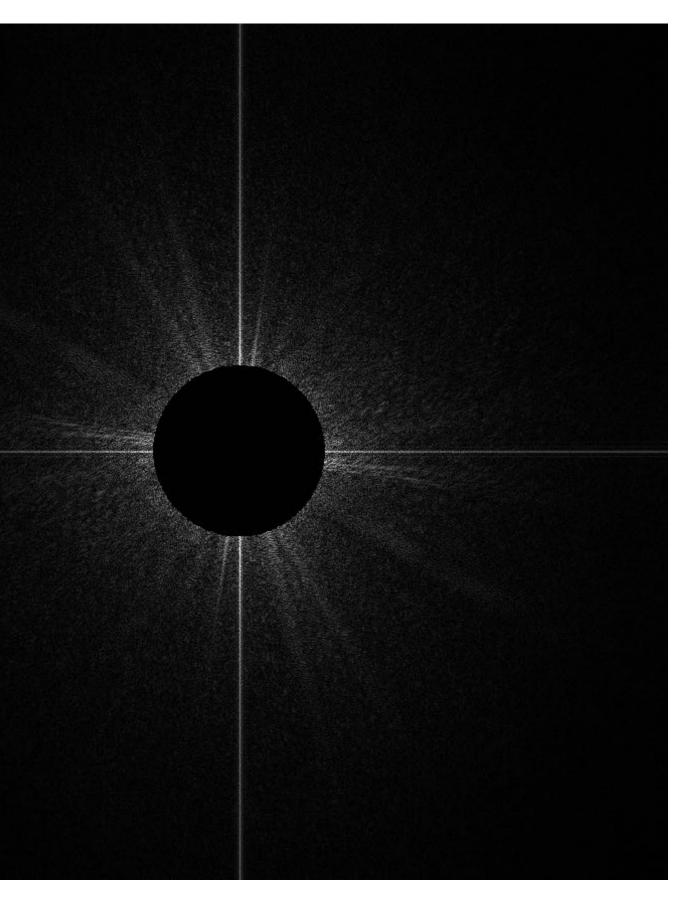


Spectrum (after low-pass filter) All frequencies above cutoff have 0 magnitude

Recall: frequency content of images



Spatial domain result (strongest edges)



Spectrum (after high-pass filter) All frequencies below threshold have 0 magnitude

A recent sunset in Half Moon Bay



A recent sunset in Half Moon Bay (with noise added)



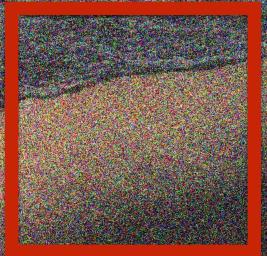
A recent sunset in Half Moon Bay (with more noise added)



A recent sunset in Half Moon Bay

Original image

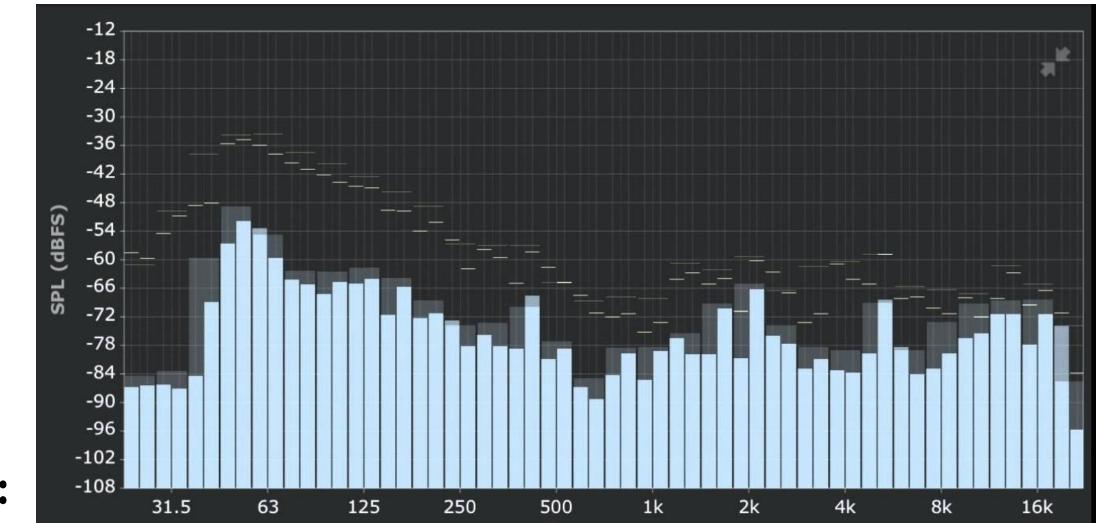
Noise added (increases high frequency content)





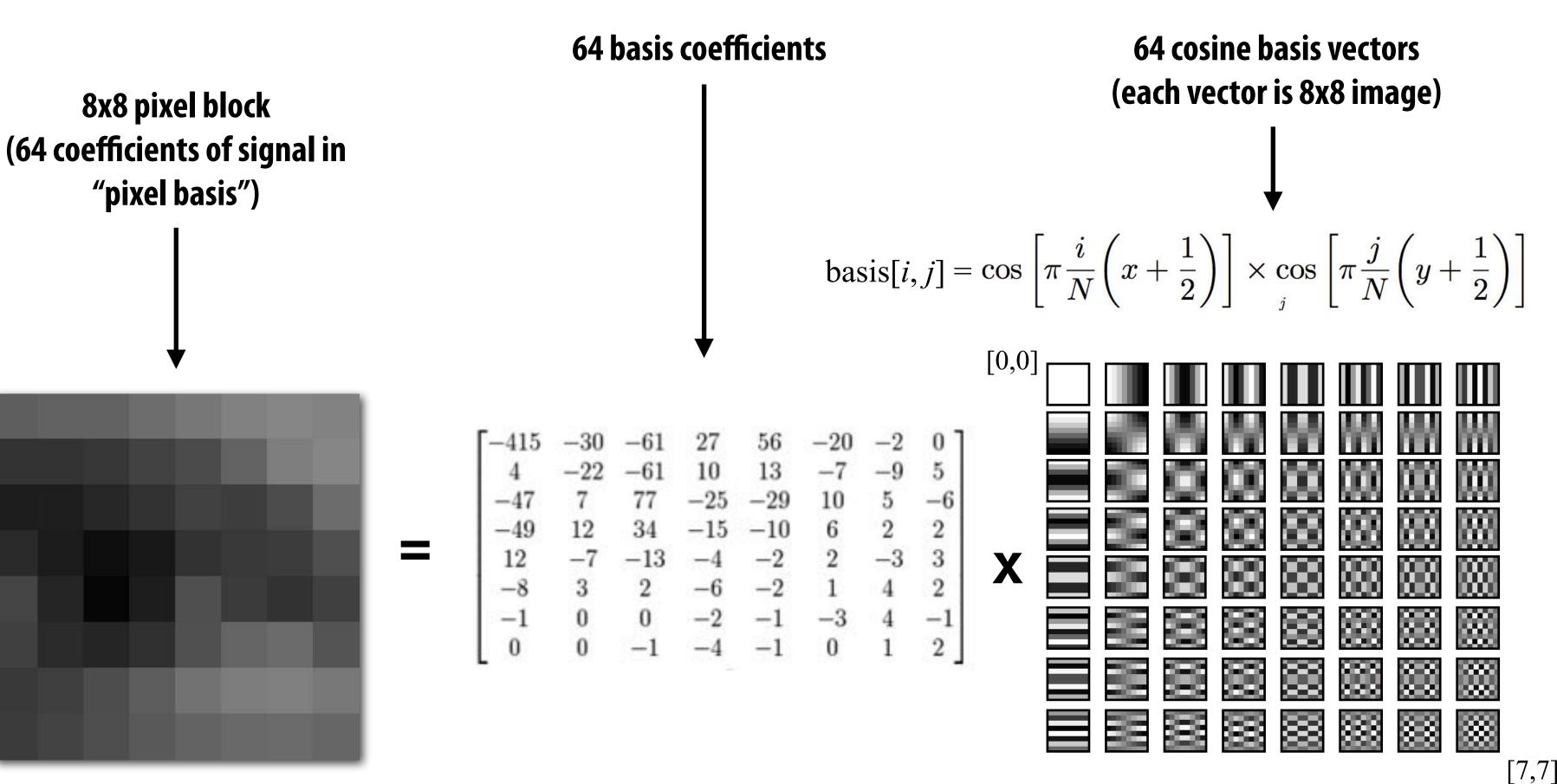
More noise added

What is a good representation for manipulating frequency content of images?



Hint:

Image transform coding via discrete cosign transform (DCT)

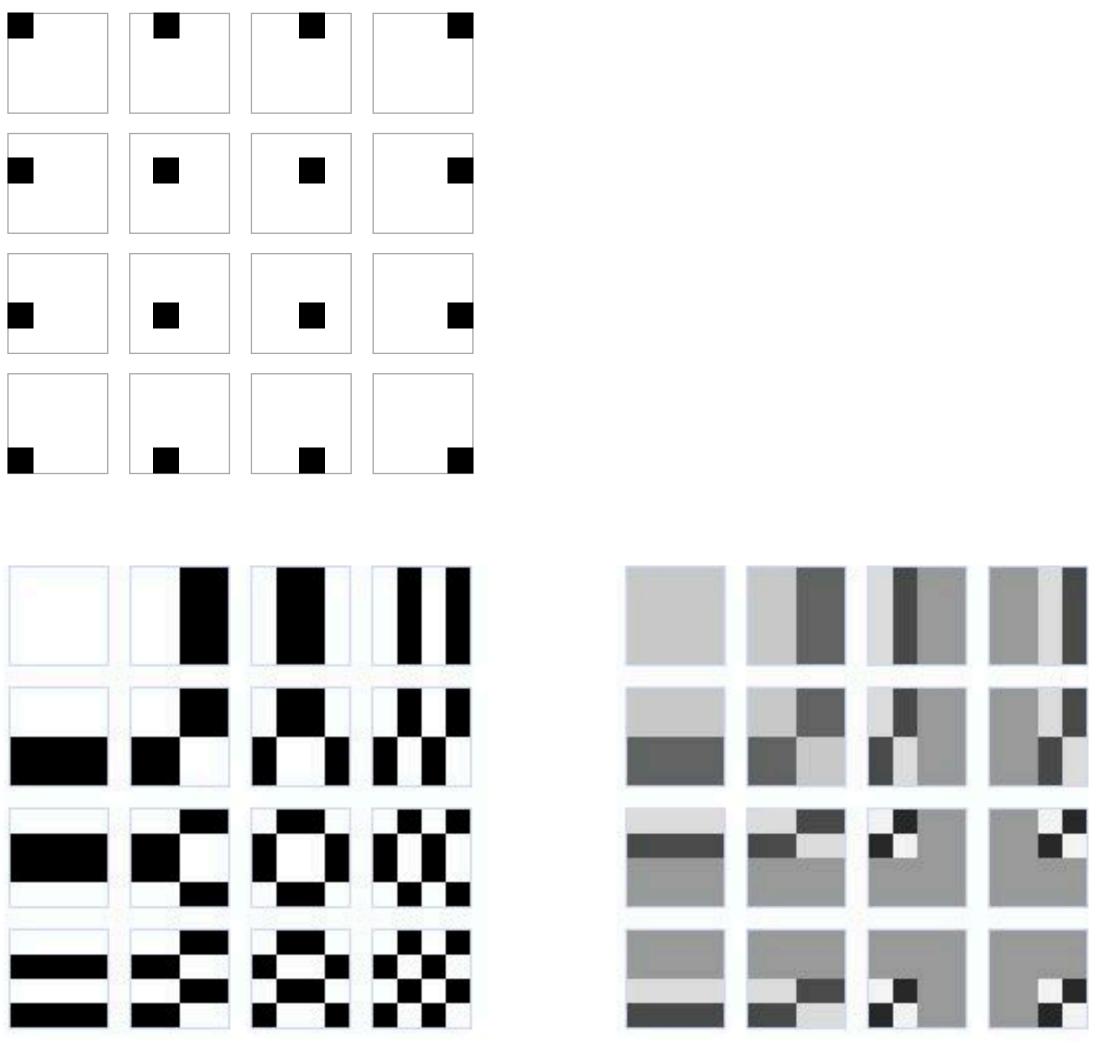


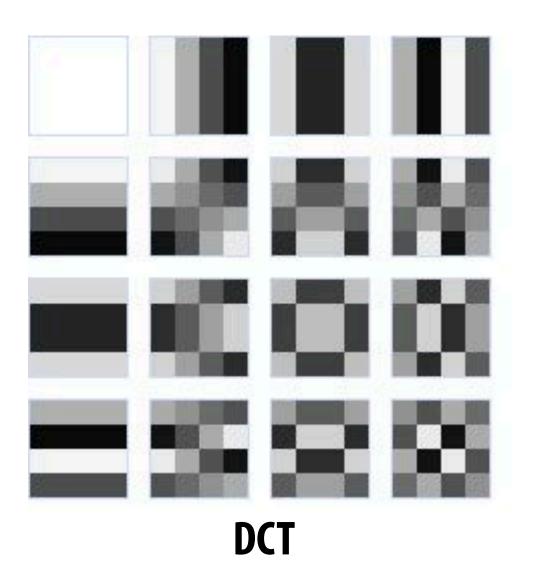
In practice: DCT applied to 8x8 pixel blocks of Y' channel, 16x16 pixel blocks of Cb, Cr (assuming 4:2:0)

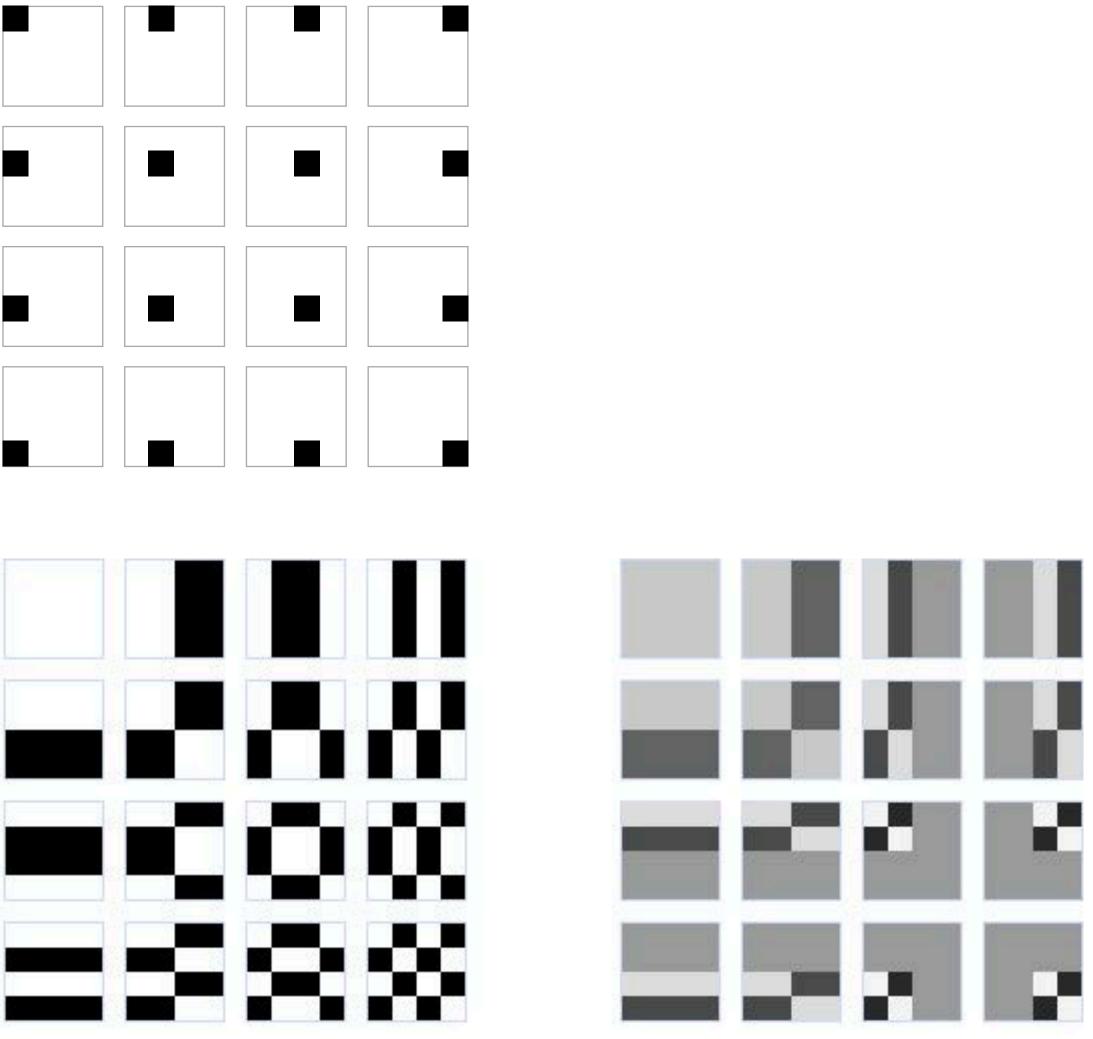
Examples of other bases

This slide illustrates basis images for 4x4 block of pixels (although JPEG works on 8x8 blocks)

Pixel Basis (Compact: each coefficient in representation only effects a single pixel of output)







Walsh-Hadamard

[Image credit: https://people.xiph.org/~xiphmont/demo/daala/demo3.shtml]

Haar Wavelet

Quantization

-415	-30	-61	27	56	-20	-2	0]
4	-22	-61	10	13	-7	-9	
-47	7			-29	10	5	-6
-49	12	34	-15	-10	6	2	2
12	-7	-13	-4	-2	2	-3	3
-8	3	2	-6	-2	1	4	2
-1	0	0		$^{-1}$	-3	4	-1
0	0	-1	-4	-1	0	1	2

Result of DCT (representation of image in cosine basis)

	$\begin{bmatrix} -26 \\ 0 \\ -3 \\ -4 \\ 1 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$	-3	-6	2	2	-1	0	0]
	0	-2	-4	1	1	0	0	0
	-3	1	5	$^{-1}$	-1	0	0	0
	-4	1	2	-1	0	0	0	0
-	1	0	0	0	0	0	0	0
	0	0	0	0	0	0	0	0
	0	0	0	0	0	0	0	0
	0	0	0	0	0	0	0	0

Quantization Matrix

elements in quantization matrix)



Quantization produces small values for coefficients (only few bits needed per coefficient) Quantization zeros out many coefficients

[Credit: Wikipedia, Pat Hanrahan]

24	40	51	61
26	58	60	55
40	57	69	56
51	87	80	62
68	109	103	77
81	104	113	92
103	121	120	101
112	100	103	99

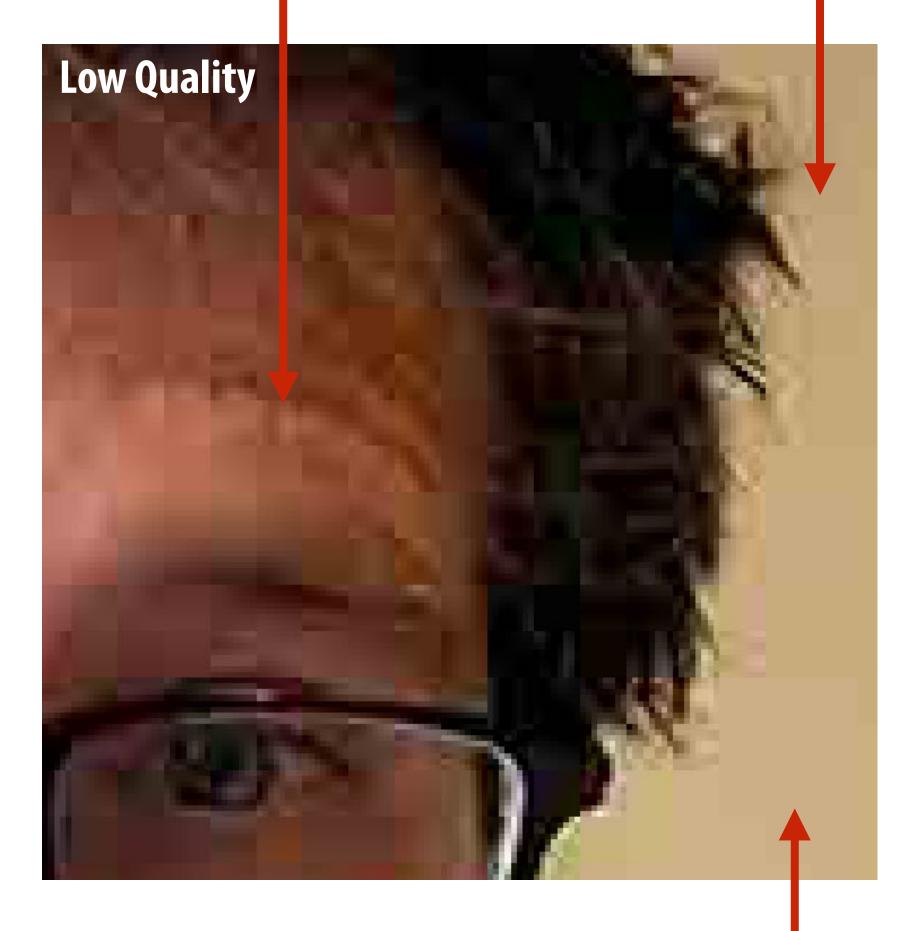
Changing JPEG quality setting in your favorite photo app modifies this matrix ("lower quality" = higher values for

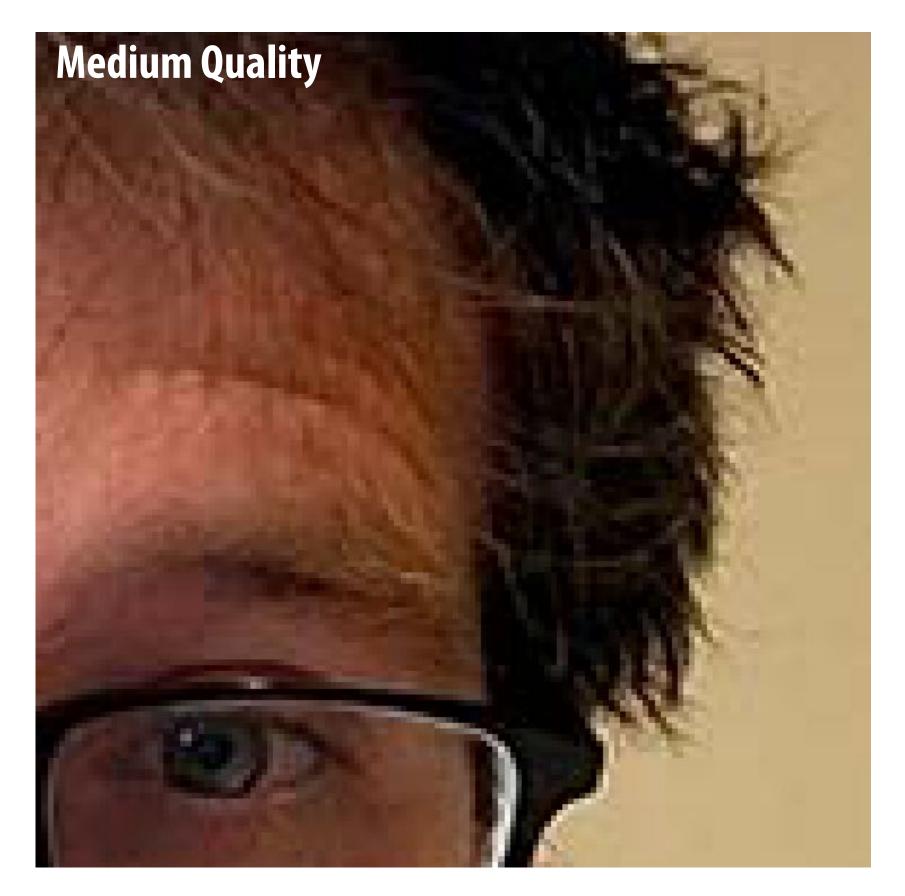
	JPEG Options	
latte:	None	ОК
- Imag	e Options	Cancel
Quality	y: 9 High ᅌ	Preview
small file	large file	836.3K

JPEG compression artifacts

Noticeable 8x8 pixel block boundaries

Noticeable error near high gradients





Low-frequency regions of image represented accurately even under high compression



JPEG compression artifacts



Original Image (actual size)



Original Image



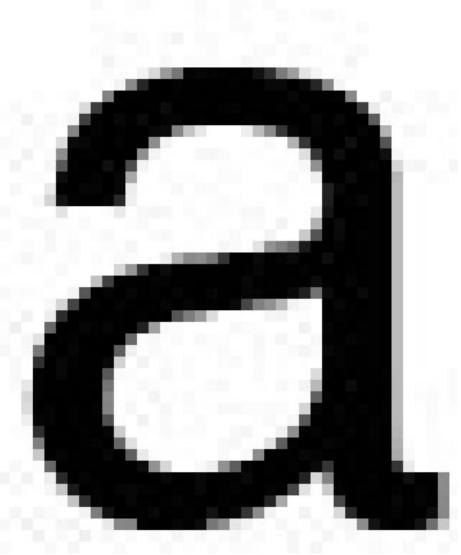
Quality Level 9



Quality Level 3



Quality Level 1



Quality Level 6

Why might JPEG compression not be a good compression scheme for illustrations and rasterized text?



ratios. Why?

Original image: 2.9MB JPG





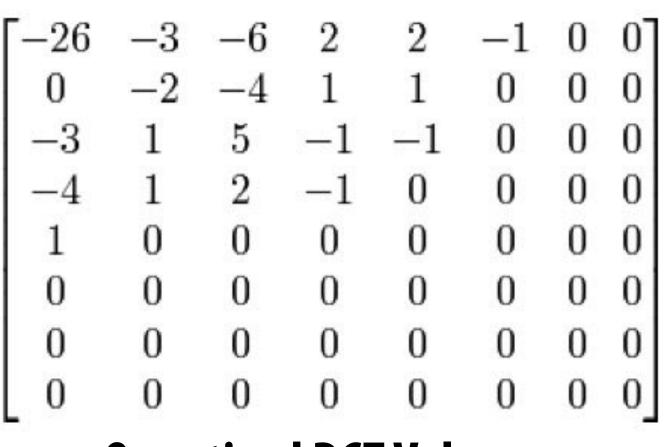
High noise: 28.9 MB JPG **Photoshop JPG compression level = 10** used for all compressed images

Uncompressed image: 4032 x 3024 x 24 bytes/pixel = 36.6 MB

Images with high frequency content do not exhibit as high compression

Medium noise: 22.6 MB JPG

Lossless compression of quantized DCT values



Quantized DCT Values

Entropy encoding: (lossless) Reorder values Run-length encode (RLE) 0's Huffman encode non-zero values

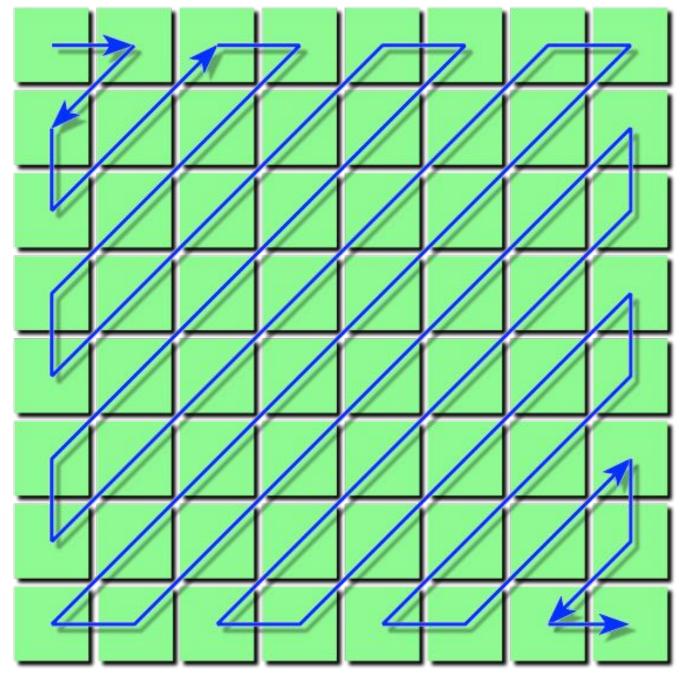
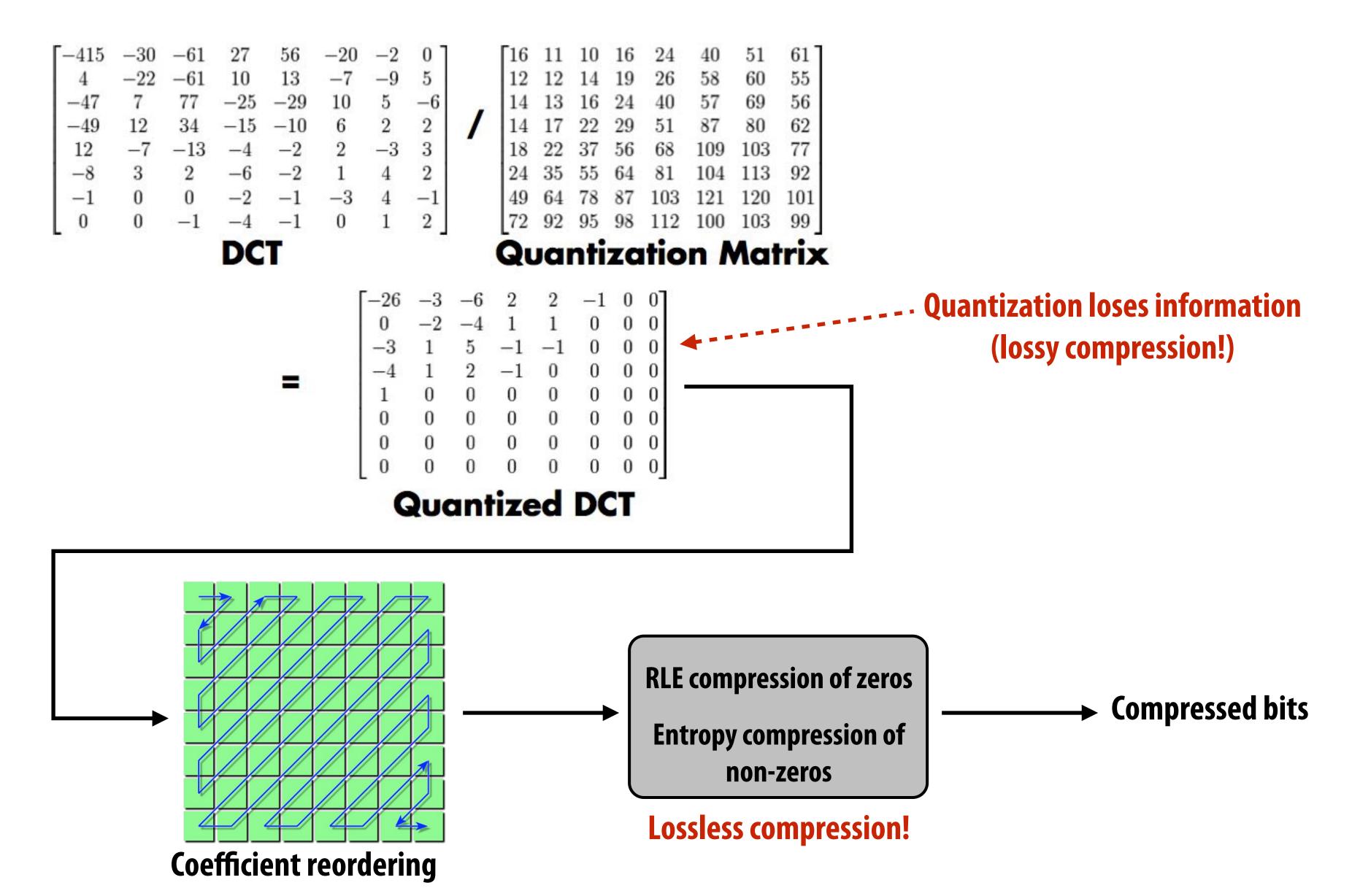


Image credit: Wikipedia

Reordering

JPEG compression summary



Credit: Pat Hanrahan

JPEG compression summary

Convert image to Y'CbCr Downsample CbCr (to 4:2:2 or 4:2:0) For each color channel (Y', Cb, Cr): For each 8x8 block of values **Compute DCT Quantize results Reorder values Run-length encode 0-spans** Huffman encode non-zero values

(information loss occurs here)

(information loss occurs here)

Key idea: exploit characteristics of human perception to build efficient image storage and image processing systems

- Separation of luminance from chrominance in color representation (Y'CrCb) allows reduced resolution in chrominance channels (4:2:0)
- Encode pixel values linearly in lightness (perceived brightness), not in luminance (distribute representable values uniformly in perceptual space)
- IPEG compression significantly reduces file size at cost of quantization error in high spatial frequencies
 - Human brain is more tolerant of errors in high frequency image components than in low frequency ones
 - Images of the real world are dominated by low-frequency components

Aside: video compression adds two main ideas

- **Exploiting redundancy:**
 - Intra-frame redundancy: value of pixels in neighboring regions of a frame are good <u>predictor</u> of values for other pixels in the frame (spatial redundancy)
 - Inter-frame redundancy: pixels from nearby frames in time are a good predictor for the current frame's pixels (temporal redundancy)

Motion vector visualization

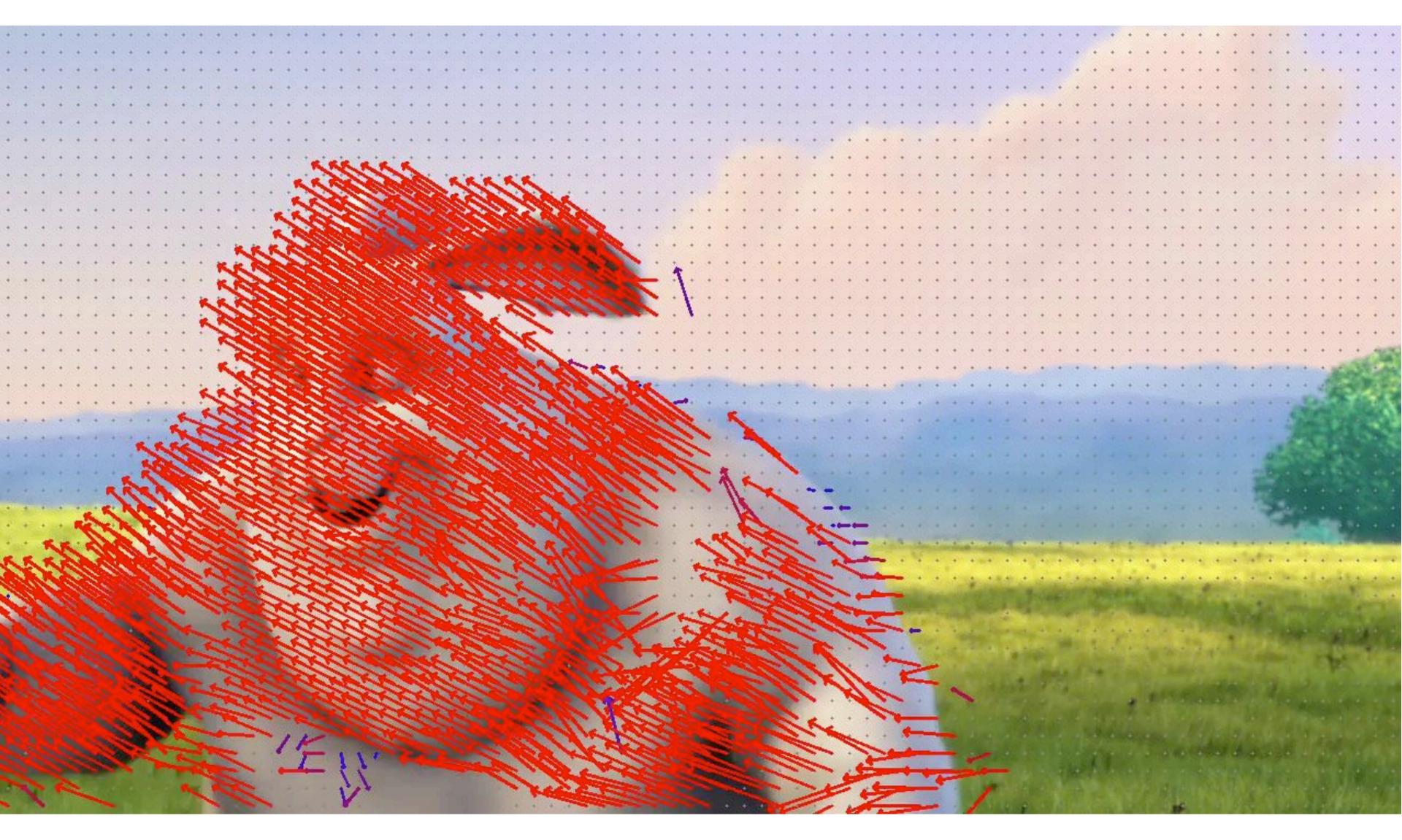
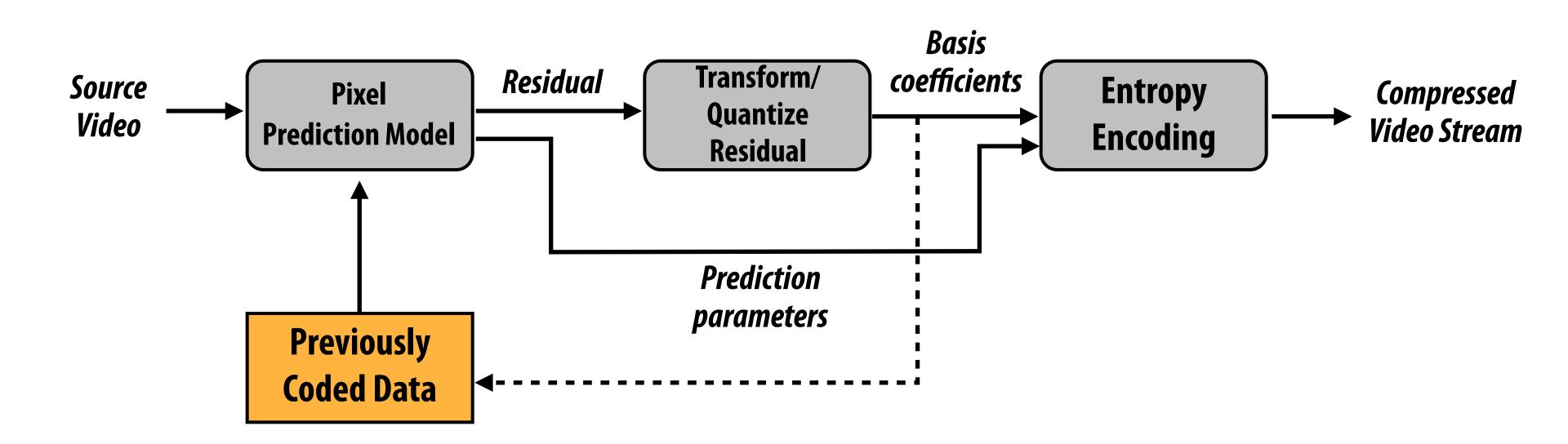


Image credit: Keyi Zhang

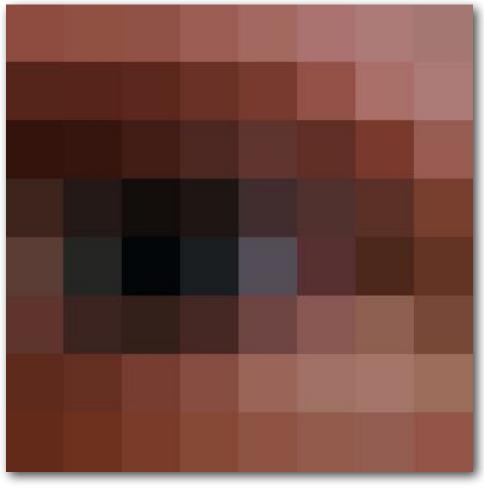
Video compression overview



Residual: difference between predicted pixel values and input video pixel values

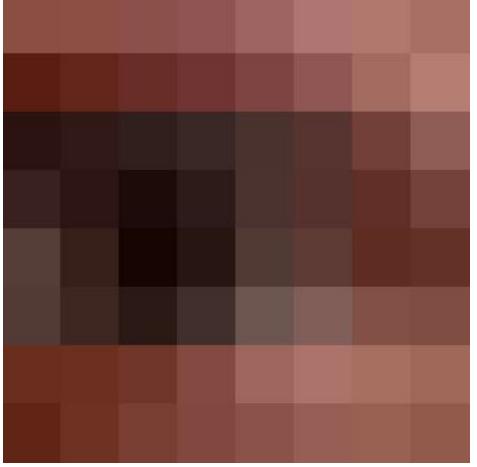
Credit: Figure derived from <u>H.264 Advanced Video Compression Standard</u>, I. Richardson, 2010

Residual: difference between compressed image and original image

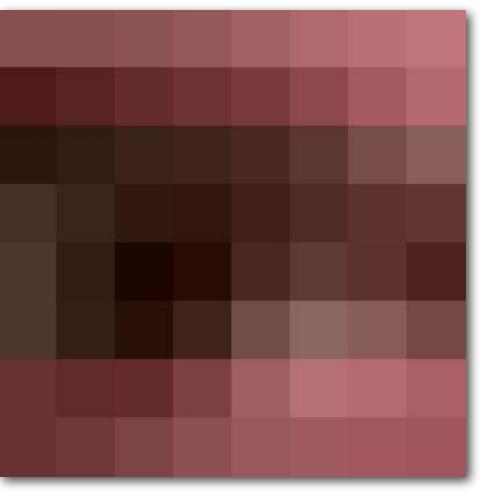


Original pixels

In video compression schemes, the residual image is compressed using techniques like those described in the earlier part of this lecture.



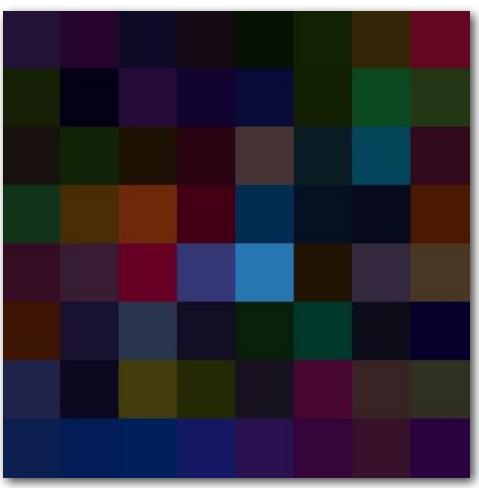
Compressed pixels (JPEG quality level 6)



Compressed pixels (JPEG quality level 2)



Residual (amplified for visualization)



Residual (amplified for visualization)

Example video

30 second video: 1920 x 1080, @ 30fps

B 白鵰大学 (+)

Uncompressed: 8-bits per channel RGB \rightarrow 24 bits/pixel \rightarrow 6.2MB/frame (6.2 MB * 30 sec * 30 fps = 5.2 GB) Size of data when each frames stored as JPG: 531MB Actual H.264 video file size: 65.4 MB (80-to-1 compression ratio, 8-to-1 compared to JPG) **Compression/encoding performed in real time on my iPhone**



Go Swallows!



Image processing basics



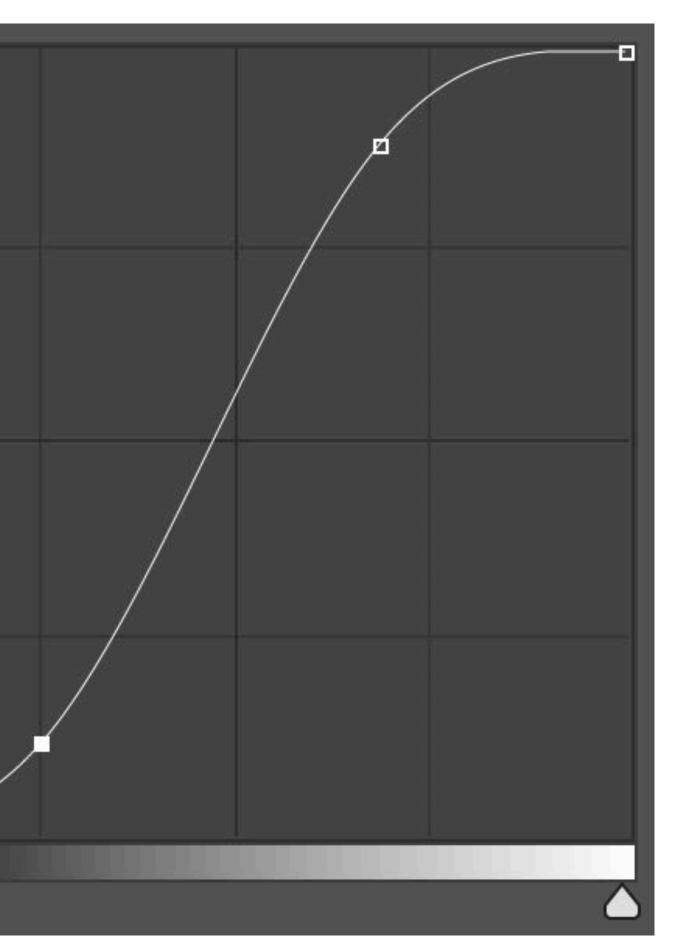
Increase contrast



Increasing contrast with "S curve"

Per-pixel operation: output(x,y) = f(input(x,y))

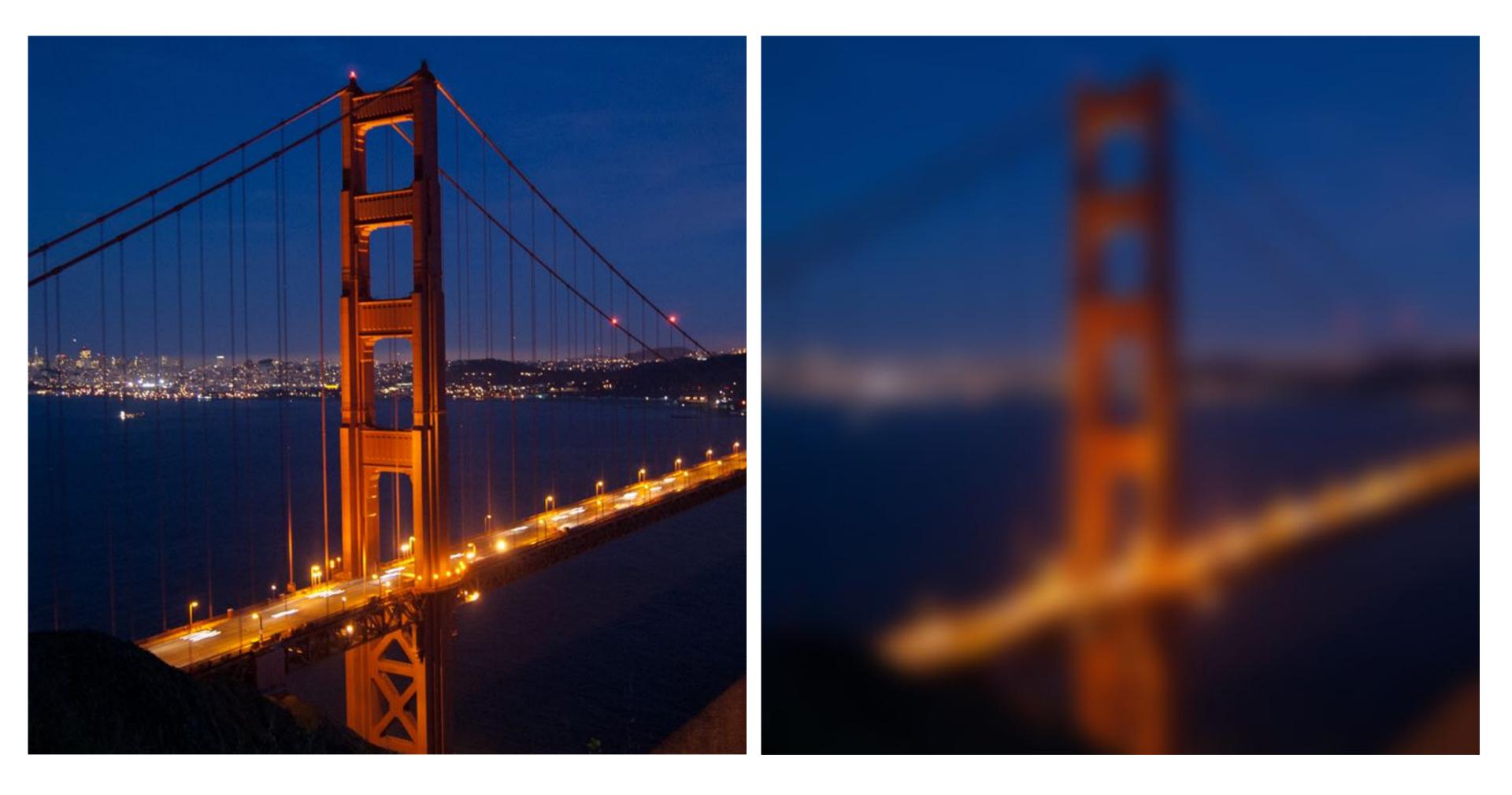
Output pixel intensity



Input pixel intensity



Image Invert: out(x,y) = 1 - in(x,y)

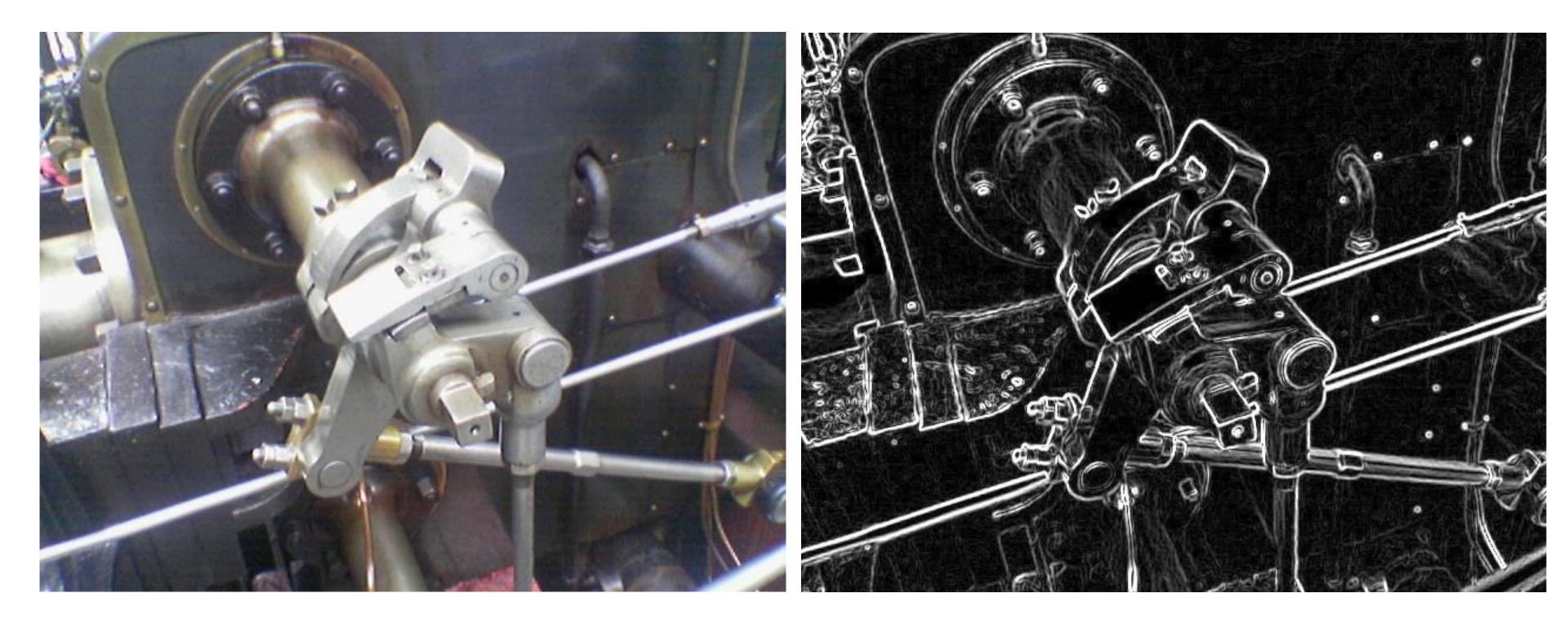








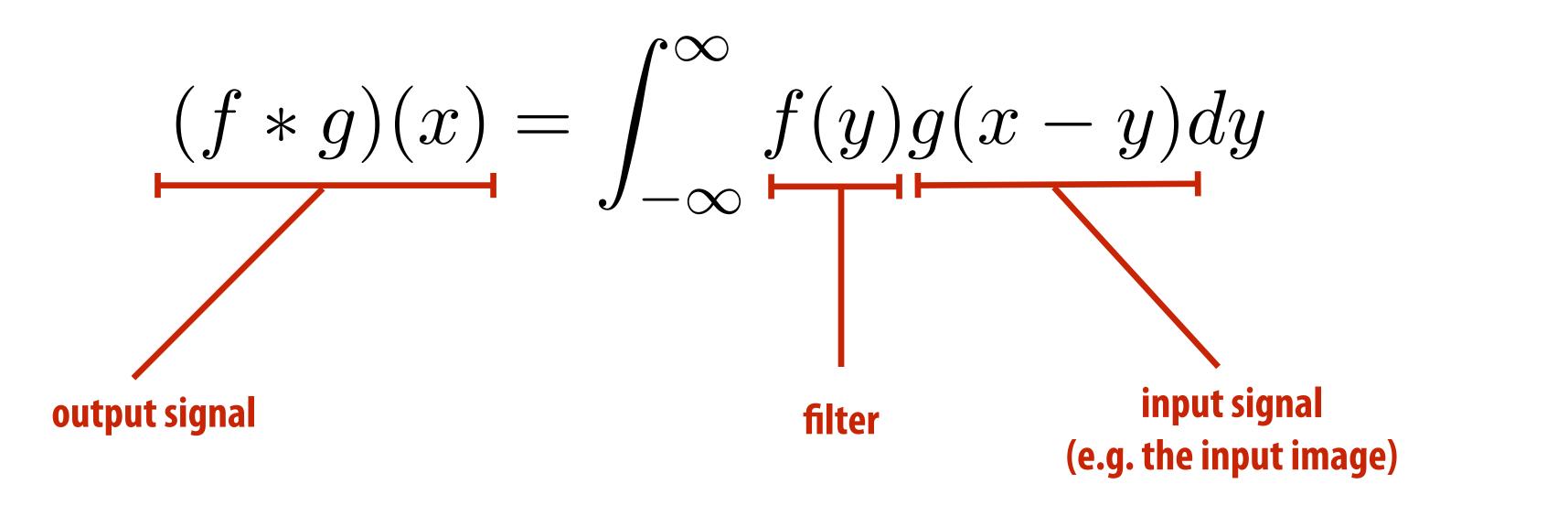
Edge detection



A "smarter" blur (doesn't blur over edges)



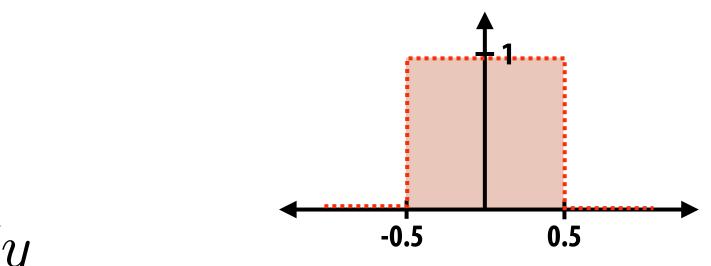
Review: convolution



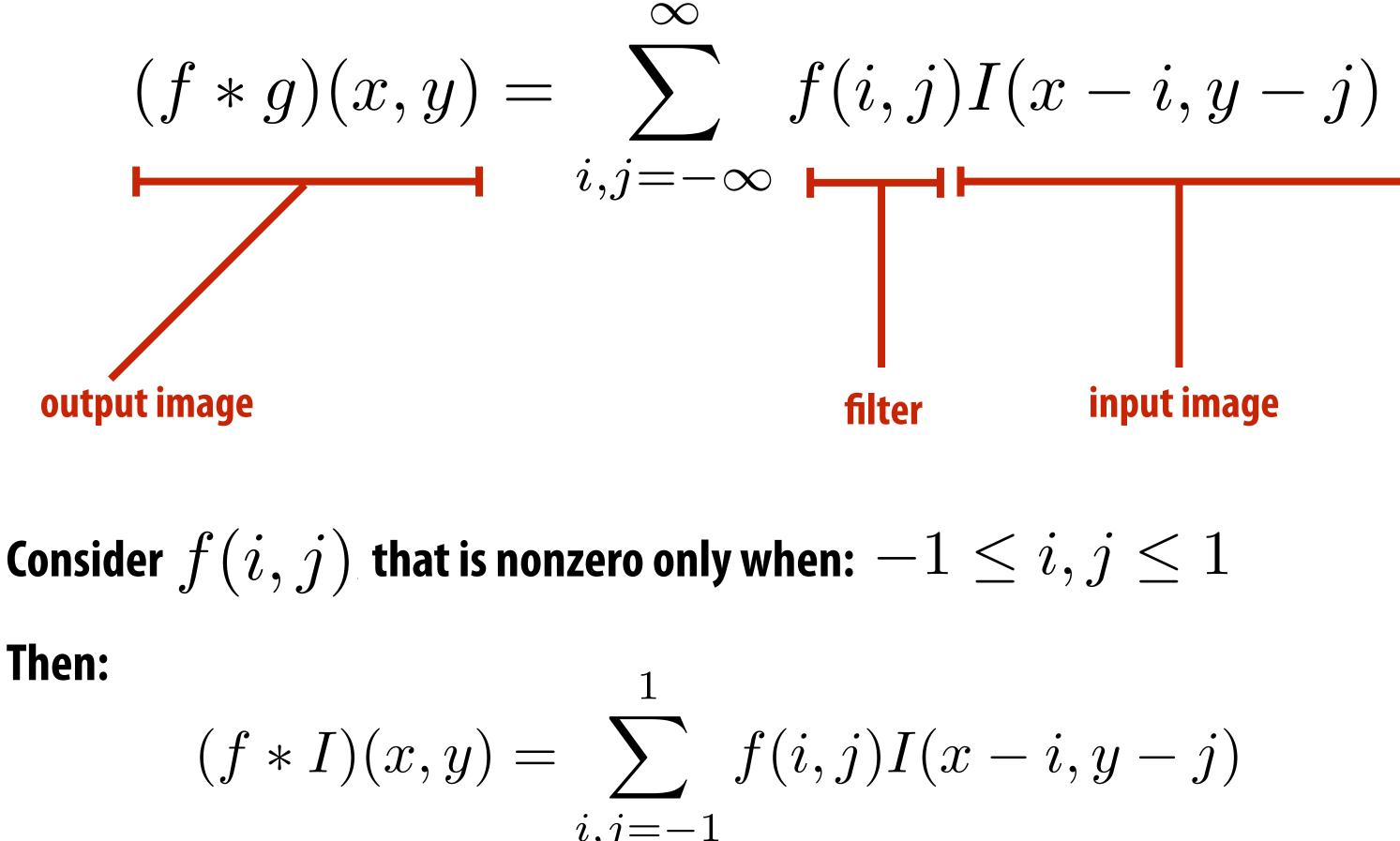
It may be helpful to consider the effect of convolution with the simple unit-area "box" function:

$$f(x) = \begin{cases} 1 & |x| \le 0.5\\ 0 & otherwise \end{cases}$$
$$(f * g)(x) = \int_{-0.5}^{0.5} g(x - y) dy$$

f * g is a "blurred" version of g where the output at x is the average value of the input between x-0.5 to x+0.5



Discrete 2D convolution



Then:

And we can represent f(i,j) as a 3x3 matrix of values where:

$$f(i,j) = \mathbf{F}_{i,j}$$
 (often called: "fi

ilter weights", "filter kernel")

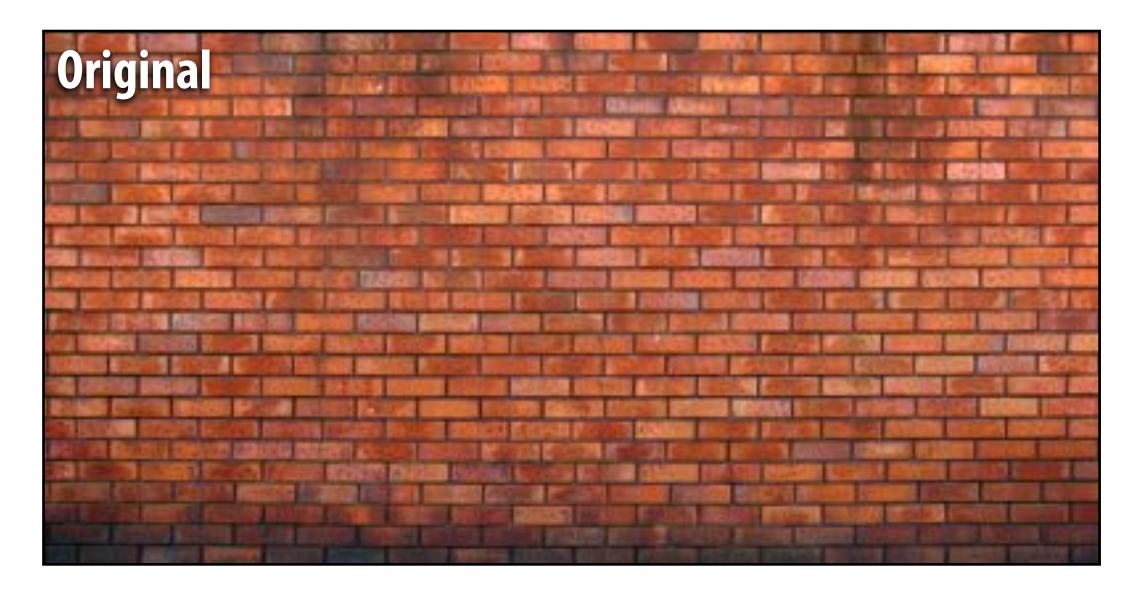
Simple 3x3 box blur

float input[(WIDTH+2) * (HEIGHT+2)];
float output[WIDTH * HEIGHT];

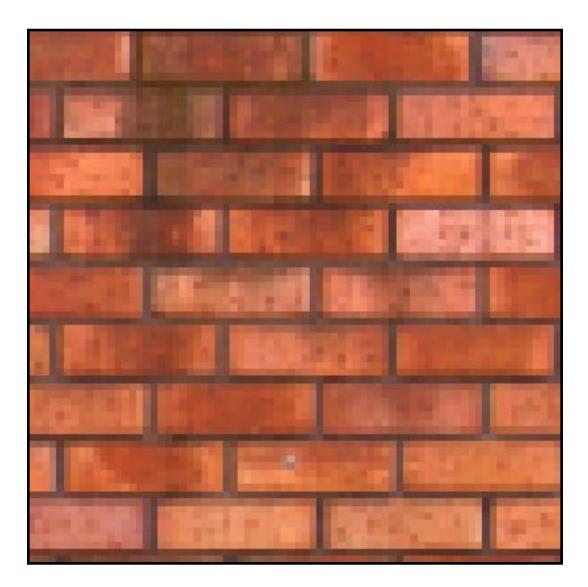
for (int j=0; j<HEIGHT; j++) {
 for (int i=0; i<WIDTH; i++) {
 float tmp = 0.f;
 for (int jj=0; jj<3; jj++)
 for (int ii=0; ii<3; ii++)
 tmp += input[(j+jj)*(WIDTH+2) + (i+ii)] * weights[jj*3 + ii];
 output[j*WIDTH + i] = tmp;
 }
</pre>

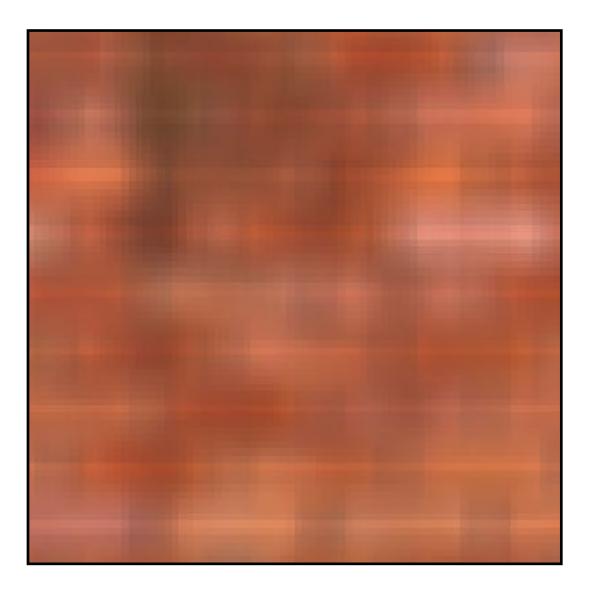
For now: ignore boundary pixels and assume output image is smaller than input (makes convolution loop bounds much simpler to write)

7x7 box blur









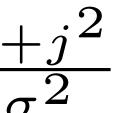
Gaussian blur

Obtain filter coefficients by sampling 2D Gaussian function

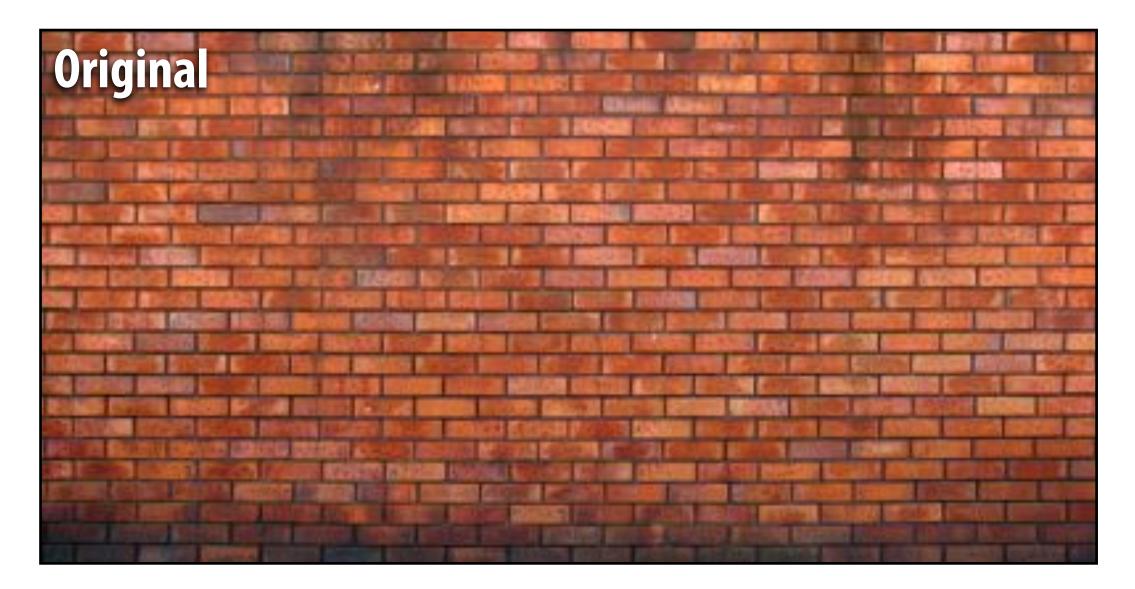
$$f(i,j) = \frac{1}{2\pi\sigma^2} e^{-\frac{i^2}{2\sigma^2}}$$

- Produces weighted sum of neighboring pixels (contribution falls off with distance)
 - In practice: truncate filter beyond certain distance for efficiency

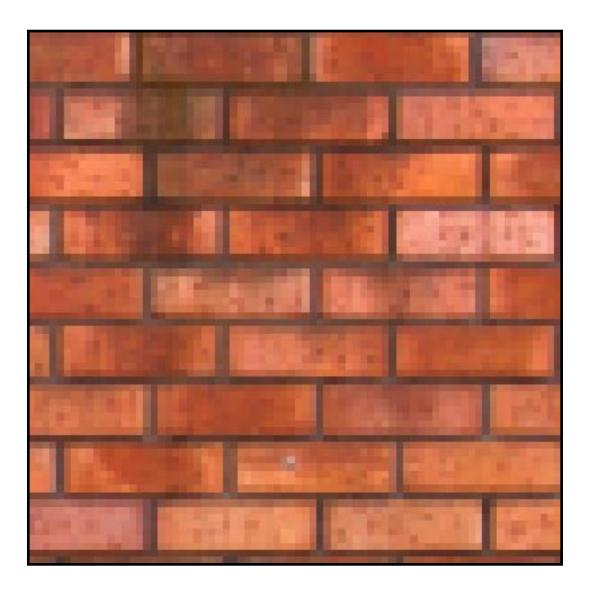
[.075	.124	.075
.124	.204	.124
.075	.124	.075



7x7 gaussian blur

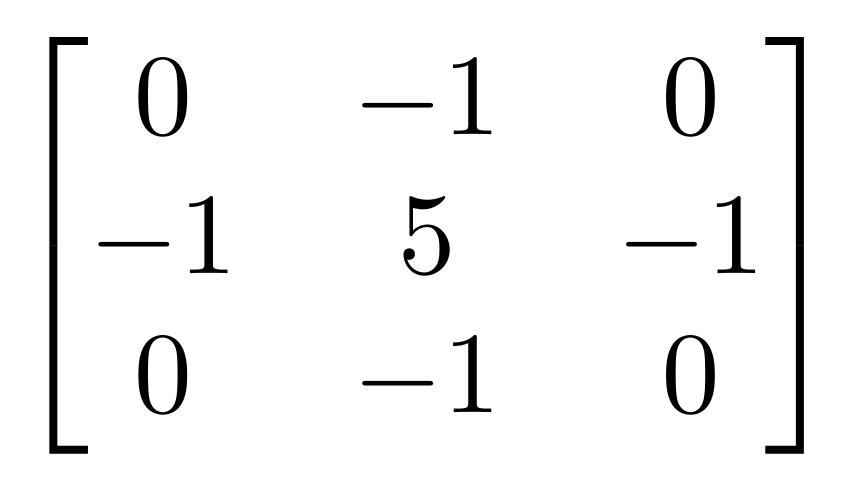




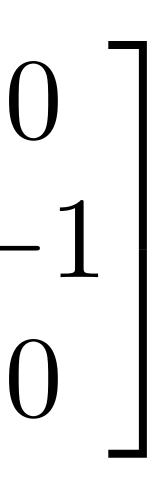




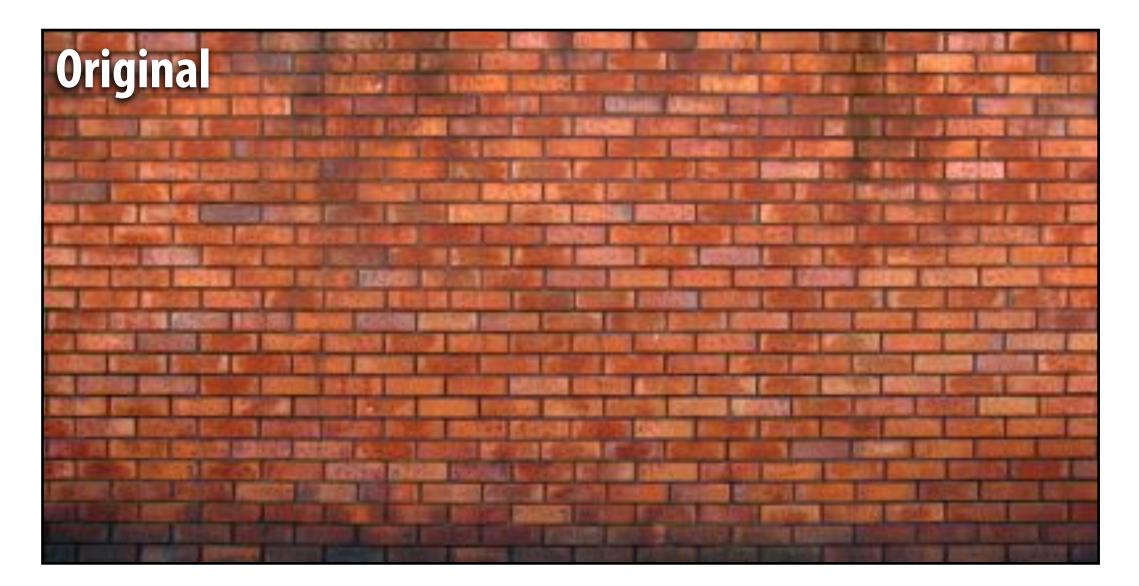
What does convolution with this filter do?

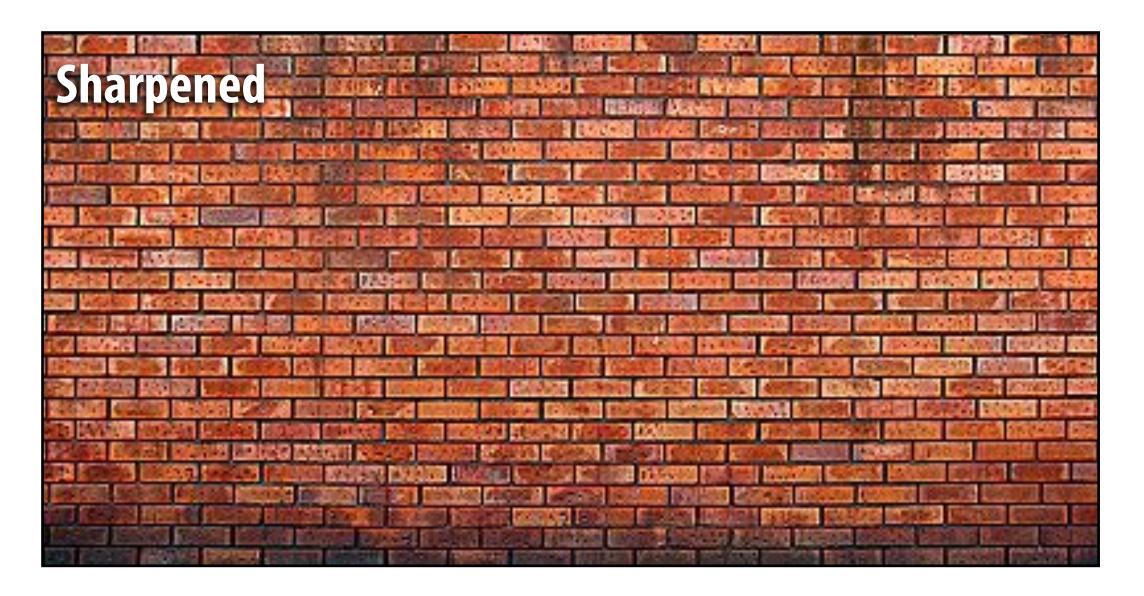


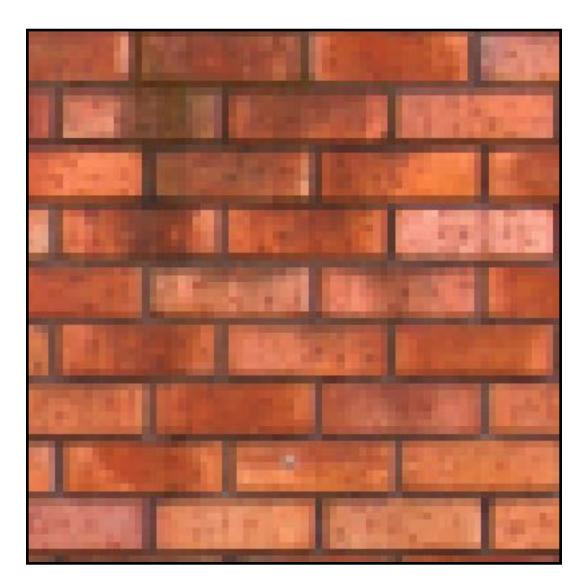
Sharpens image!

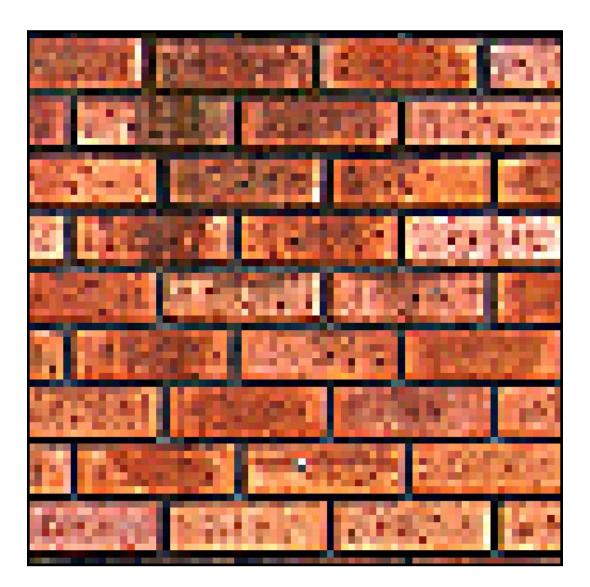


3x3 sharpen filter





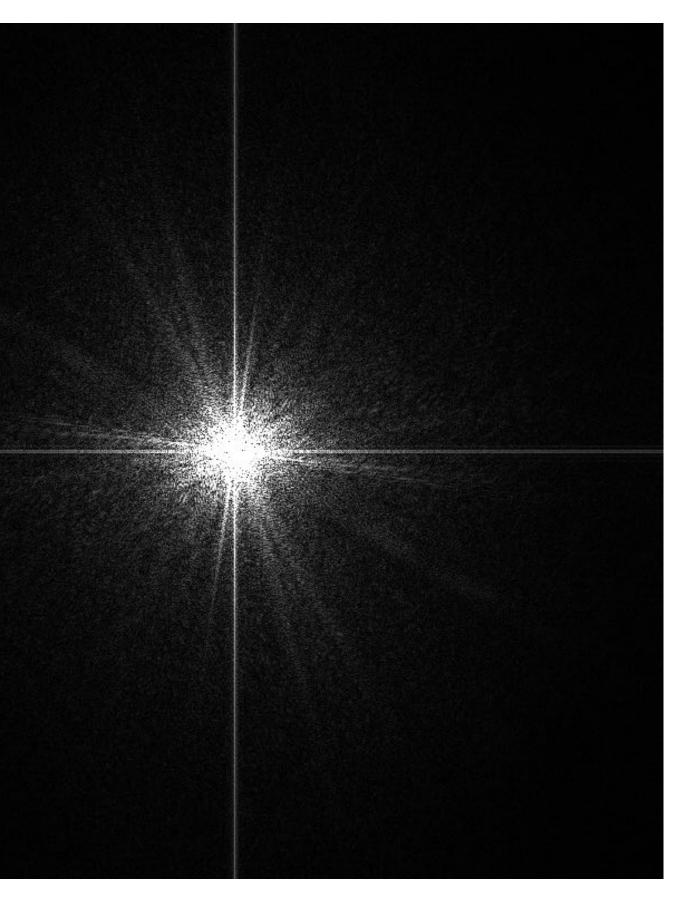




Recall: blurring is removing high frequency content



Spatial domain result

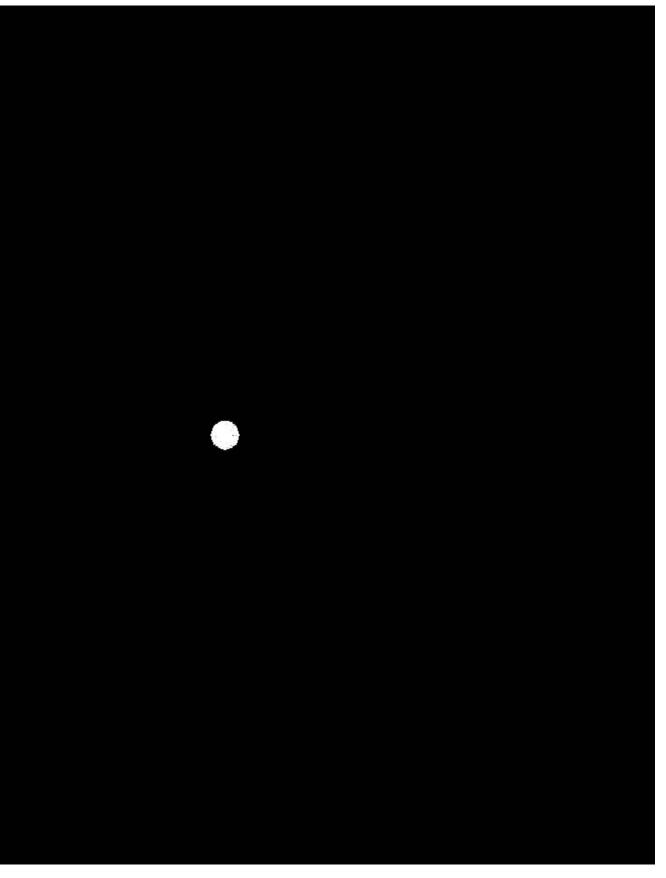


Spectrum

Recall: blurring is removing high frequency content



Spatial domain result



Spectrum (after low-pass filter) All frequencies above cutoff have 0 magnitude

Sharpening is adding high frequencies

- Let I be the original image
- High frequencies in image I = I blur(I)
- Sharpened image = I + (I-blur(I))



Original image (l) Image credit: Kayvon's parents



Blur(I)



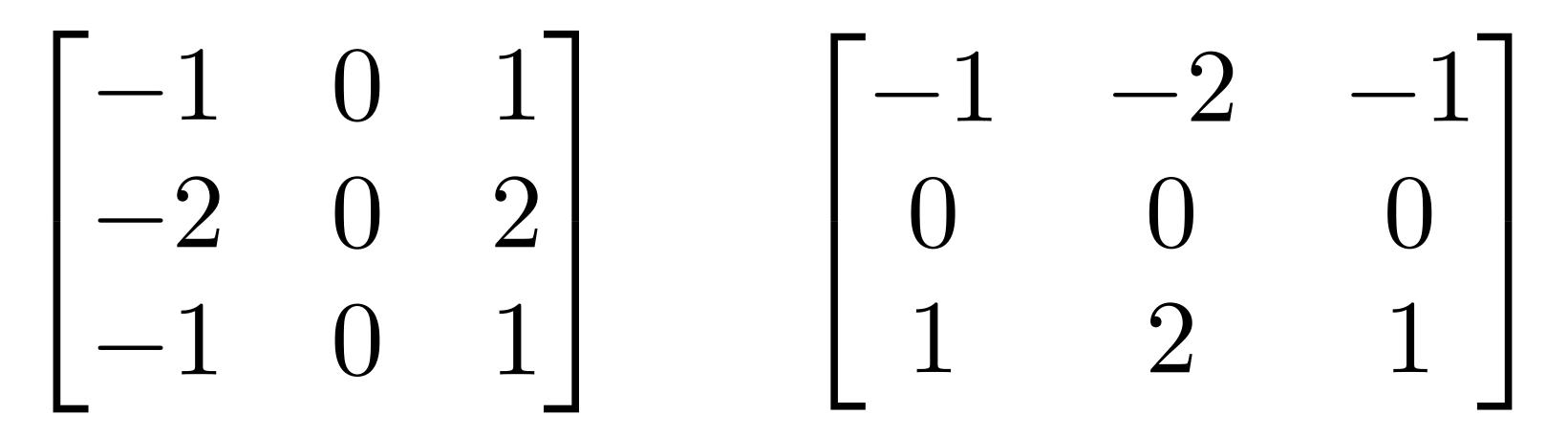
I - blur(I)



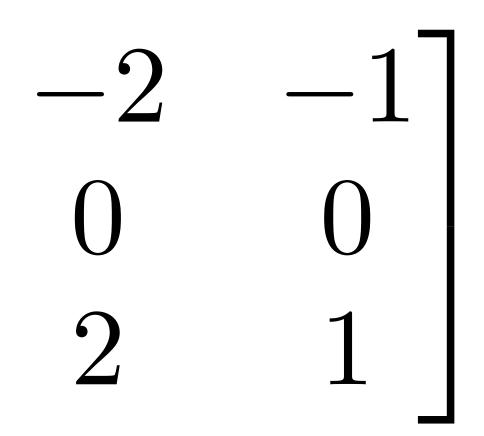
I -F (I - blur(I))



What does convolution with these filters do?



Extracts horizontal gradients



Extracts vertical gradients

Gradient detection filters





Horizontal gradients

Vertical gradients

Note: you can think of a filter as a "detector" of a pattern, and the magnitude of a pixel in the output image as the "response" of the filter to the region surrounding each pixel in the input image (this is a common interpretation in computer vision)

Sobel edge detection

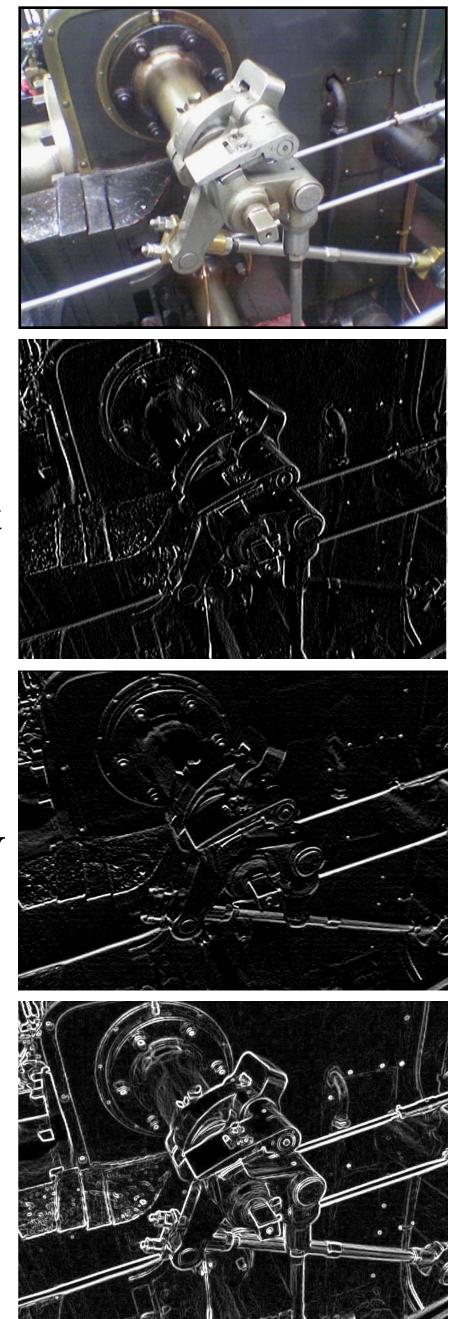
Compute gradient response images

$$G_{x} = \begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{bmatrix} * I$$
$$G_{y} = \begin{bmatrix} -1 & -2 & -1 \\ 0 & 0 & 0 \\ 1 & 2 & 1 \end{bmatrix} * I$$

Find pixels with large gradients

 $G = \sqrt{G_x^2 + G_y^2}$

Pixel-wise operation on images



 G_{x}

Gy

G

Stanford CS248, Winter 2021

Cost of convolution with N x N filter?

float input[(WIDTH+2) * (HEIGHT+2)]; float output[WIDTH * HEIGHT];

float weights[] = {1./9, 1./9, 1./9, 1./9, 1./9, 1./9, 1./9, 1./9, 1./9;

```
for (int j=0; j<HEIGHT; j++) {</pre>
   for (int i=0; i<WIDTH; i++) {</pre>
      float tmp = 0.f;
      for (int jj=0; jj<3; jj++)</pre>
          for (int ii=0; ii<3; ii++)</pre>
             tmp += input[(j+jj)*(WIDTH+2) + (i+ii)] * weights[jj*3 + ii];
      output[j*WIDTH + i] = tmp;
  }
```

In this 3x3 box blur example: **Total work per image = 9 x WIDTH x HEIGHT**

For N x N filter: N² x WIDTH x HEIGHT

Separable filter

A filter is separable if can be written as the outer product of two other filters. Example: a 2D box blur

- Exercise: write 2D gaussian and vertical/horizontal gradient detection filters as product of 1D filters (they are separable!)
- Key property: 2D convolution with separable filter can be written as two 1D convolutions!

Implementation of 2D box blur via two 1D convolutions

```
int WIDTH = 1024
int HEIGHT = 1024;
float input[(WIDTH+2) * (HEIGHT+2)];
float tmp_buf[WIDTH * (HEIGHT+2)];
                                              2N x WIDTH x HEIGHT
float output[WIDTH * HEIGHT];
float weights[] = {1./3, 1./3, 1./3};
for (int j=0; j<(HEIGHT+2); j++)</pre>
  for (int i=0; i<WIDTH; i++) {</pre>
    float tmp = 0.f;
    for (int ii=0; ii<3; ii++)</pre>
      tmp += input[j*(WIDTH+2) + i+ii] * weights[ii];
    tmp_buf[j*WIDTH + i] = tmp;
  }
for (int j=0; j<HEIGHT; j++) {</pre>
  for (int i=0; i<WIDTH; i++) {</pre>
    float tmp = 0.f;
    for (int jj=0; jj<3; jj++)</pre>
      tmp += tmp_buf[(j+jj)*WIDTH + i] * weights[jj];
    output[j*WIDTH + i] = tmp;
  }
}
```

Total work per image for NxN filter:

Bilateral filter

Original



Example use of bilateral filter: removing noise while preserving image edges

https://www.thebest3d.com/howler/11/new-in-version-11-bilateral-noise-filter.html

After bilateral filter

Bilateral filter

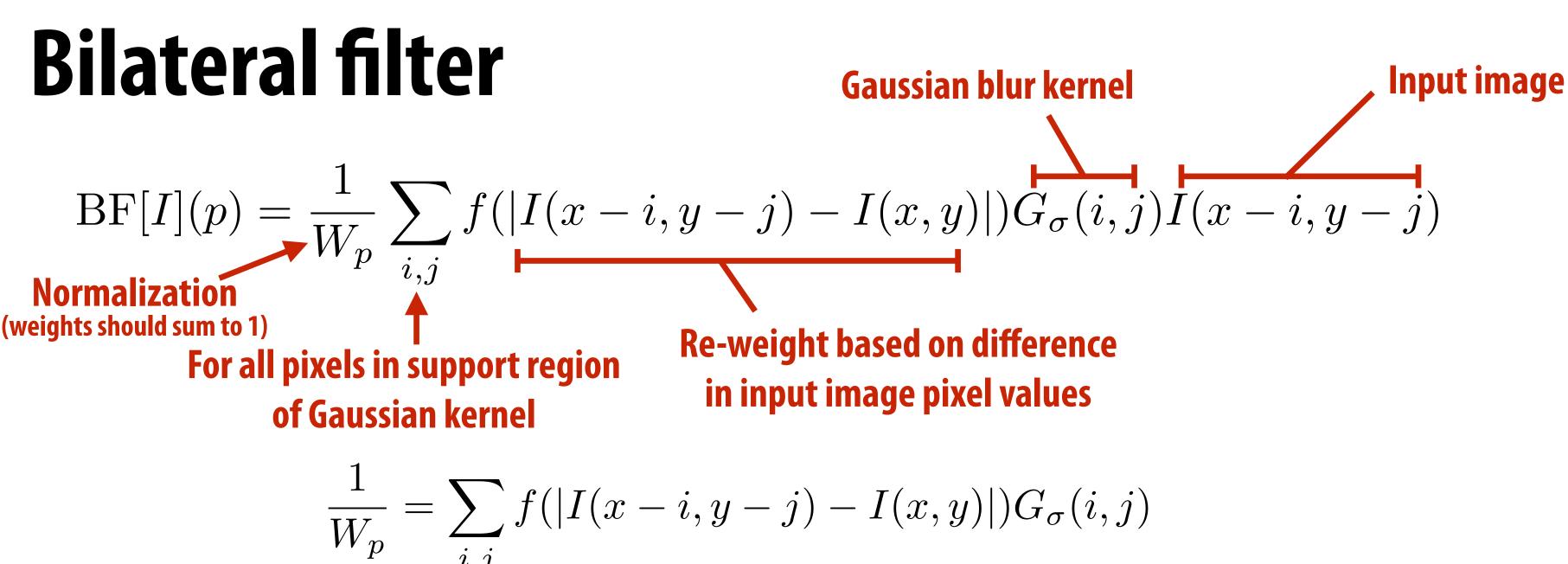
Original



Example use of bilateral filter: removing noise while preserving image edges

http://opencvpython.blogspot.com/2012/06/smoothing-techniques-in-opencv.html

After bilateral filter



- The bilateral filter is an "edge preserving" filter: down-weight contribution of pixels on the "other side" of strong edges. f(x) defines what "strong edge means"
- Spatial distance weight term f(x) could itself be a gaussian

- Or very simple: f(x) = 0 if x > threshold, 1 otherwise

Value of output pixel (x,y) is the weighted sum of all pixels in the support region of a truncated gaussian kernel

But weight is combination of <u>spatial distance</u> and input image <u>pixel intensity difference</u>. (the filter's weights depend on input image content)

Bilateral filter

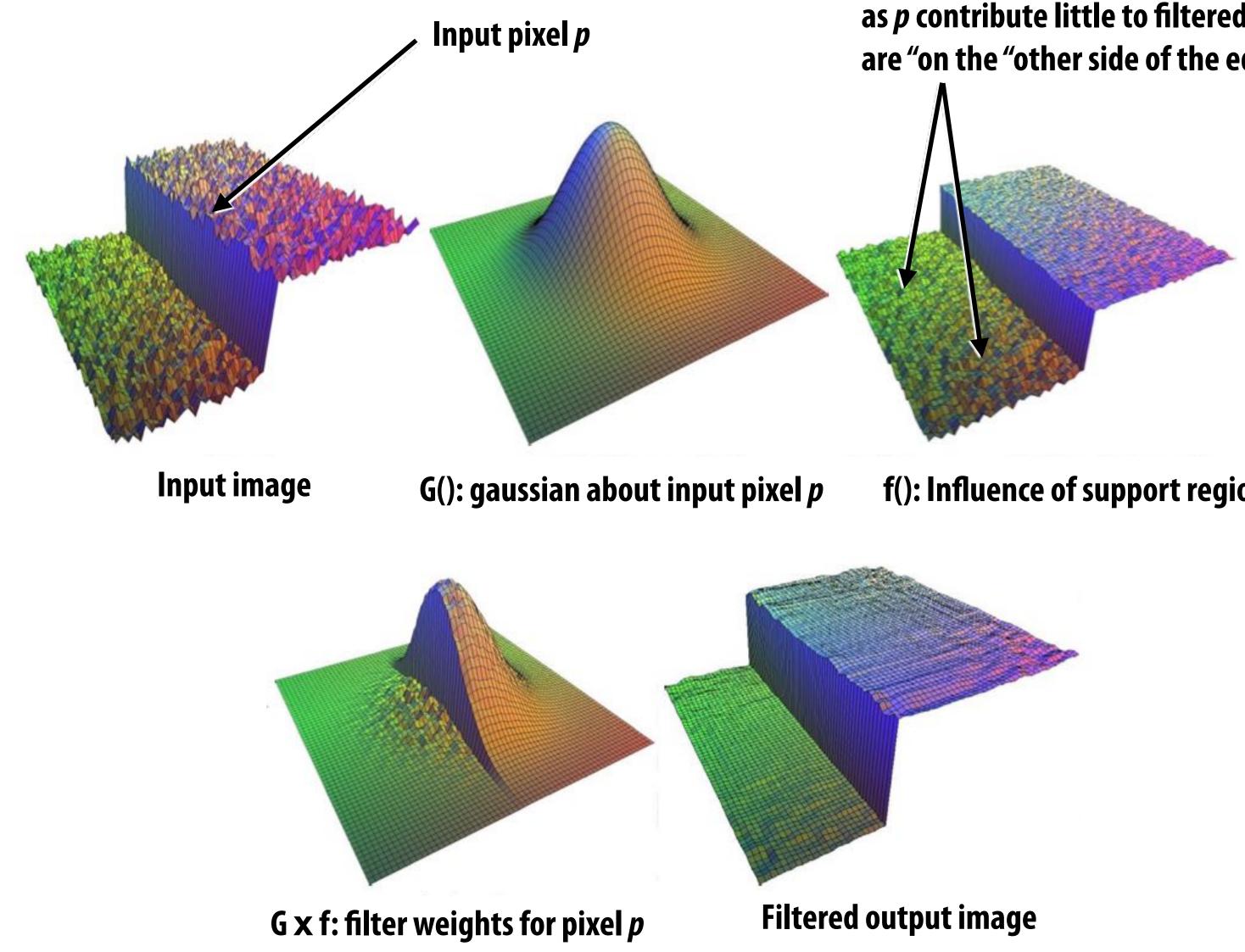


Figure credit: Durand and Dorsey, "Fast Bilateral Filtering for the Display of High-Dynamic-Range Images", SIGGRAPH 2002

Pixels with significantly different intensity as *p* contribute little to filtered result (they are "on the "other side of the edge"

f(): Influence of support region

Bilateral filter: kernel depends on image content

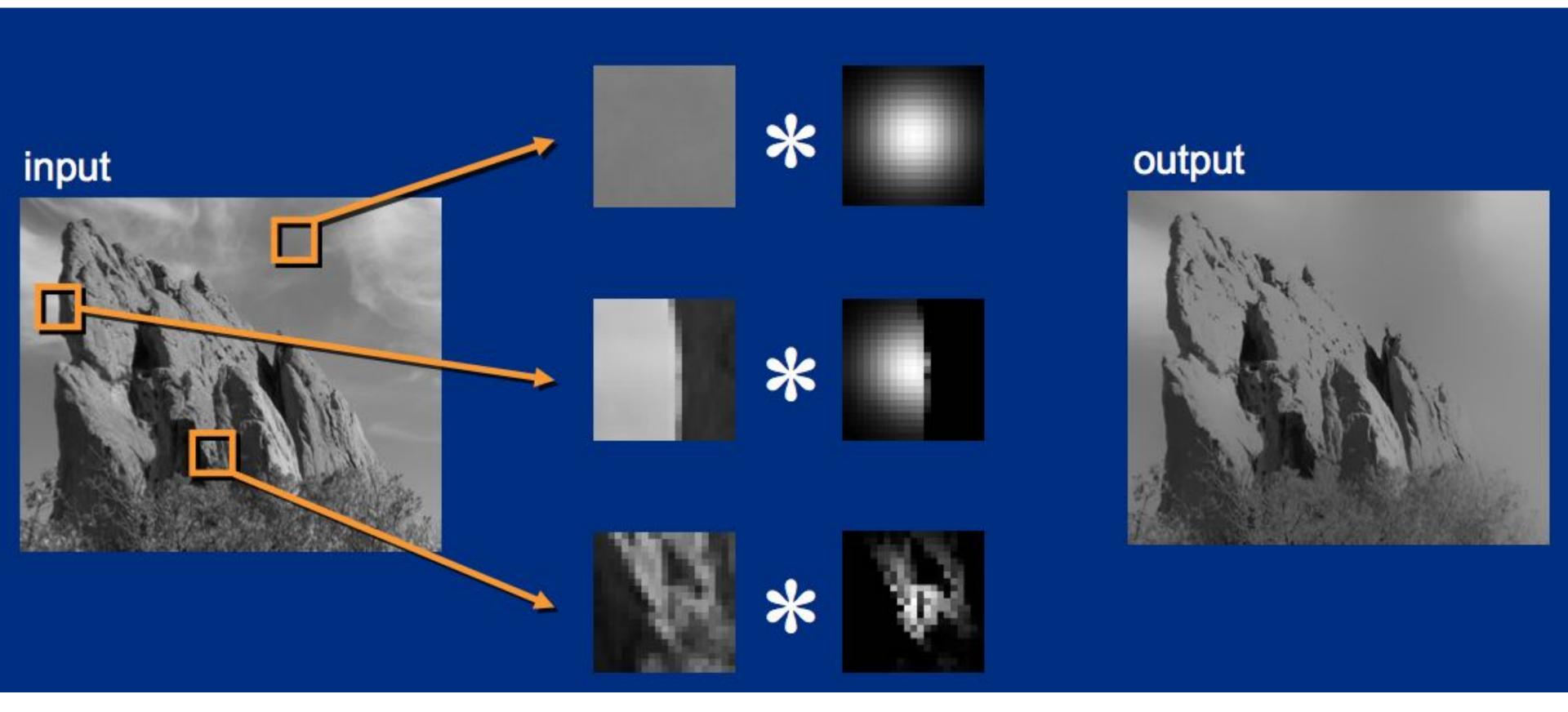


Figure credit: SIGGRAPH 2008 Course: "A Gentle Introduction to Bilateral Filtering and its Applications" Paris et al.

Summary

Last two lectures: representing images

- Choice of color space (different representations of color)
- Store values in perceptual space (non-linear in energy)
- JPEG image compression (tolerate loss due to approximate representation of high frequency components)

Basic image processing operations

- Per-pixel operations out(x,y) = f(in(x,y)) (e.g., contrast enhancement)
- Image filtering via convolution (e.g., blur, sharpen, simple edge-detection)
- Non-linear, data-dependent filters (median filter, avoid blurring over strong edges, etc.)