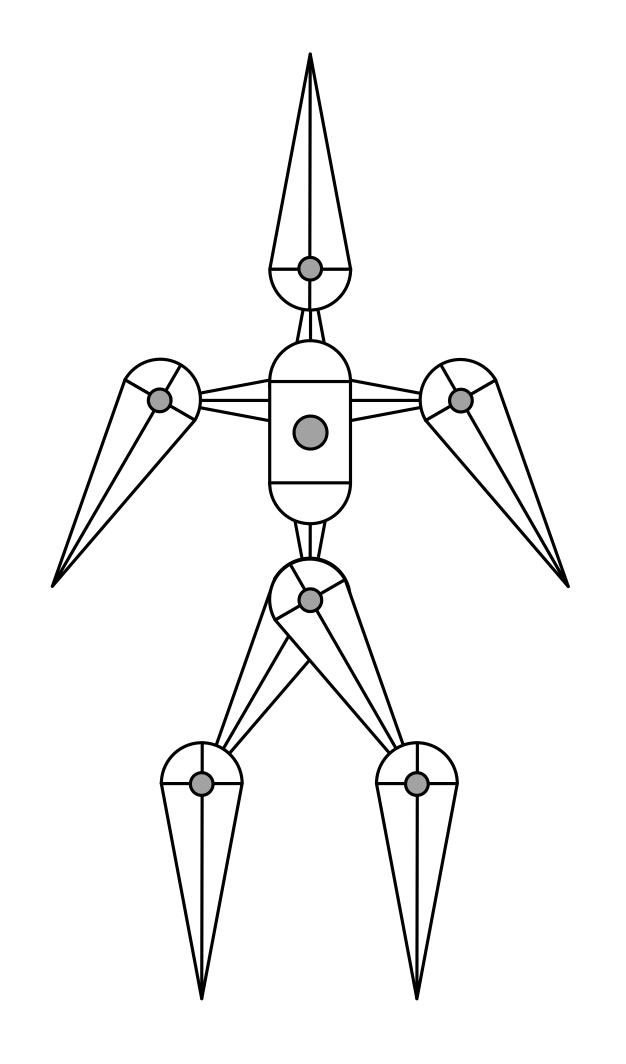
Lecture 17

Kinematics and Motion Capture

Interactive Computer Graphics Stanford CS248, Winter 2021

Today

KINEMATICS: we are going to describe how objects move, without considering the underlying forces that generate that motion

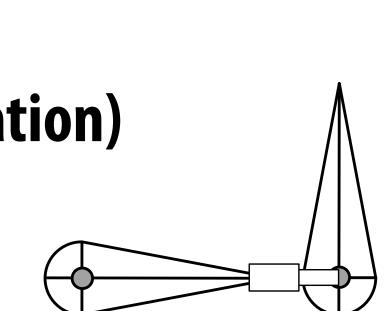


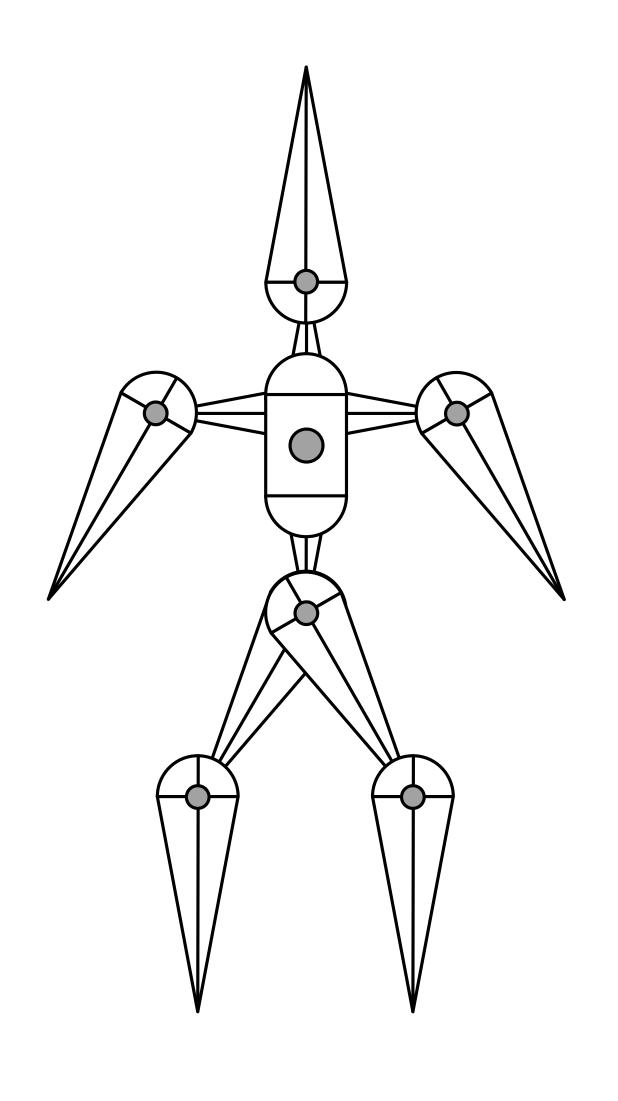
Articulated skeleton

- Topology (what's connected to what)
- Geometric relations from joints
- Tree structure (in absence of loops)

Joint types

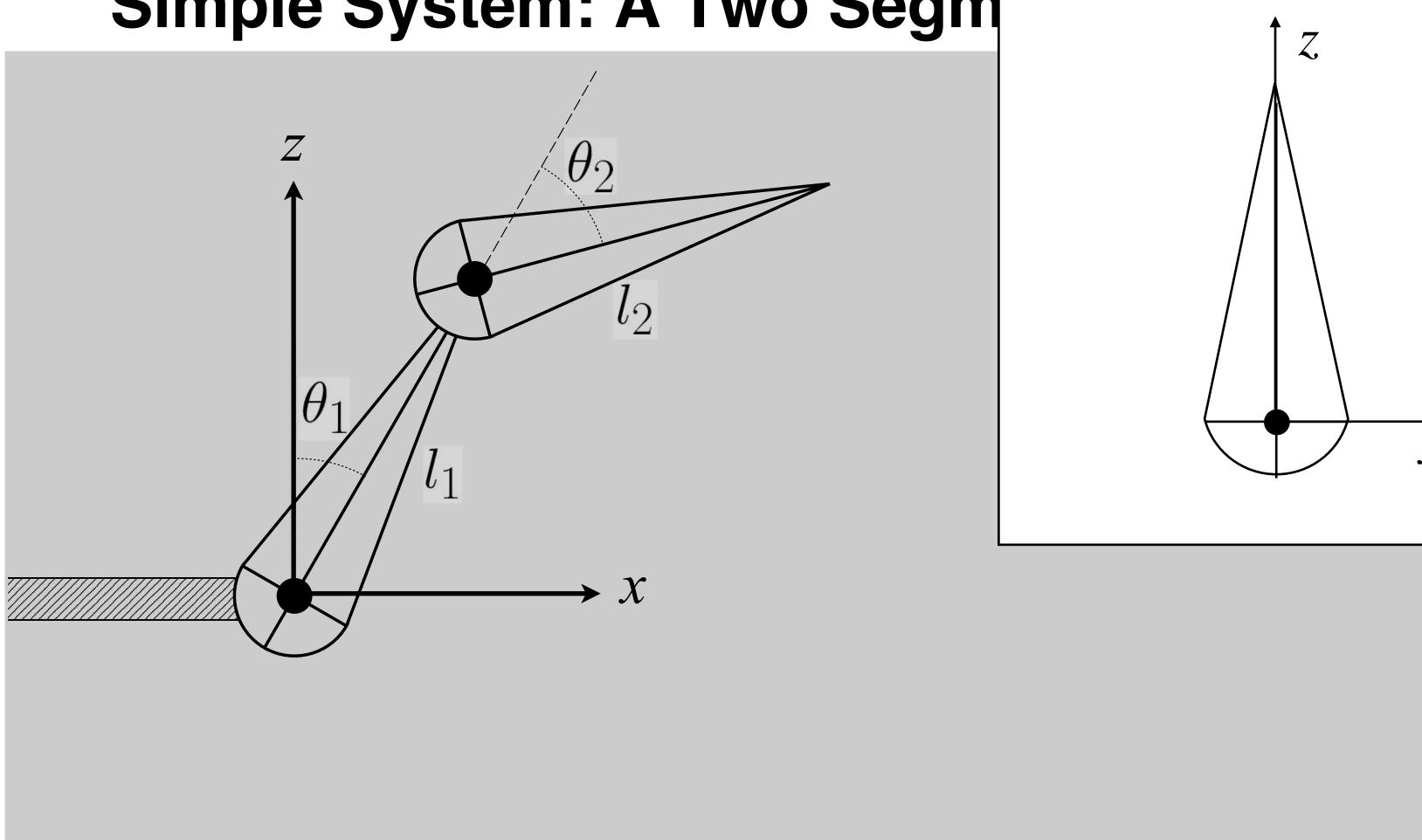
- Pin (1D rotation)
- Ball (2D rotation)
- Prismatic joint (translation)





Example: simple two segment arm in 2D

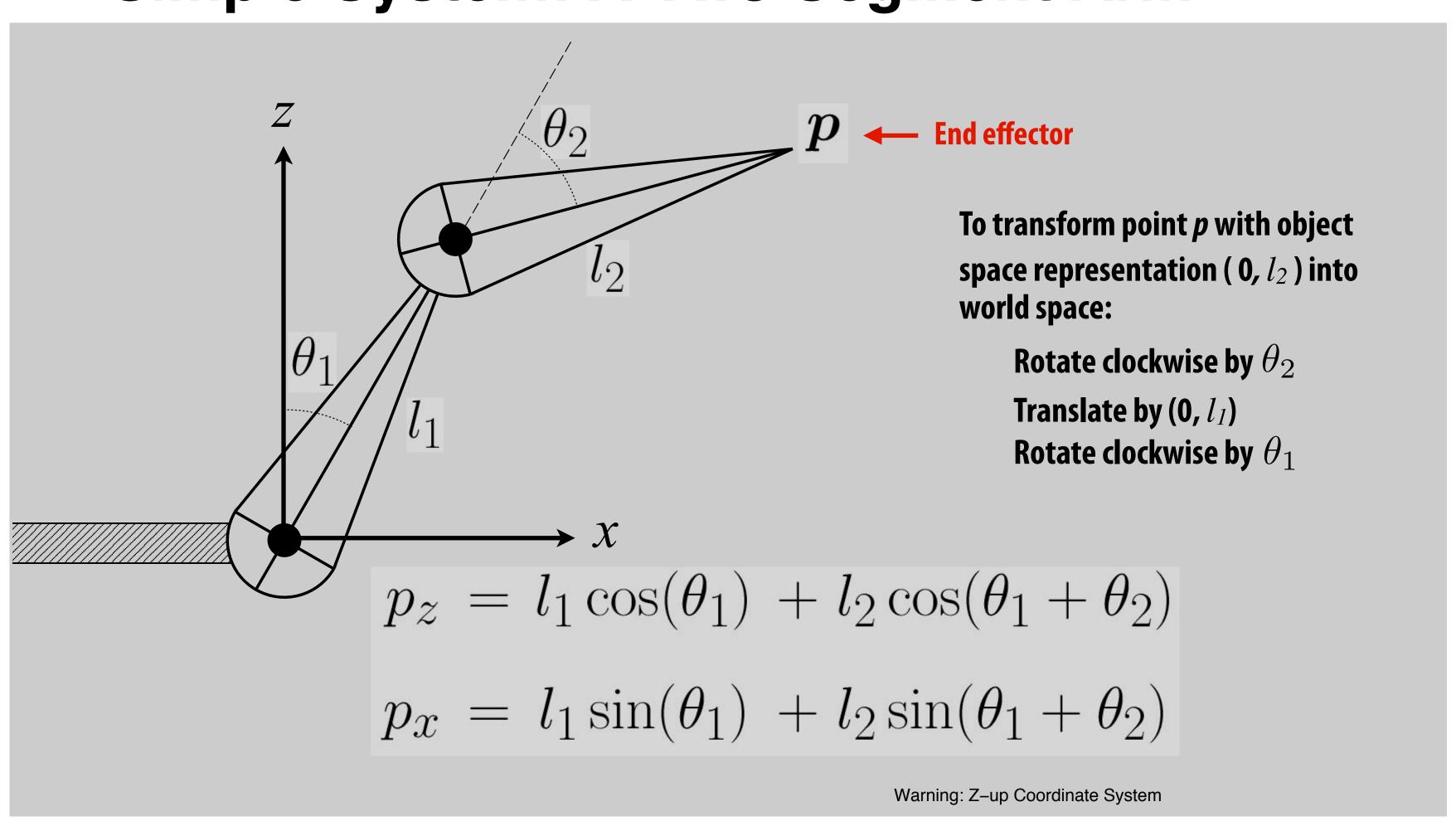
Simple System: A Two Segm



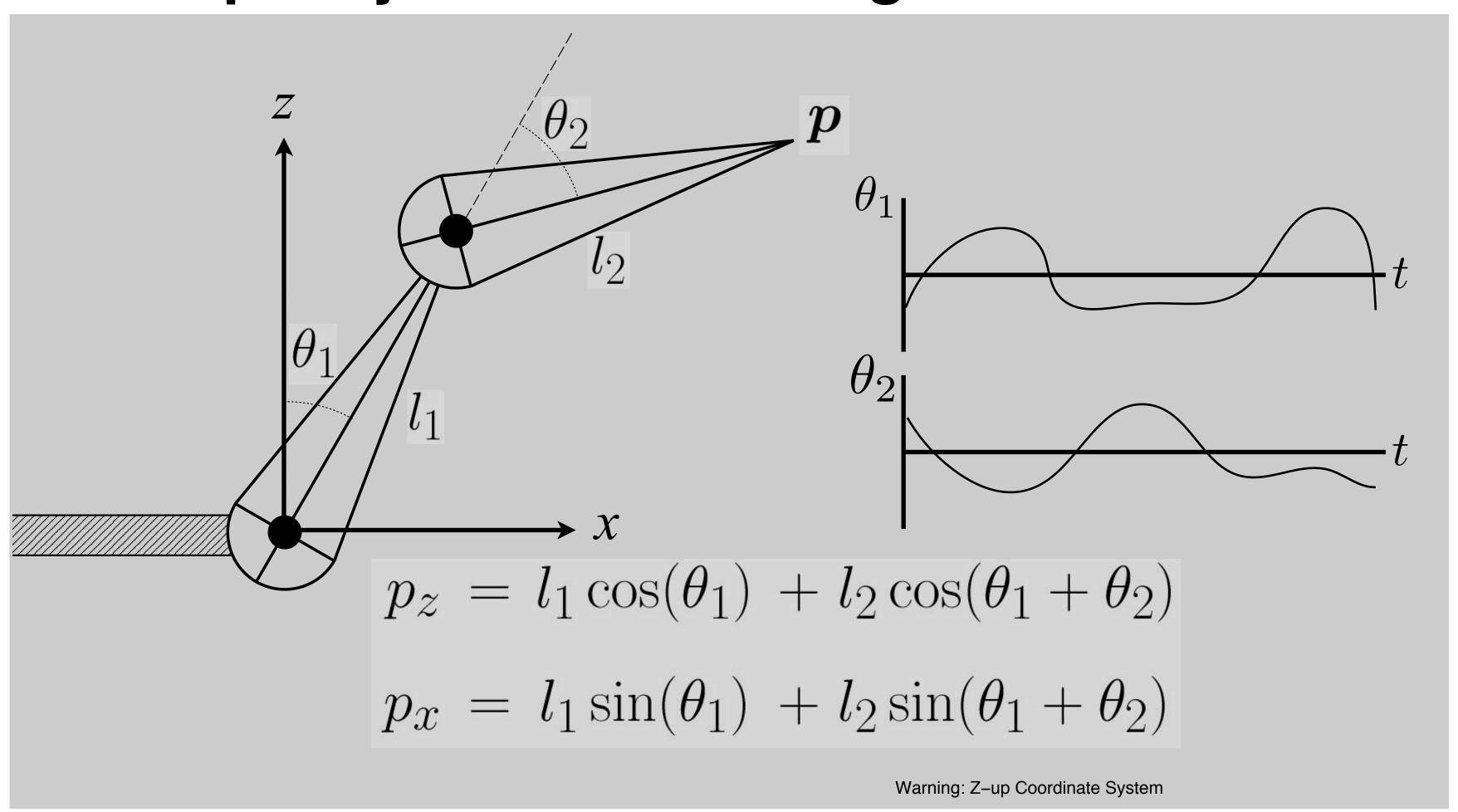
Object space position of part

Warning: Z-up Coordinate System

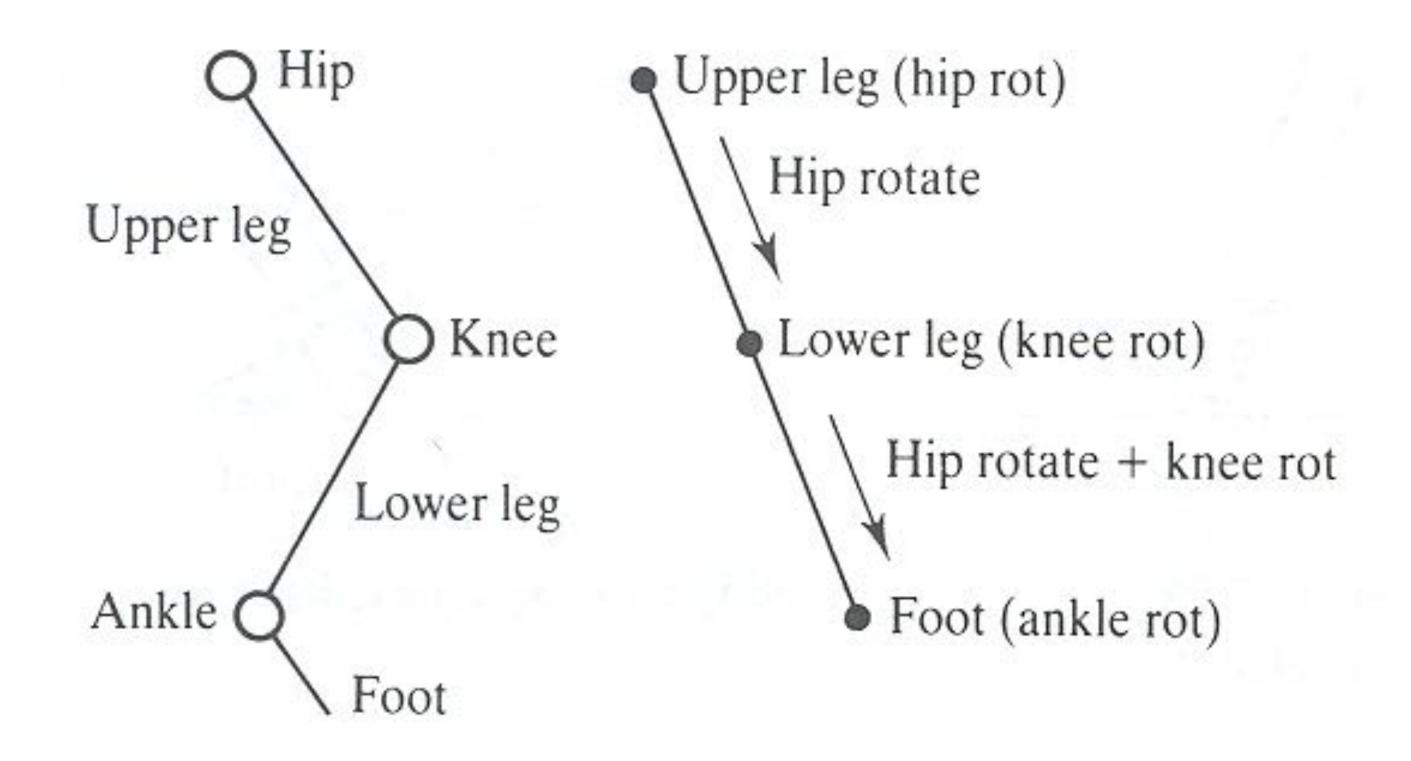
Animator provides angles, and computer determines position of end-effector Simple System: A Two Segment Arm



Animation is described as angle parameter values as a function of time: $\theta_1(t), \theta_2(t)$ Simple System: A Two Segment Arm

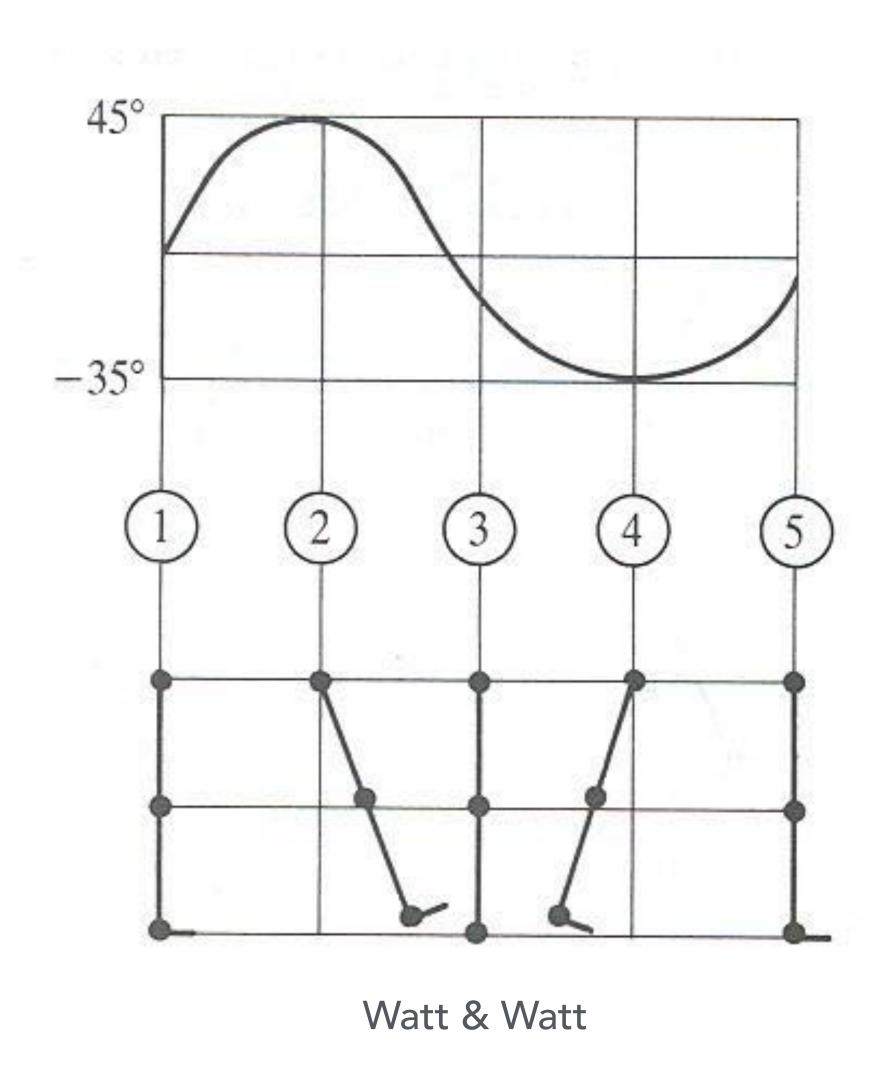


Articulated leg:

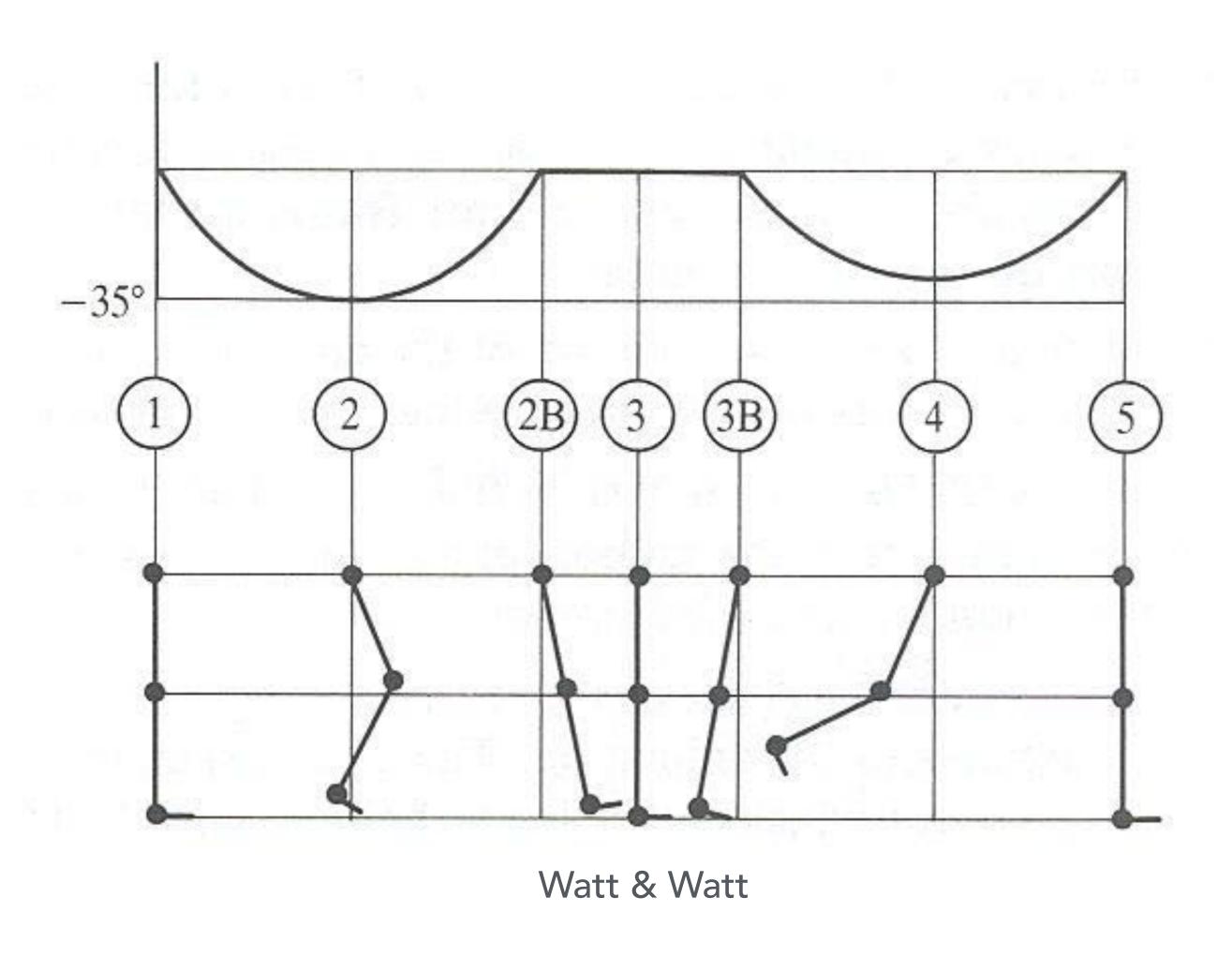


Watt & Watt

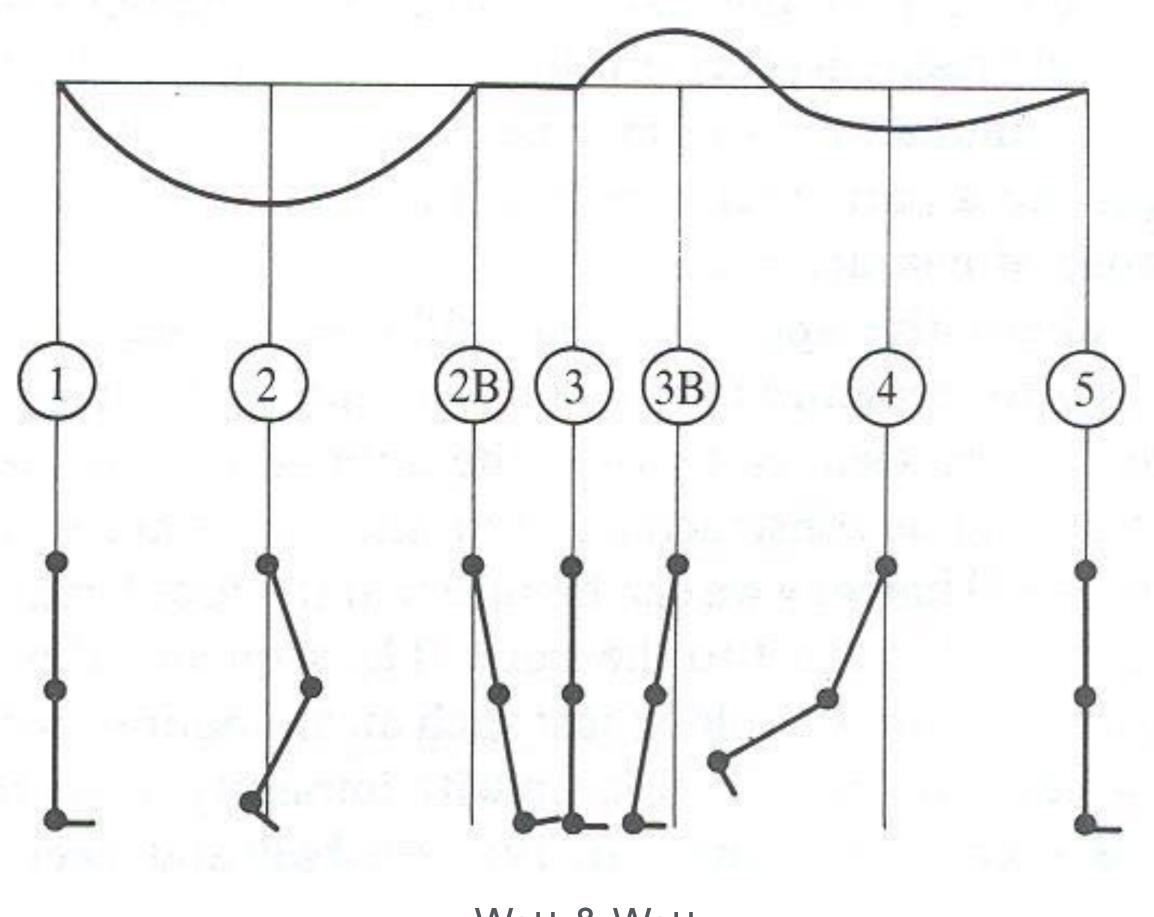
Hip joint angle



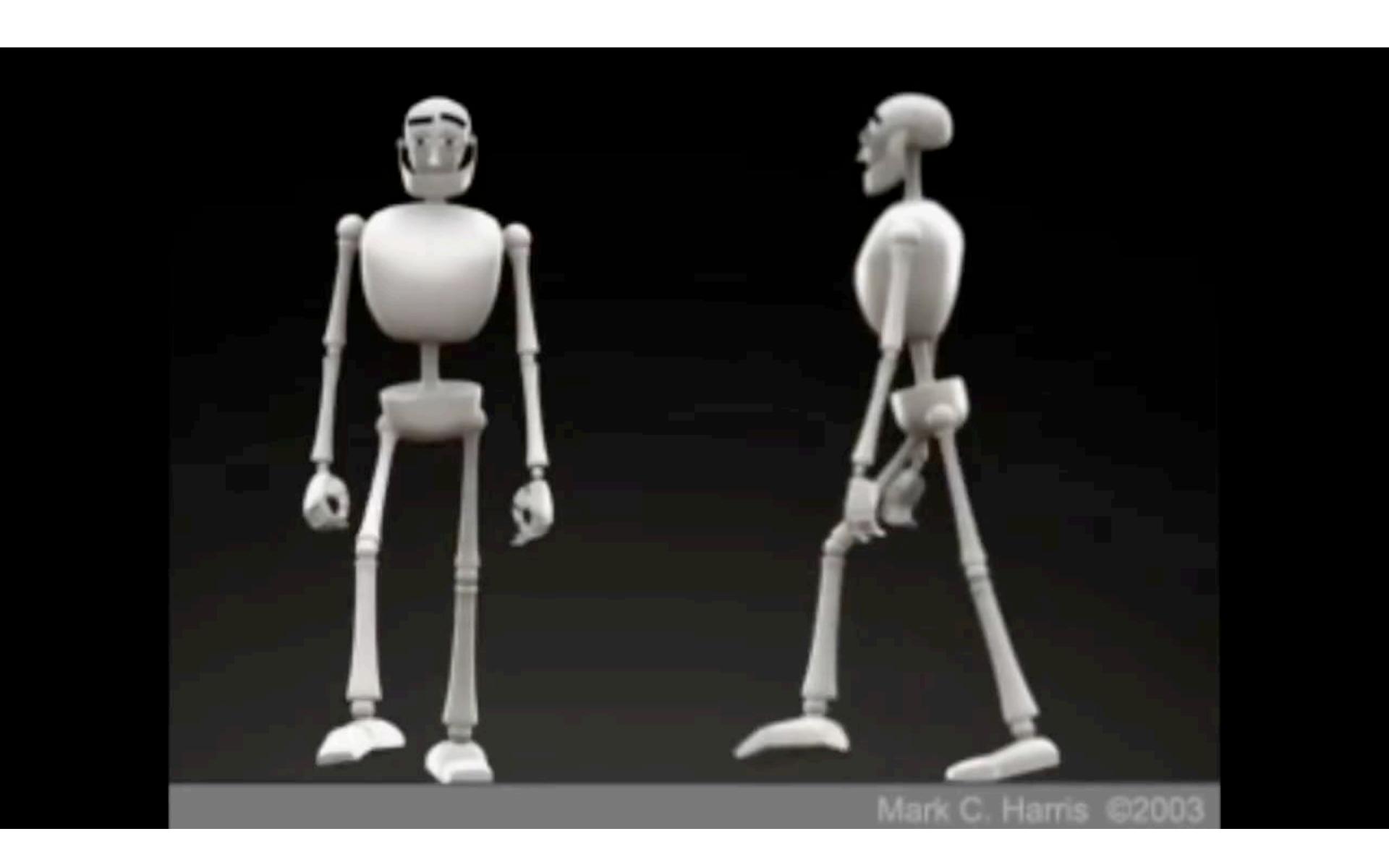
Knee joint angle



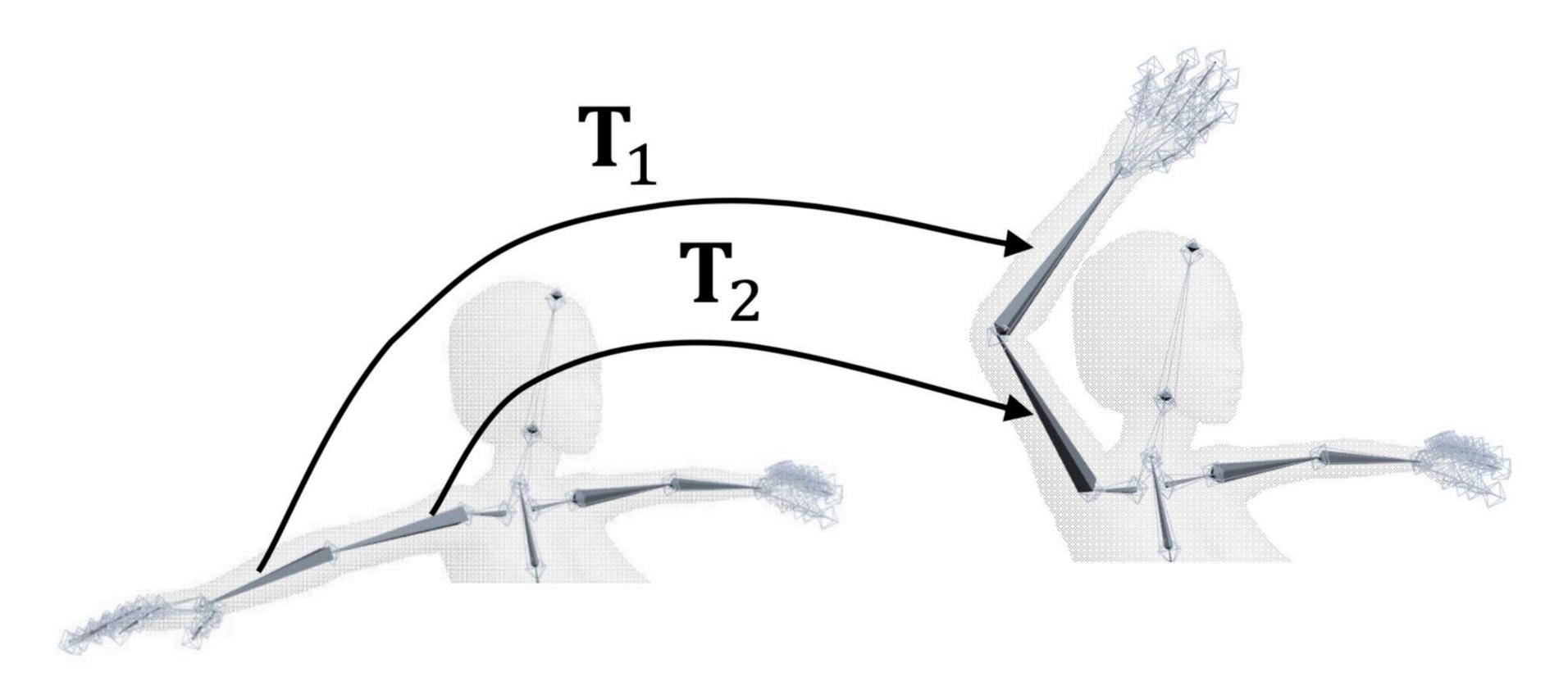
Ankle joint angle



Watt & Watt



Skinning: how to transform surface mesh vertices according to skeleton transforms



Skeleton joint transforms: T₁, T₂

Image credit: Ladislav Kavan
Stanford CS248, Winter 2021

Vertex i on mesh

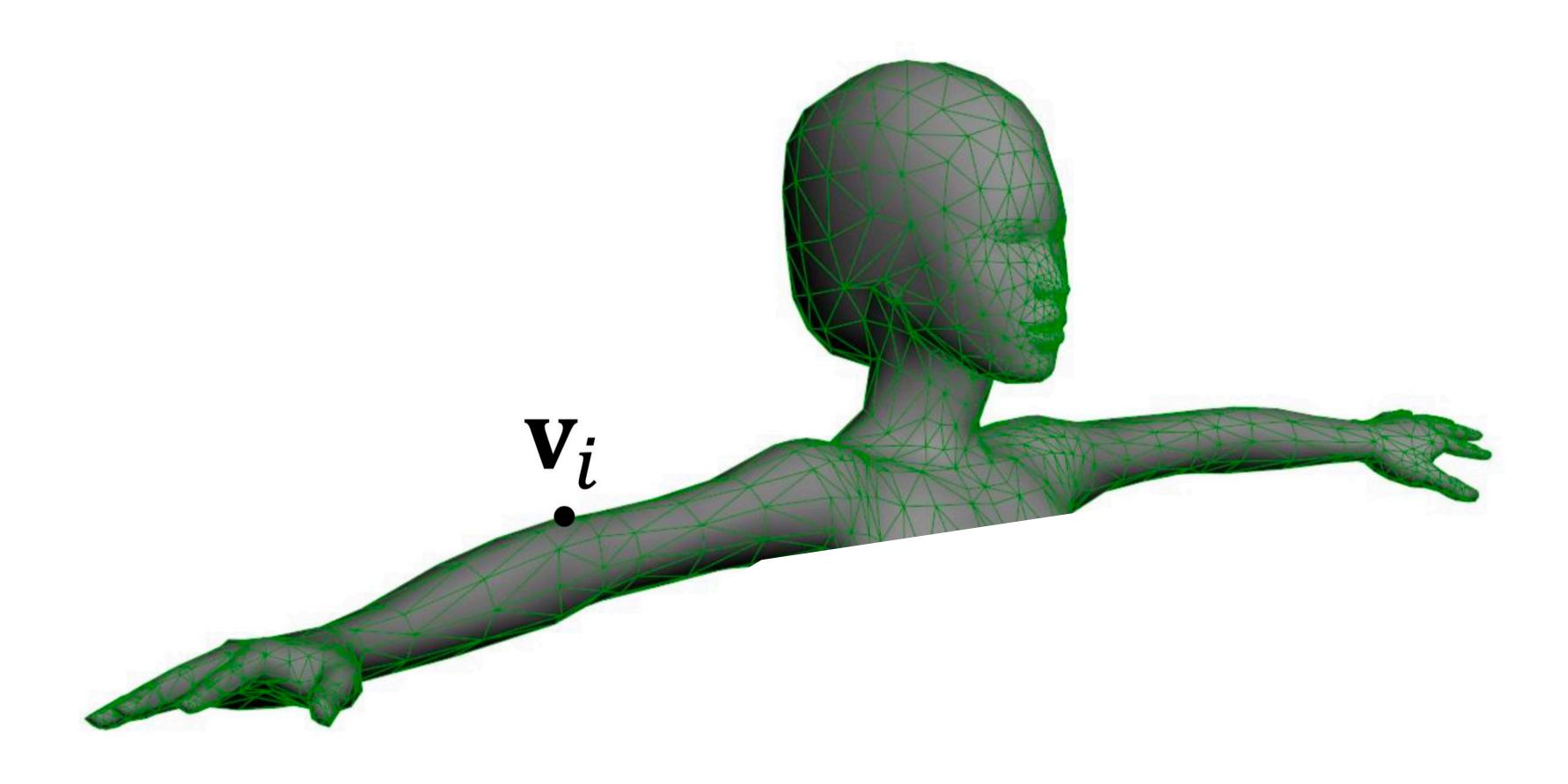
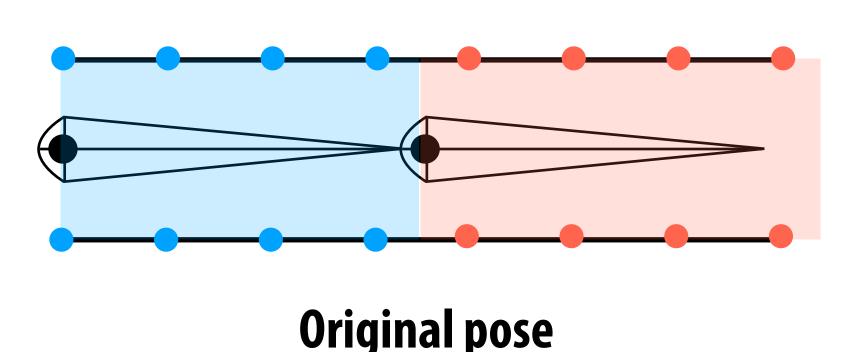


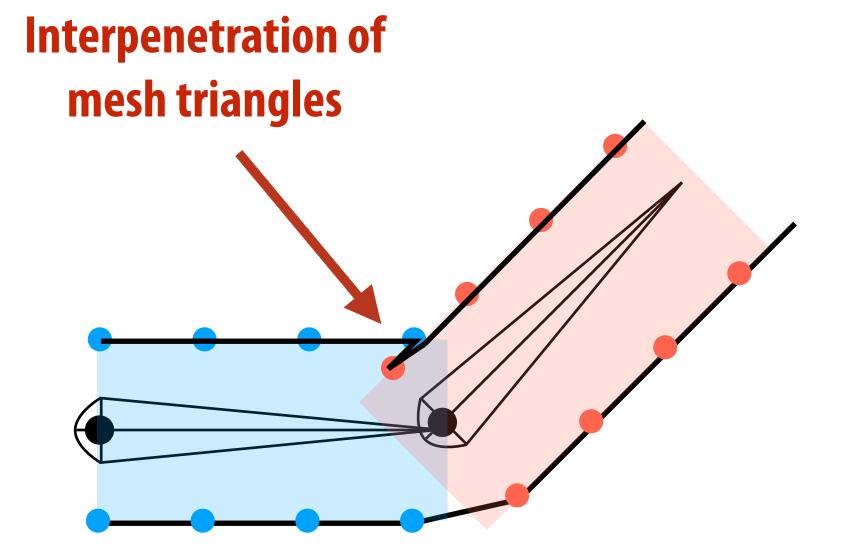
Image credit: Ladislav Kavan
Stanford CS248, Winter 2021

Rigid body skinning

 One idea: transform mesh vertices according to transform for nearby skeleton joint



Blue verts = associated with first joint **Red verts** = associated with second joint



Vertices transforms according to corresponding joint transform (notice surface interpenetration)

Linear blend skinning *

Mesh vertices transformed by *linear combination* of nearby joint transforms Very common technique for character animation in games

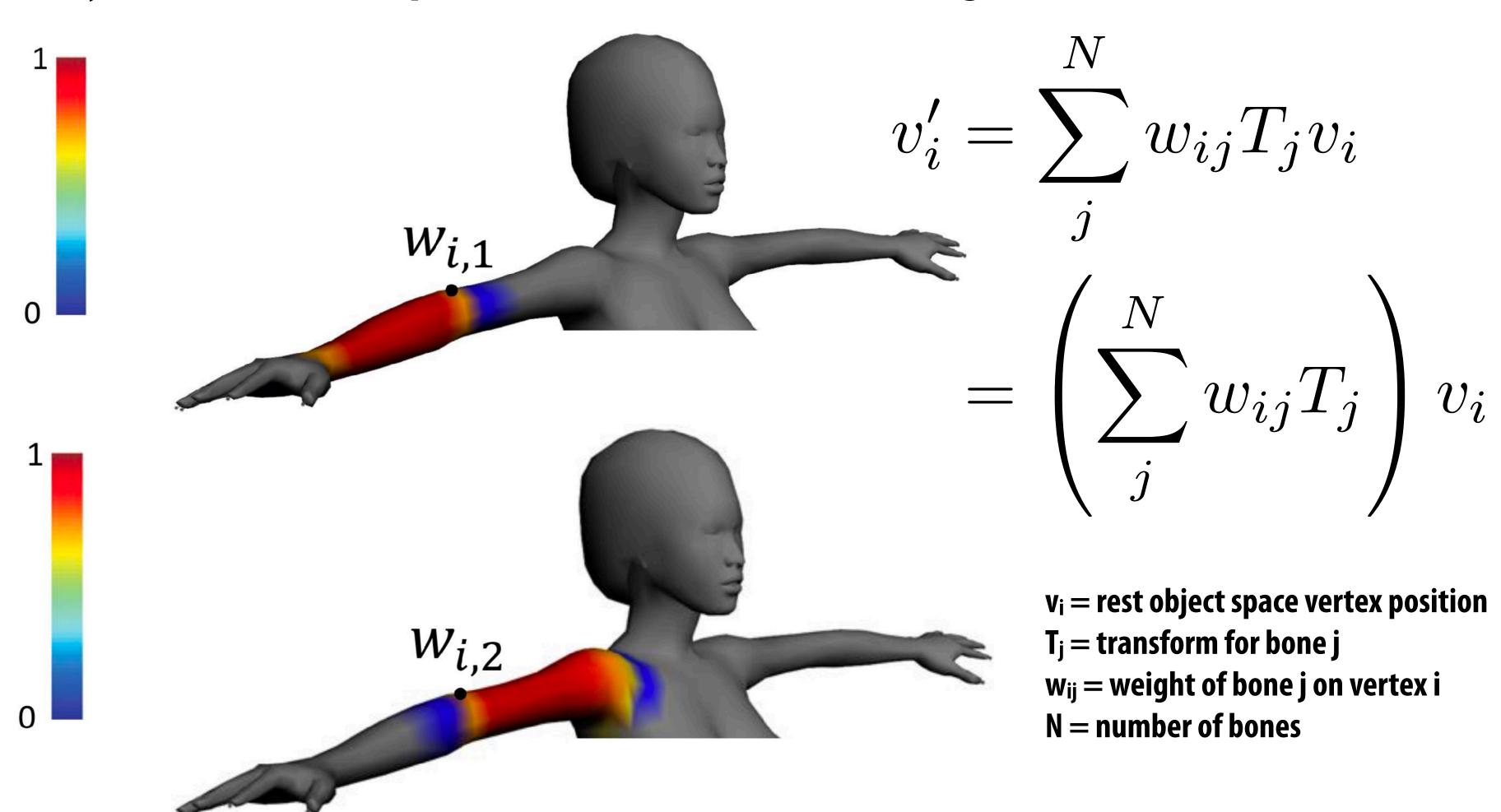
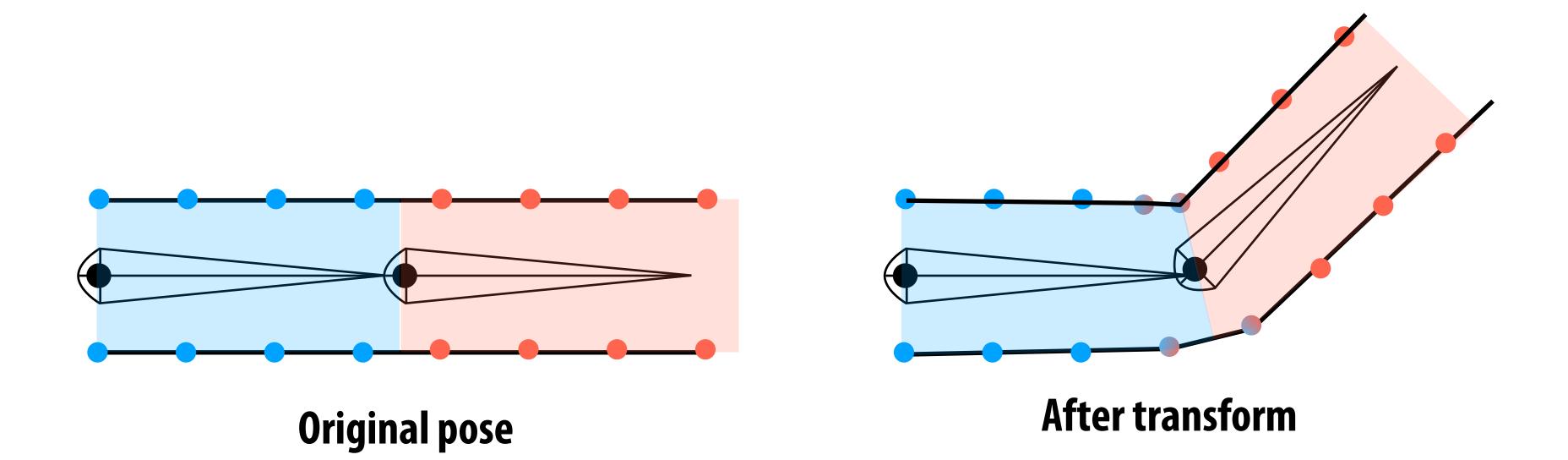


Image credit: Ladislav Kavan

^{*} Also called "matrix palette skinning" or "skeletal subspace deformation" (SSD)

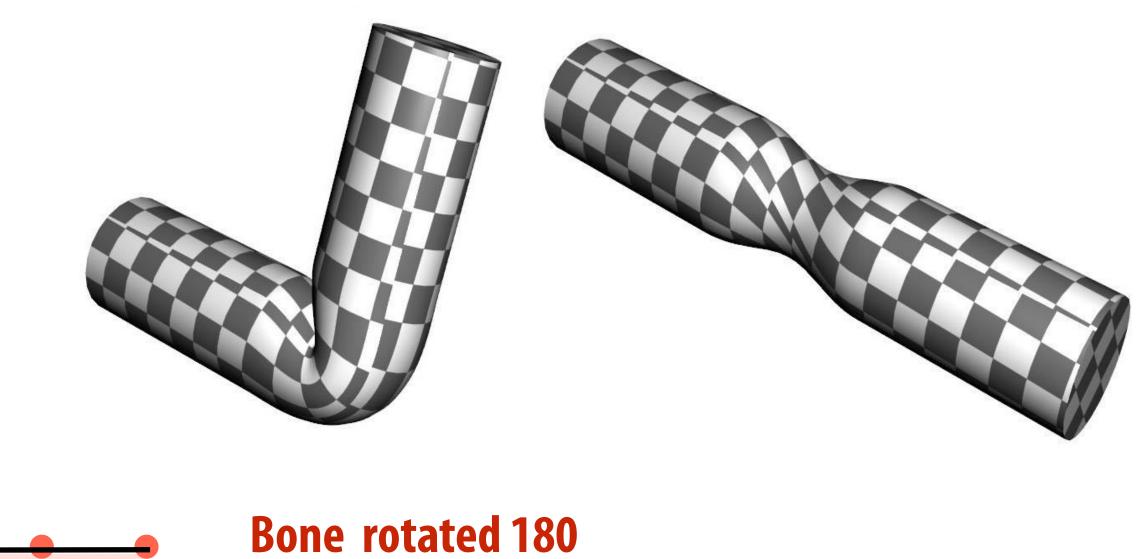
Linear blend skinning

 Transform mesh vertices according to linear combination of transforms for nearby skeleton joint

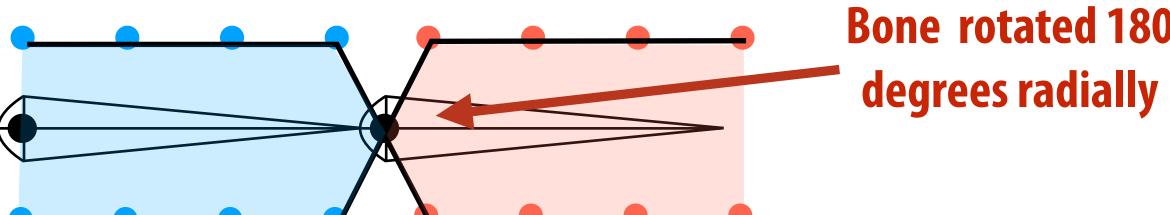


Shortcomings of linear blend skinning

Loss of volume under large transformations



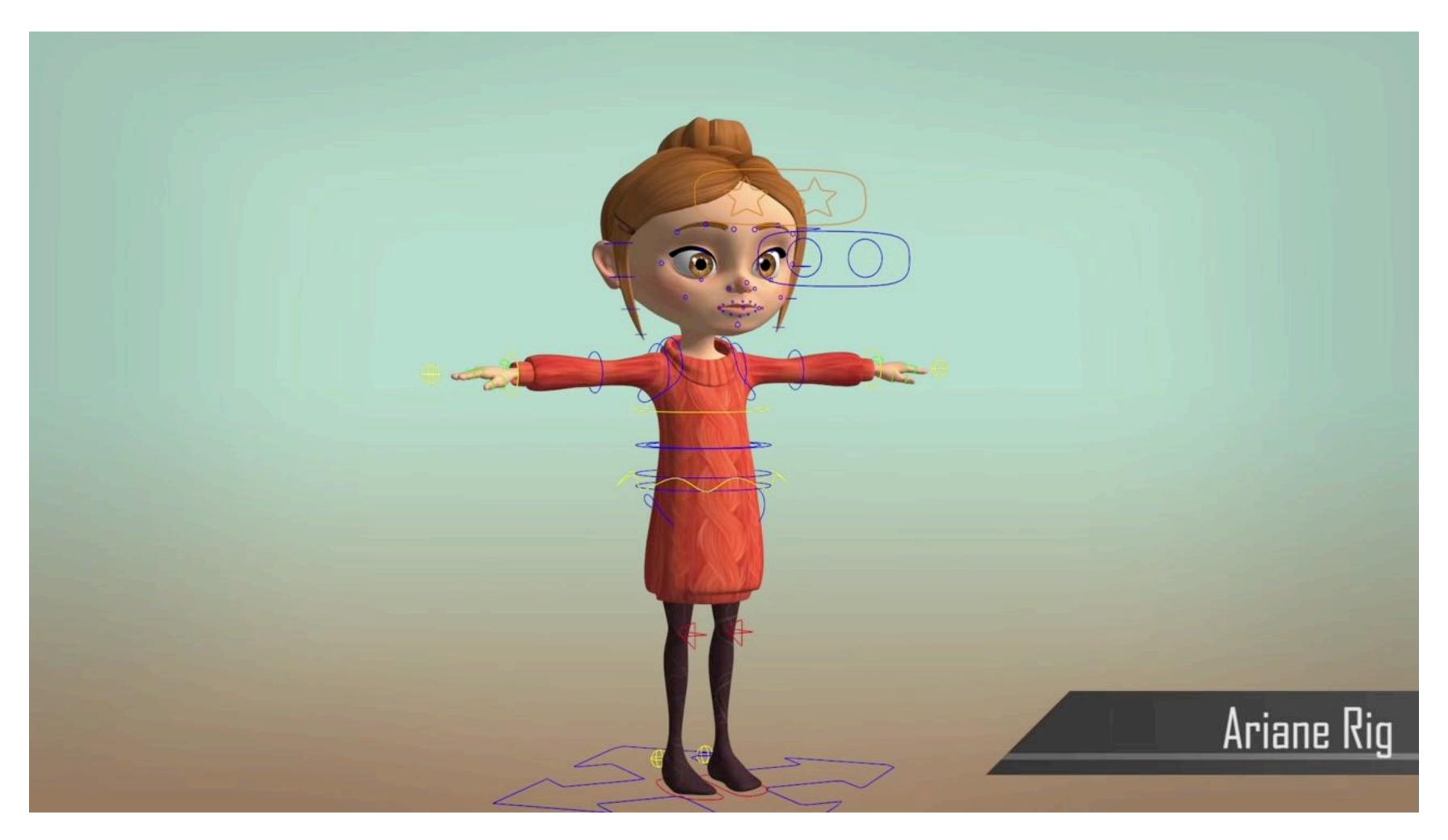
"candy wrapper effect"



Many more advanced solutions in literature: dual-quaternion skinning, joint-based deformers, etc.

Image credit: Jacka et al. Stanford CS248, Winter 2021

Skinning example



Courtesy Matthew Lailler via Keenan Crane via Ren Ng

Rigging

- "Rigging" is the process of attaching a set of animation controls to a mesh
- In the case of linear blend skinning: it is attaching a skeleton to the mesh (and setting per vertex blend weights)
- In the image to the right, the brightness of the rendering visualizes the influence of the selected joint on the mesh vertices.

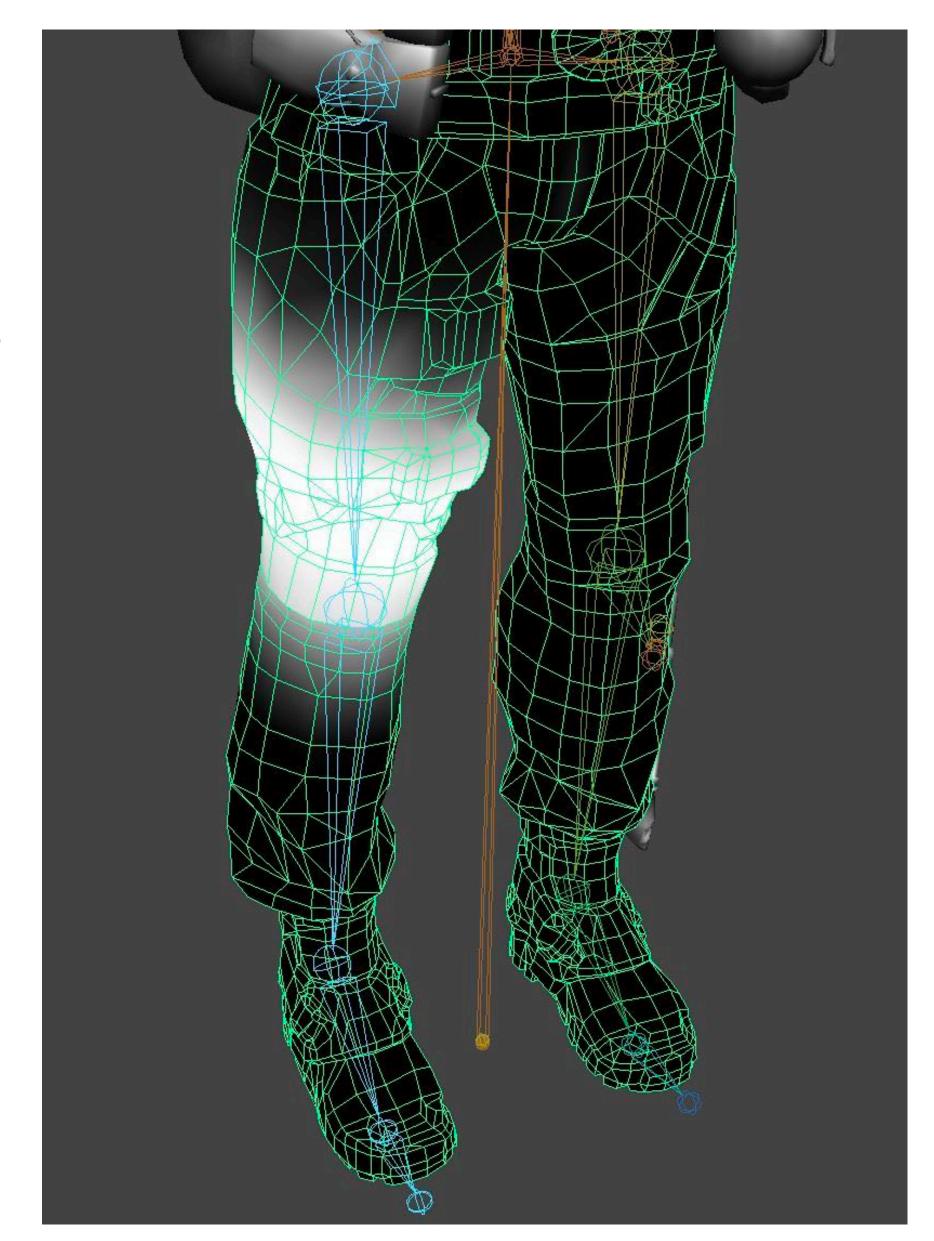


Image credit: Unreal Engine 4 Documentation (see "Paint Skin Weights" Tool)

Different ways to obtain joint angles

- Hand animate values (as discussed above)
 - For example, by defining splines that give angle over time
- Measure angles from a performance via motion capture
- Solve for angles based on higher-level goal (optimization)

Motion Capture

Motion capture

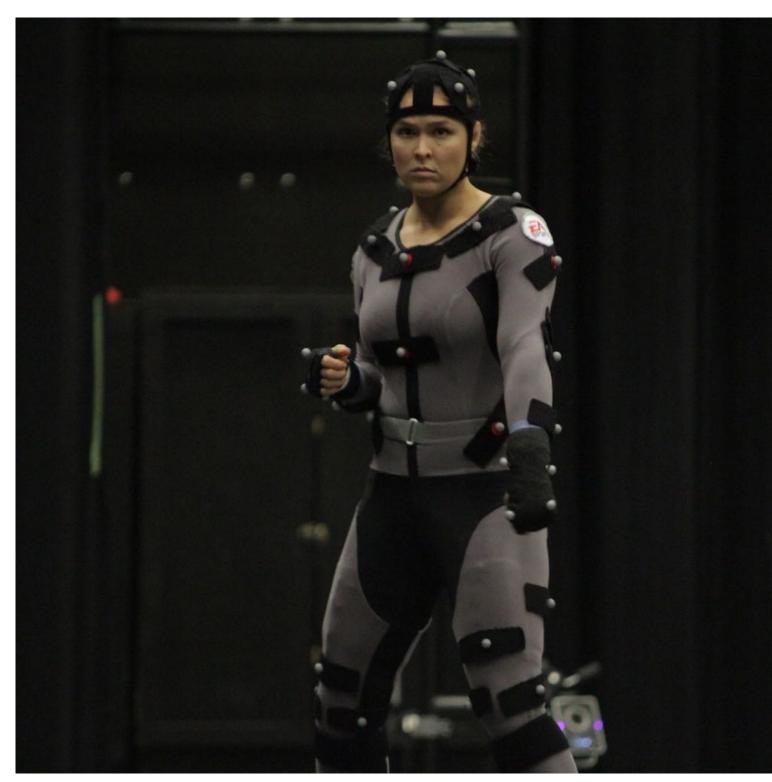
- Data-driven approach to creating animation sequences
 - Record real-world performances (e.g. person executing an activity)
 - Extract pose as a function of time from the data collected



Motion capture room for ShaqFu

Optical motion capture





Source: http://fightland.vice.com/blog/ronda-rousey-20-the-queen-of-all-media

Ronda Rousey in Electronic Arts' motion capture studio

Optical motion capture



Retroreflective markers attached to subject



IR illumination and cameras

- Affix markers to joints of subject
- Compute 3D positions by triangulation from multiple cameras
- 8+ cameras, 240 Hz, occlusions are difficult

Slide credit: Steve Marschner
Stanford CS248, Winter 2021

Motion capture pros and cons

Strengths

- Can capture large amounts of real motion data quickly
- Realism can be high

Weaknesses

- Complex and costly set-ups (but progress in computer vision is changing this)
- Occlusions (e.g., hard to capture ballroom dance)
- Captured animation may not meet artistic needs, requiring alterations

Challenges of facial animation

- "Uncanny valley"
 - In robotics and graphics
 - As artificial character appearance approaches human realism, our emotional response goes negative, (until appearance achieves a sufficiently convincing level of realism in expression)



Cartoon. Brave, Pixar



Semi-realistic. Polar Express, Warner Bros

Challenges of facial motion capture



Final Fantasy Spirits Within (2001)

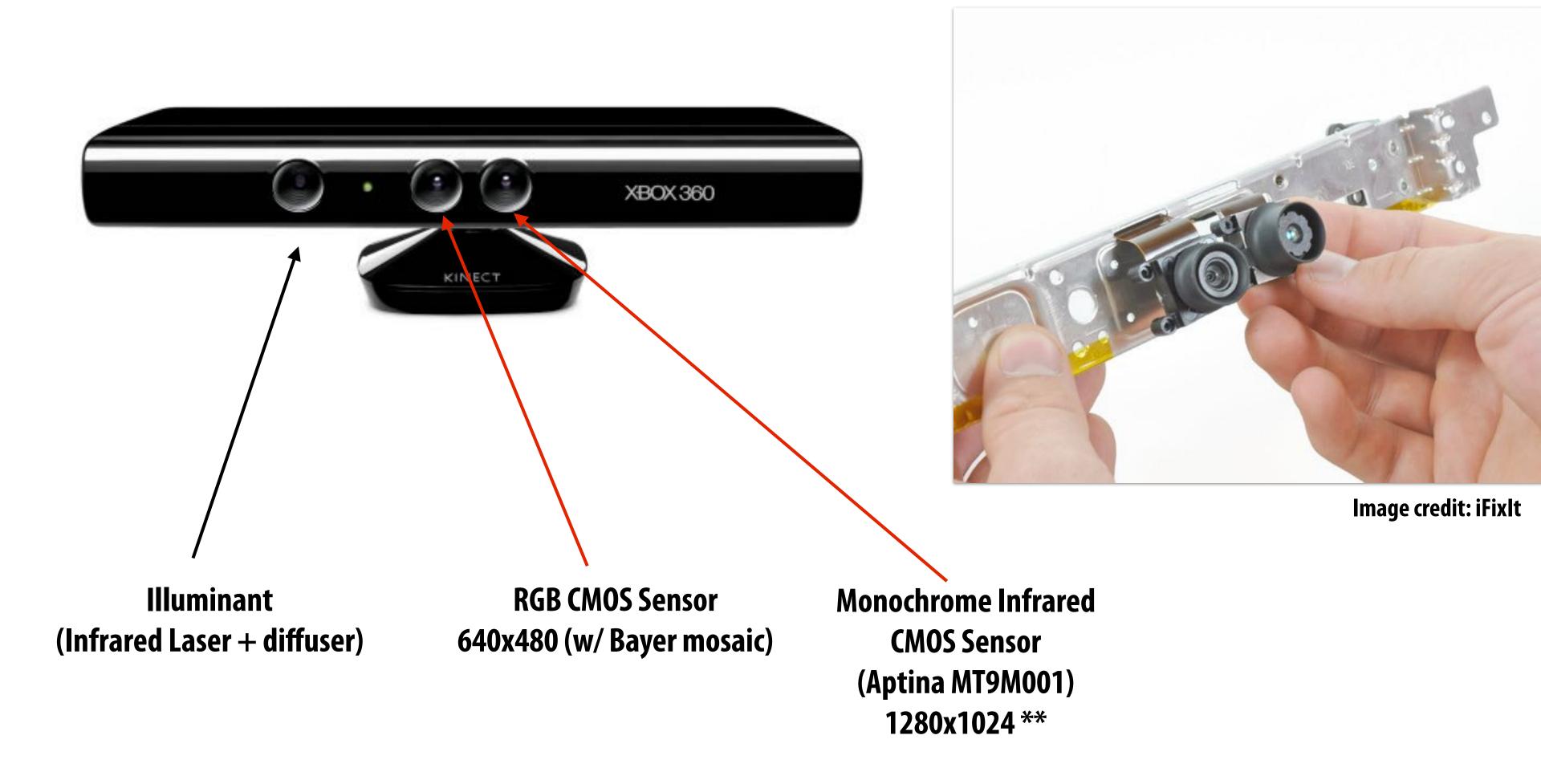
Facial motion capture



Discovery, "Avatar: Motion Capture Mirrors Emotions", https://youtu.be/1wK1lxr-UmM

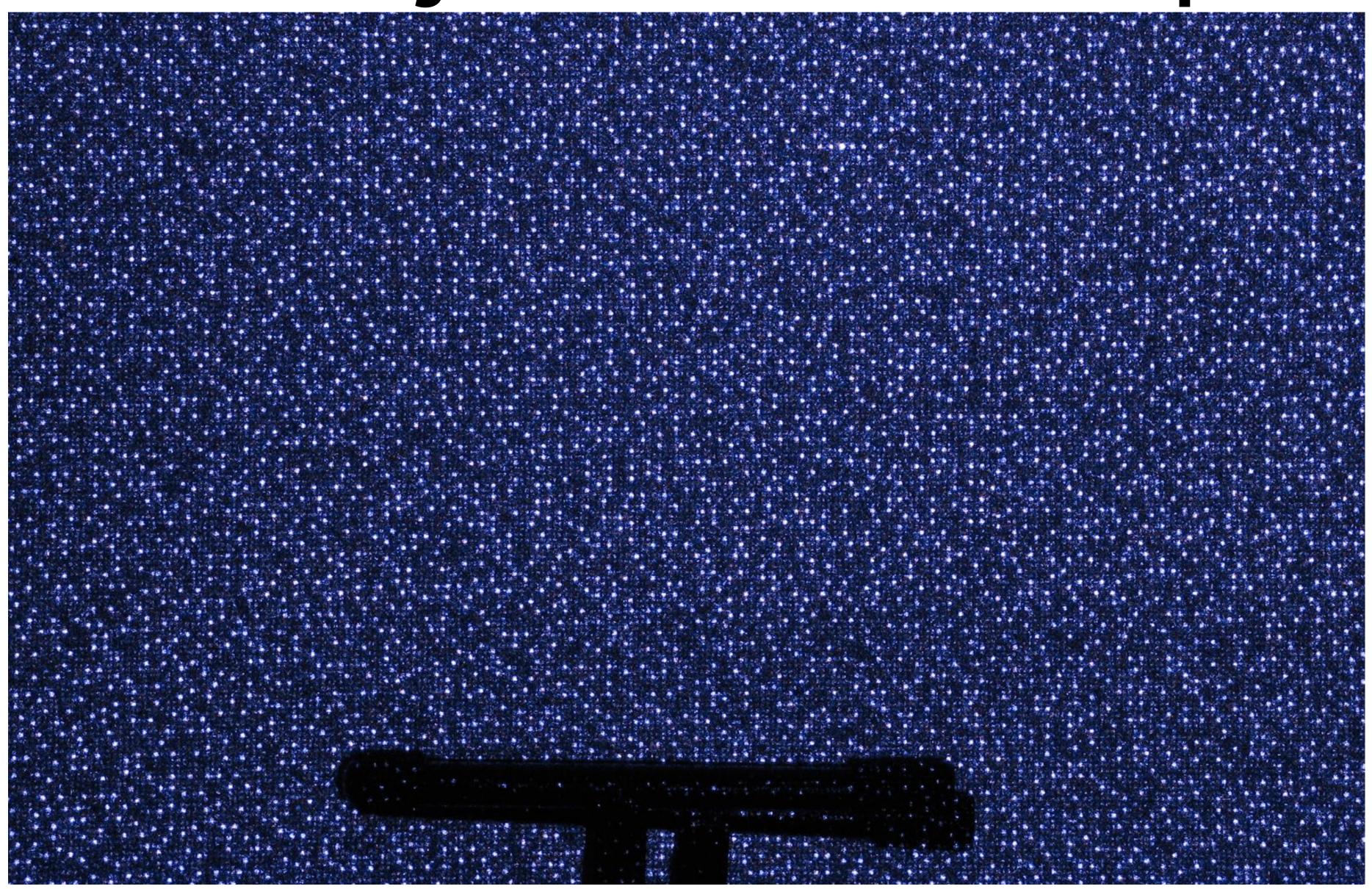
Aside: lower-cost forms of capture

Microsoft XBox 360 Kinect



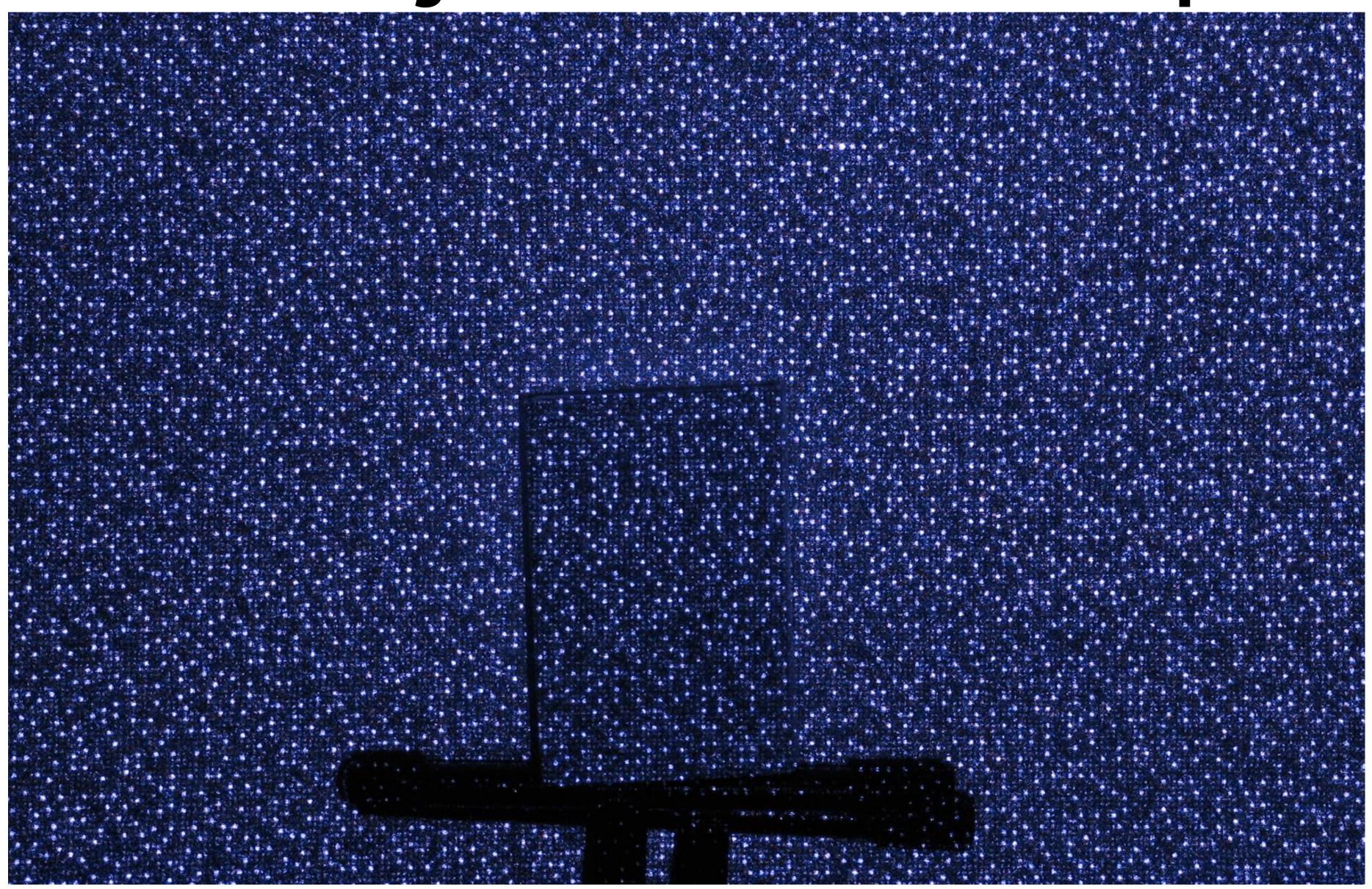
^{**} Kinect returns 640x480 disparity image, suspect sensor is configured for 2x2 pixel binning down to 640x512, then crop

Infrared image of Kinect illuminant output



Credit: www.futurepicture.org

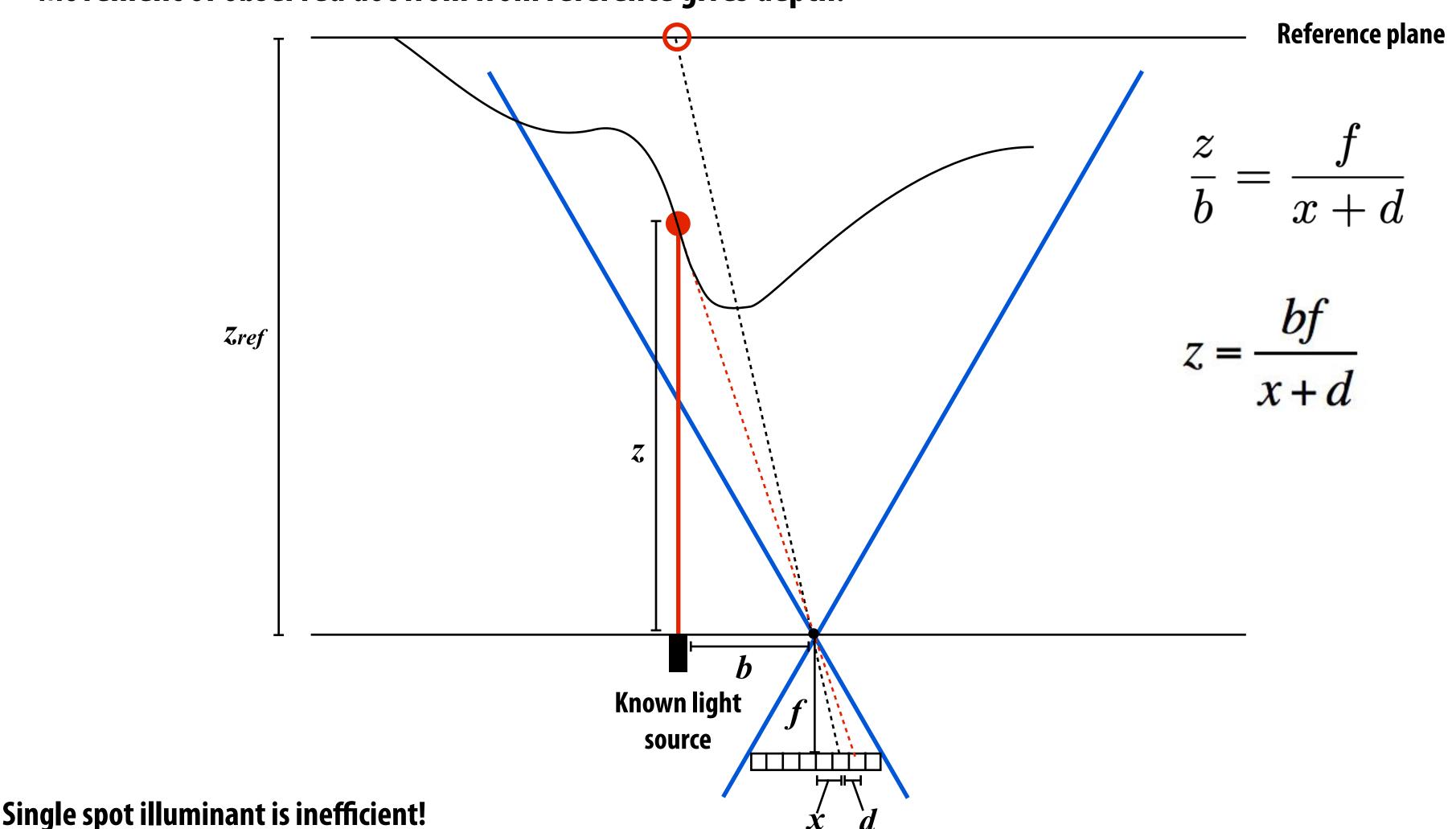
Infrared image of Kinect illuminant output



Credit: www.futurepicture.org

Depth from "disparity" using structured light

System: one light source emitting known beam + one camera measuring scene appearance If the scene is at reference plane, image that will be recorded by camera is known Movement of observed dot from from reference gives depth.



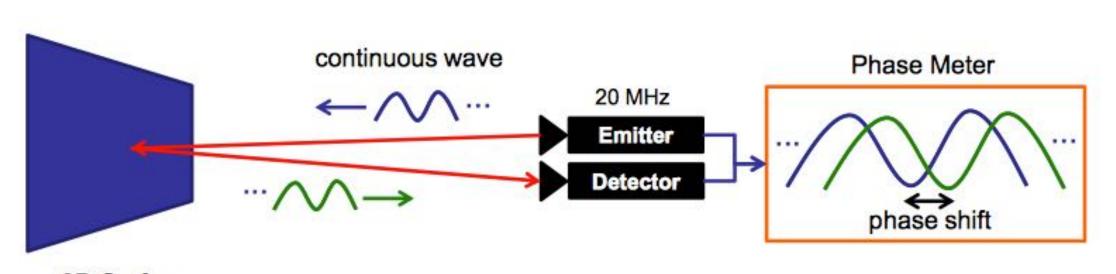
(Must "scan" scene to get depth, so high latency to retrieve a single depth image. Hence the dot pattern on the Kinect)

Xbox One Sensor

- Time-of-flight sensor (not based on structured light like the original Kinect)
- Measure phase offset of light reflected off environment
 - Phase shift proportional to distance from object
- "Computer vision" challenges in obtaining high-quality signal:
 - Flying pixels
 - Segmentation
 - Motion blur







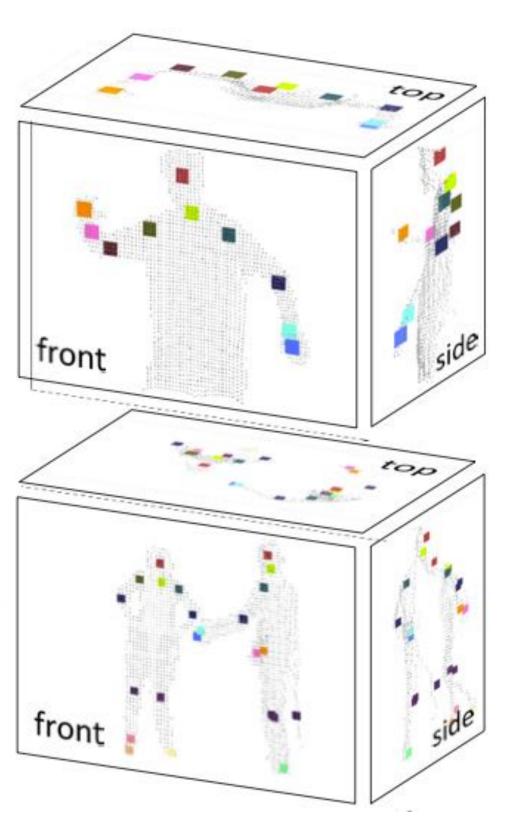
3D Surface
Image credit: V. Castaneda and N. Navab

http://campar.in.tum.de/twiki/pub/Chair/TeachingSs11Kinect/2011-DSensors_LabCourse_Kinect.pdf

Another TOF camera: Creative Depth Camera

(enabling full-body game input)





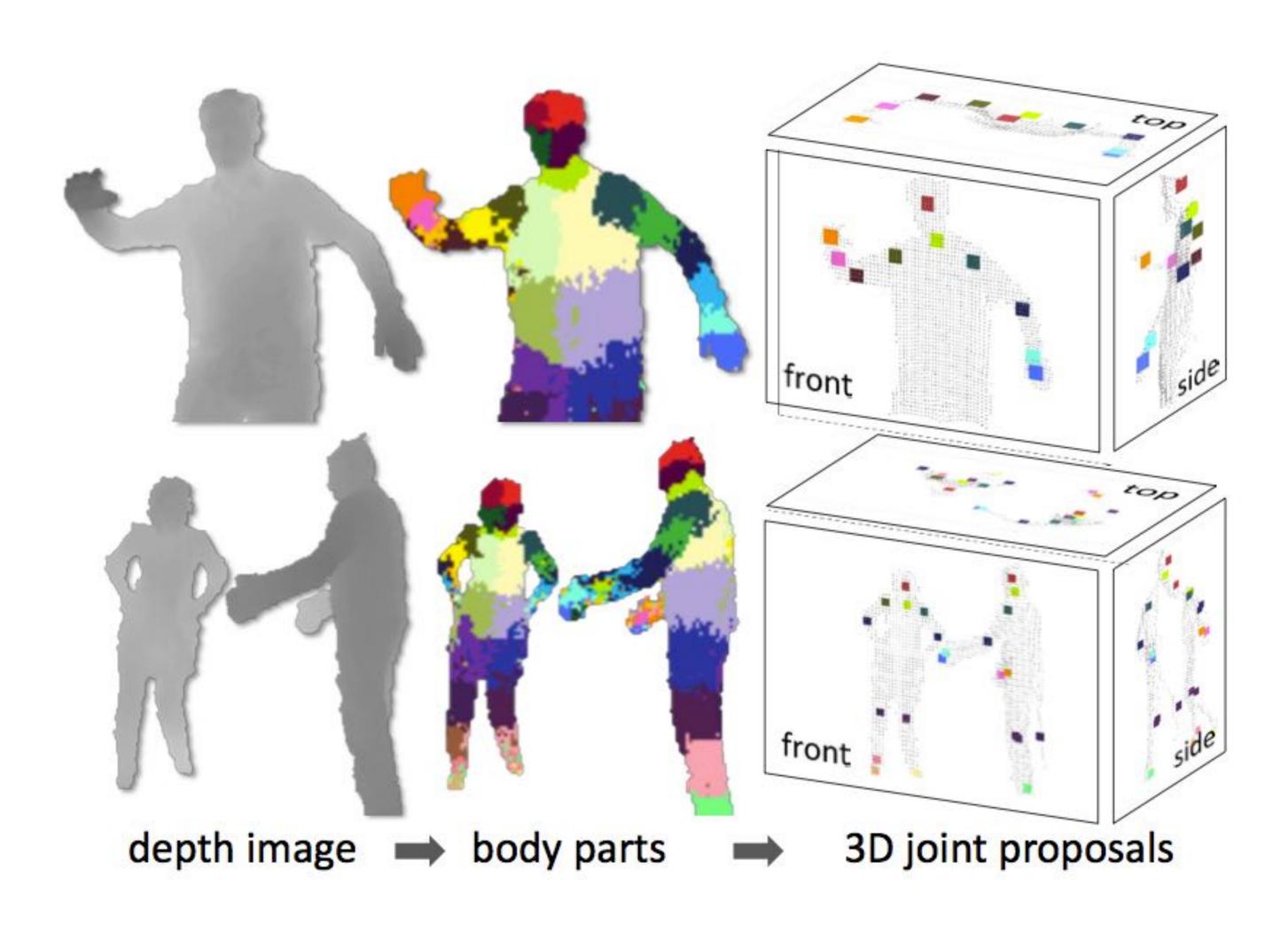
Challenge: how to determine player's position and motion from (noisy) depth images... without consuming a large fraction of the XBox 360's compute capability?

Depth Image

Character Joint Angles

Key idea: classify pixels into body regions

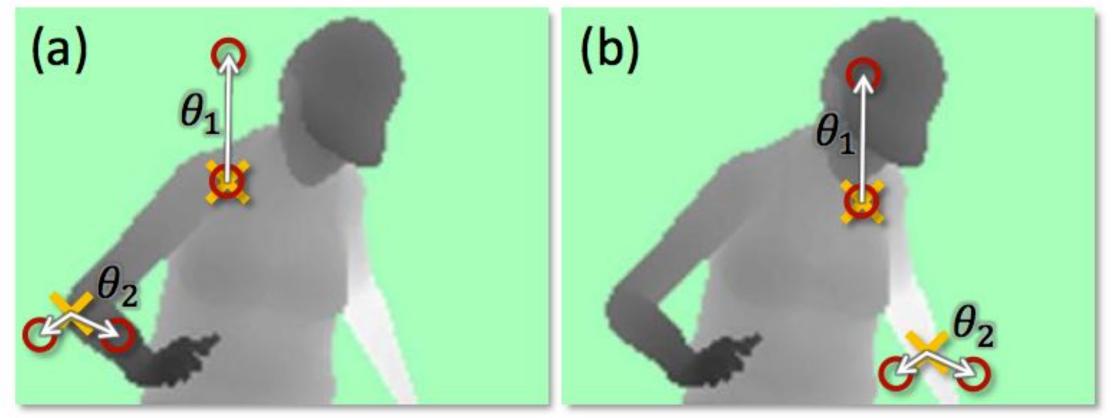
[Shotton et al. 2011]



Pixel classification

For each pixel: compute features from depth image

$$f_{\theta}(I,X) = d_I\left(X + \frac{u}{d_I(X)}\right) + d_I\left(X + \frac{v}{d_I(X)}\right) \qquad \text{Where } \theta = \left(u,v\right) \text{ and } d_I(X) \text{ is the depth image value at pixel X.}$$



Two example depth features

Features are cheap to compute + can be computed for all pixels in parallel

Features do not depend on velocities: only information from current frame

Classify pixels into body parts using randomized decision forest classifier

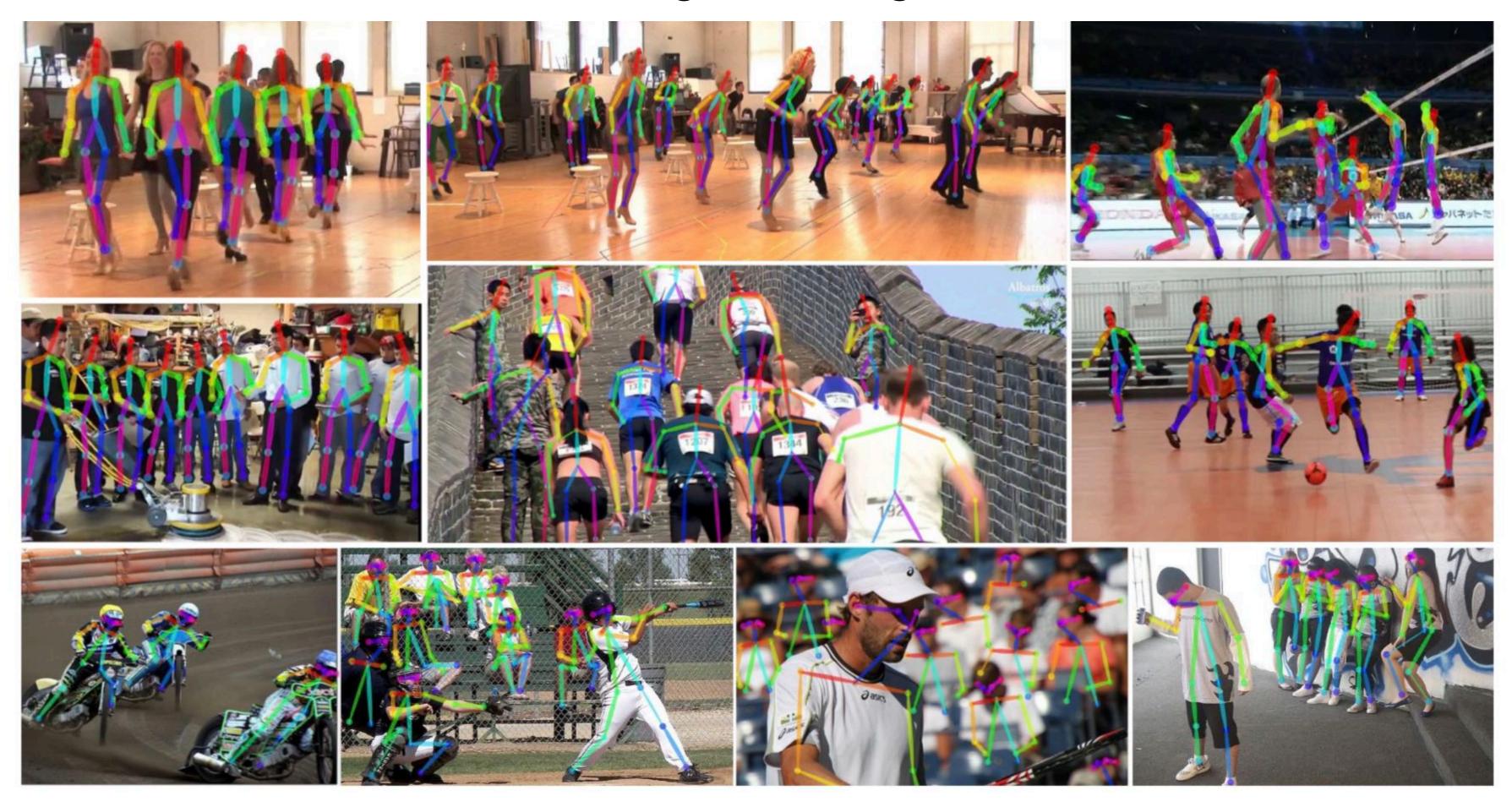
- Trained on 100K motion capture poses + database of rendered images as ground truth

Result of classification: $P(c|I,\mathbf{x})$ (probability pixel x in depth image I is body part c)

Per-pixel probabilities pooled to compute 3D spatial density function for each body part c(joint angles inferred from this density)

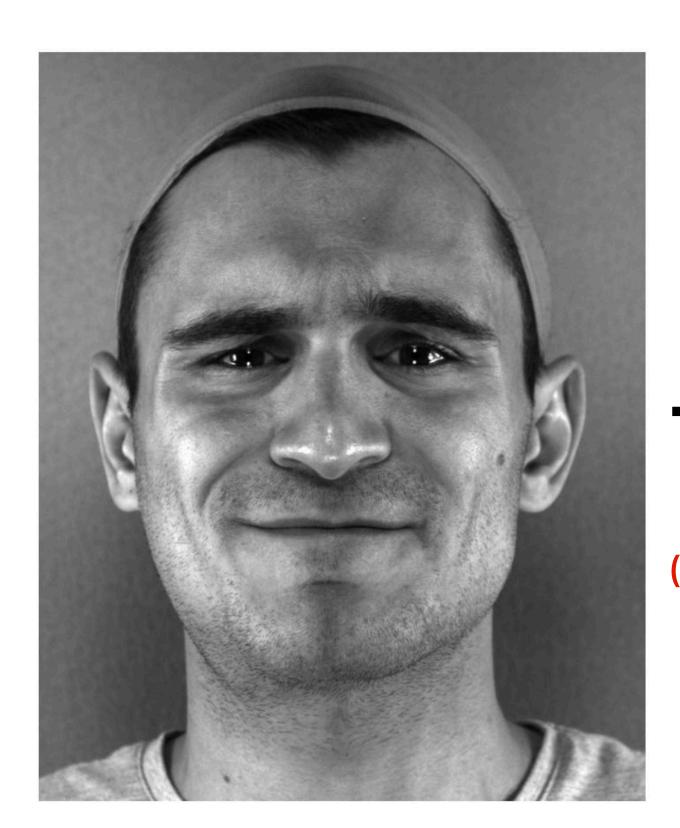
Modern computer vision approaches

■ 2D (but not 3D) skeleton from single RGB image

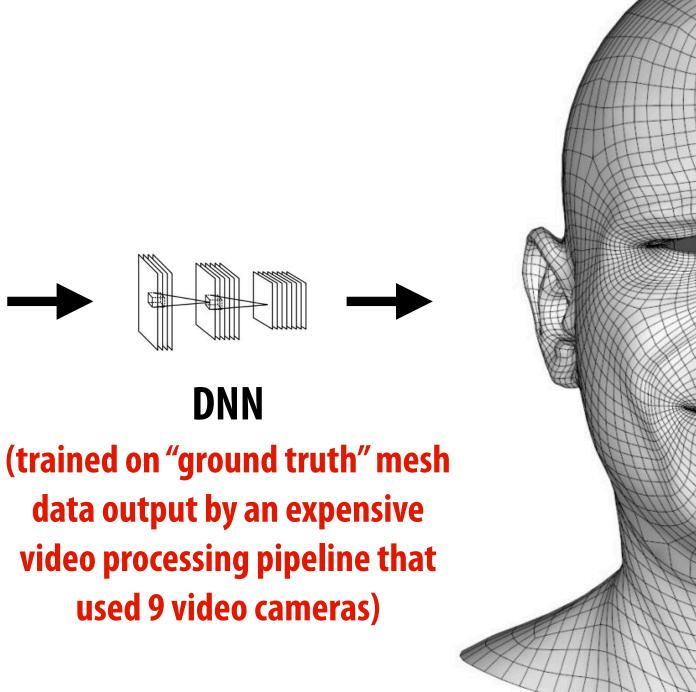


Ongoing research to obtain high-quality 3D poses

Single camera facial performance capture



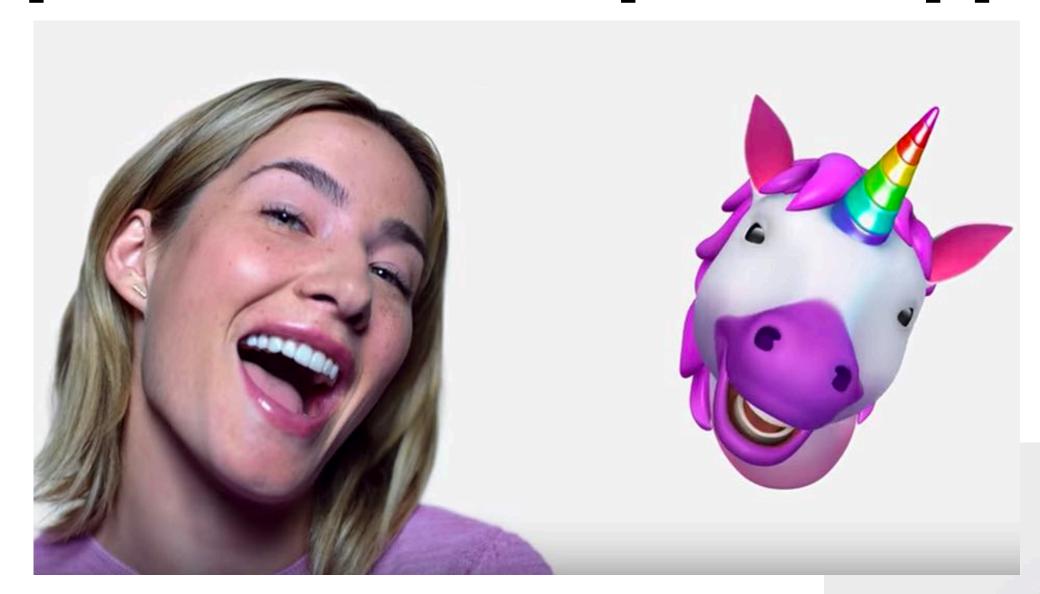
Input video frame





[Image credit: "Production-Level Facial Performance Capture Using Deep Convolutional Neural Networks", Lehtinen et al 2017]

Single smartphone camera facial performance capture (Apple Animoji)

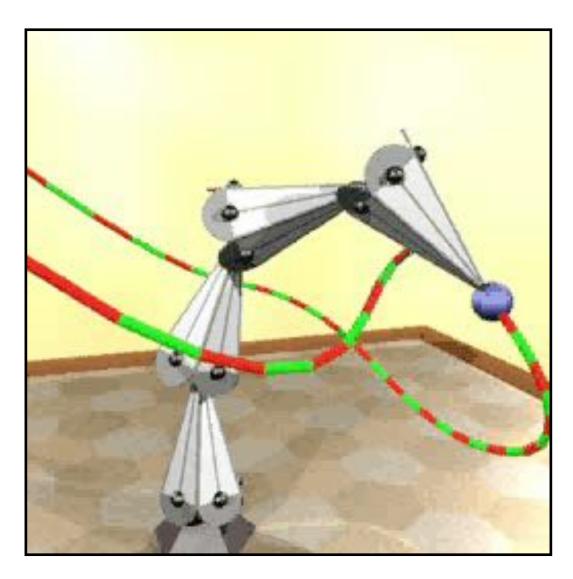


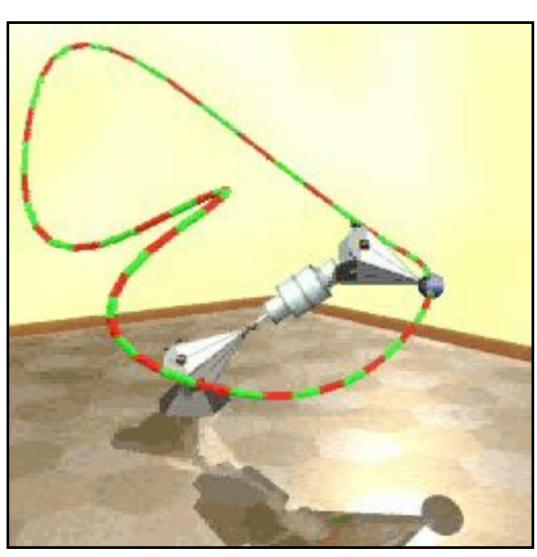
So far... we've discussed hand animating or directly measuring joint positions

Inverse Kinematics

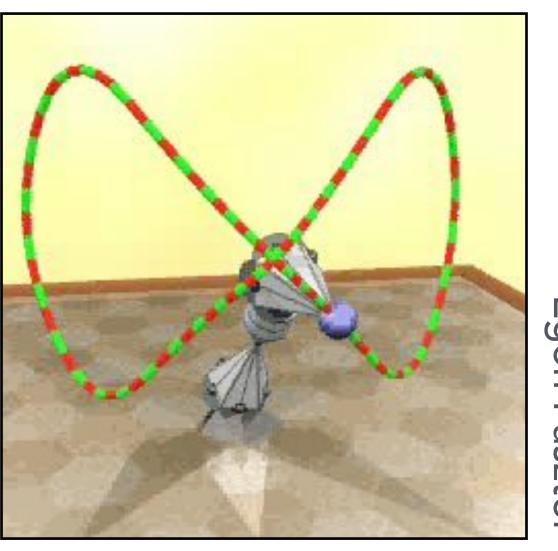
(computer solves for joint angles based on high-level goal)

Example: inverse kinematics



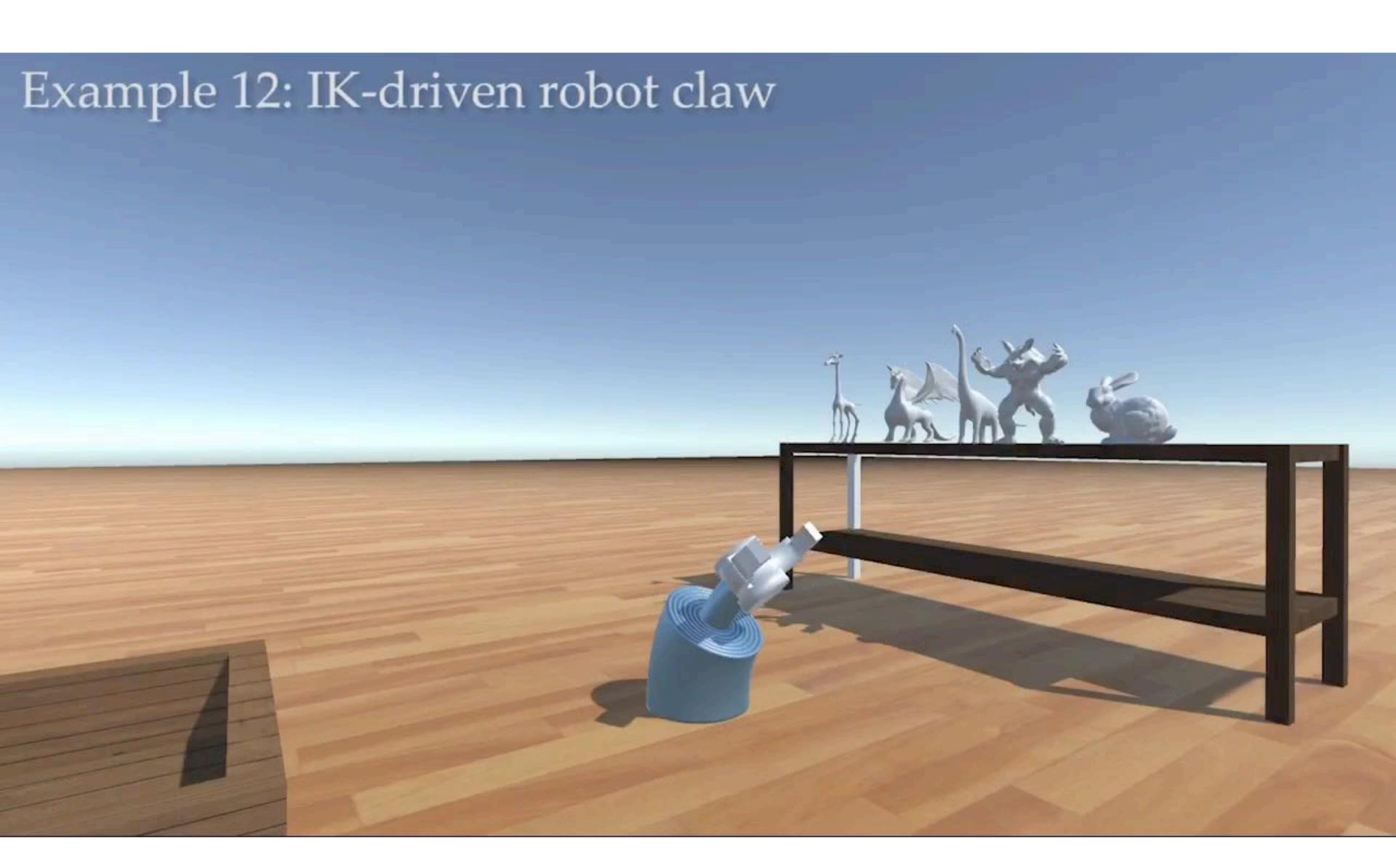






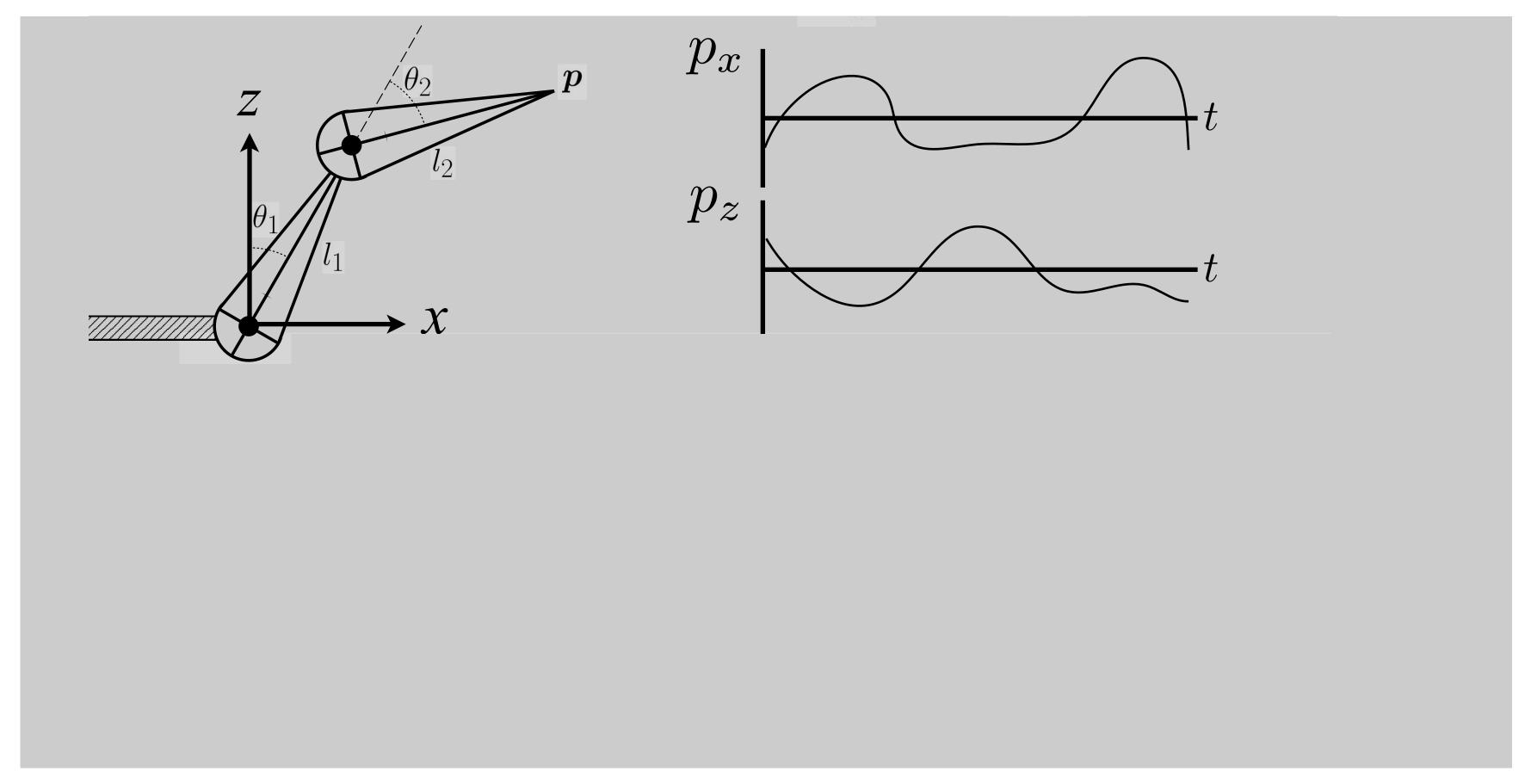
Egon Pasztor

Example: inverse kinematics



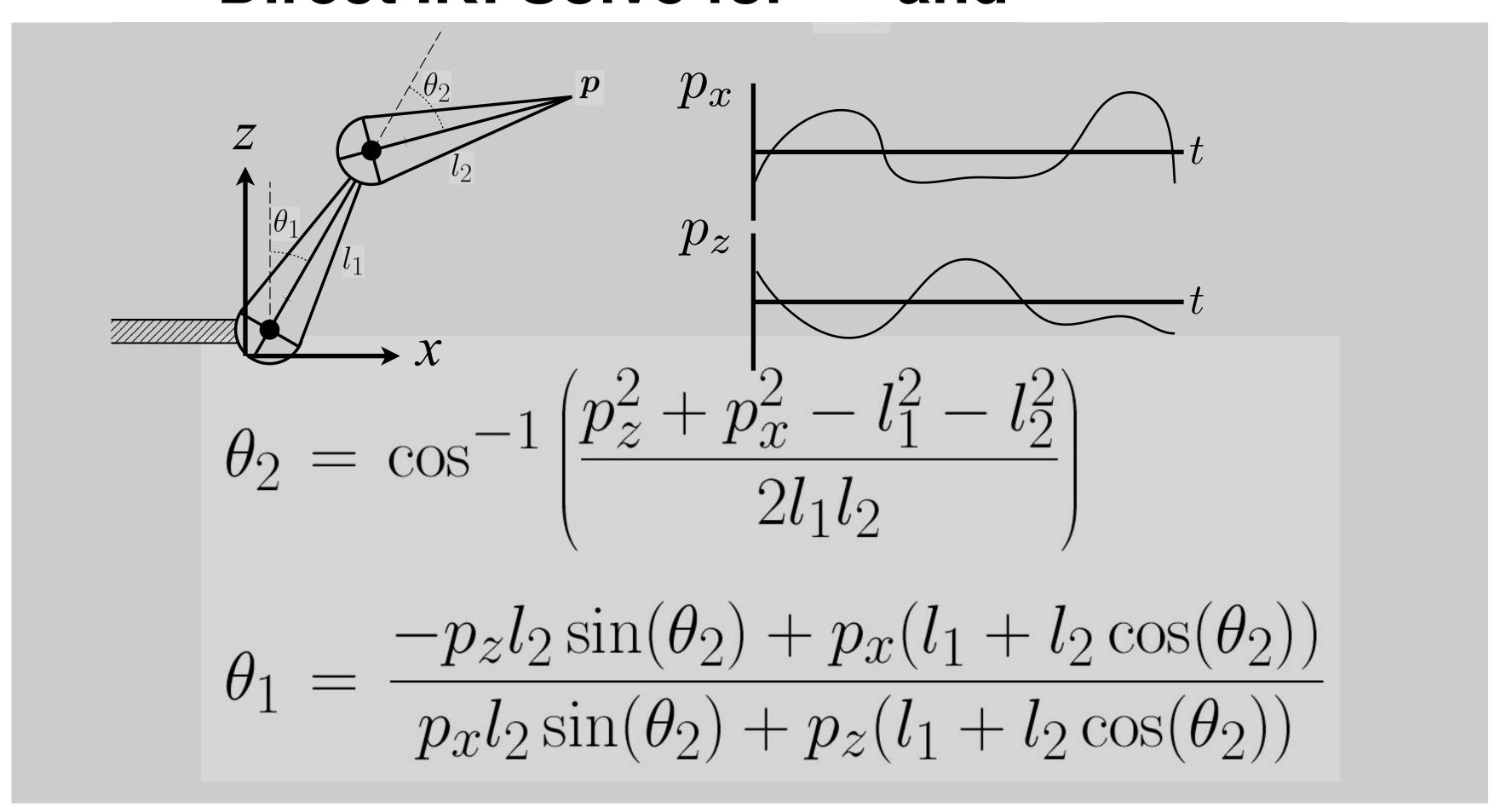
Input: animator provides position of end-effector

Output: computer must determine joint angles that satisfy constraints Direct IK: Solve for and



Direct inverse kinematics: for two-segment arm, can solve for parameters analytically (not true for general N-link problem)

Direct IK: Solve for and

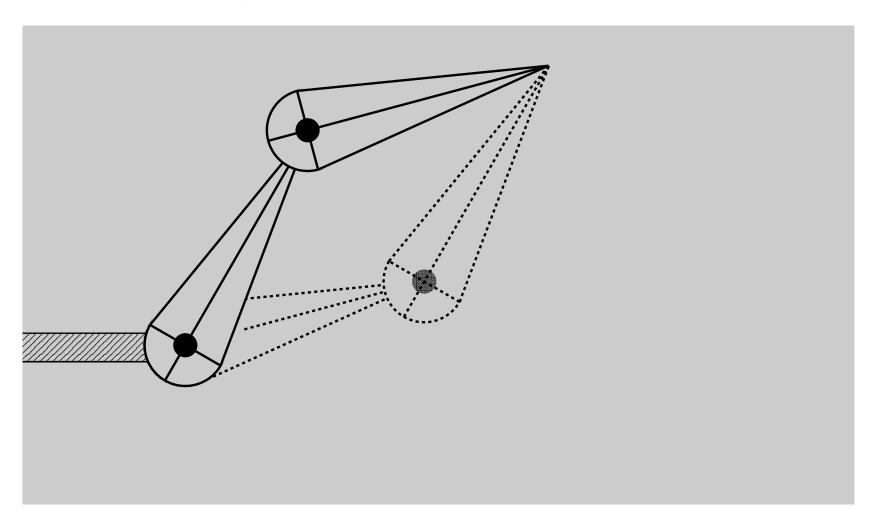


- Why is the problem hard?
 - Multiple solutions in configuration space (and these may not be nearby, causing jumps from frame-to-frame)

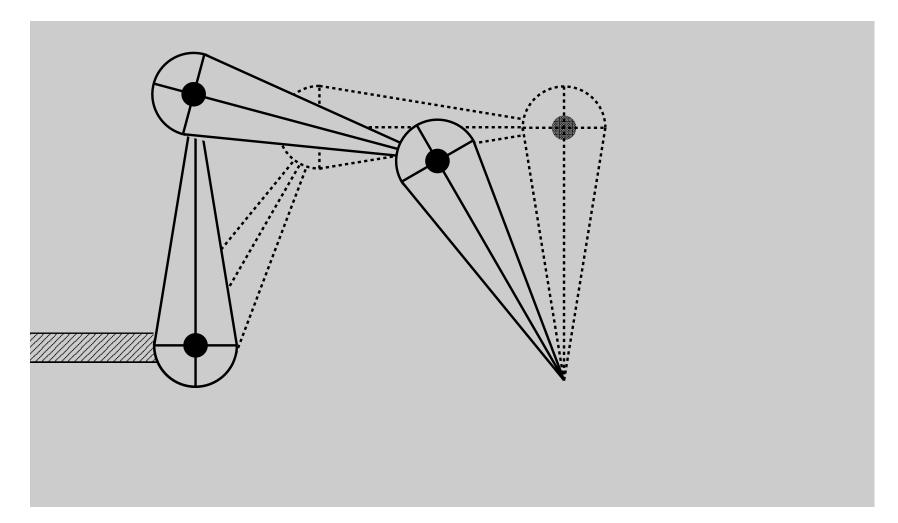
 Why is this a hard problem?... Why is this a hard problem?

- Why is this a hard problem? - Solution may not be possible

Multiple solutions separated in configuration space



Multiple solutions connected in configuration space



- Numerical solution to general N-link IK problem
 - Choose an initial configuration
 - Define an error metric (e.g. square of distance between goal and end effector's current position)
 - Apply *optimization method* to solve for joint angles given the desired (goal) end effector position

A few bits on optimization

(a commonly used tool in graphics)

Optimization problem in standard form

Can formulate most continuous optimization problems this way:

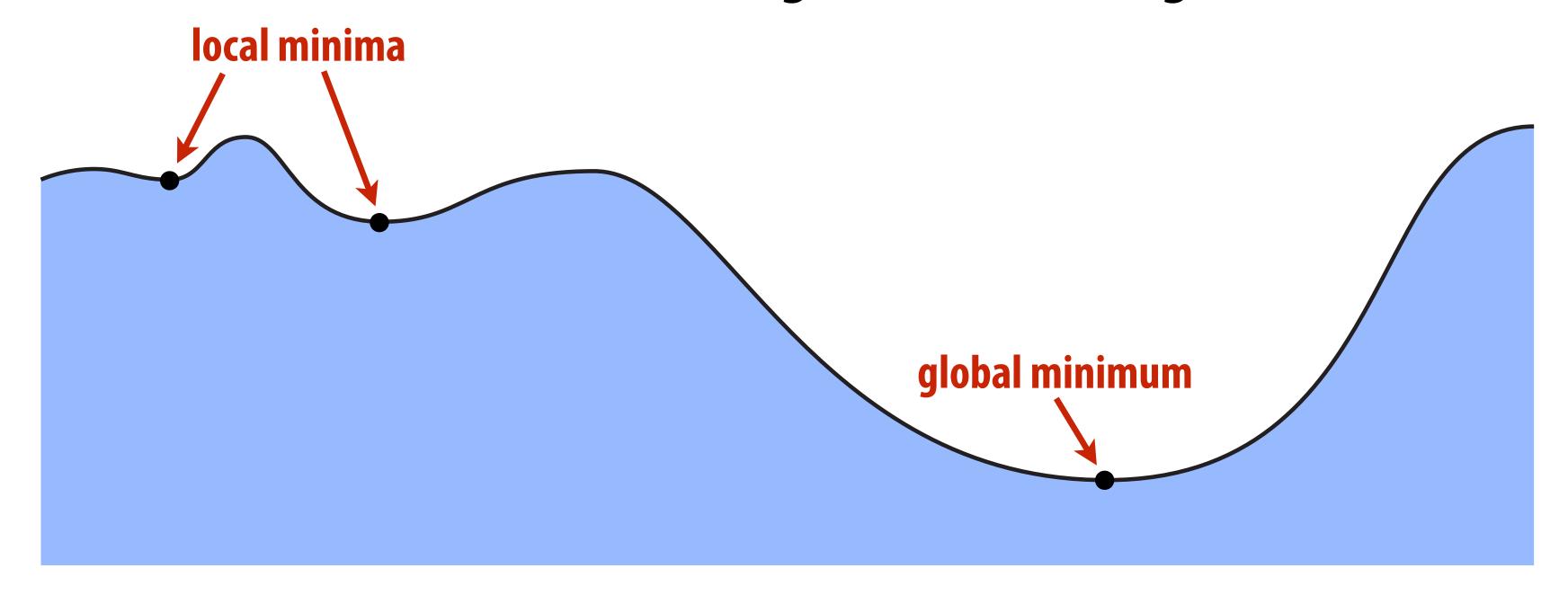
"objective": how much does solution x cost?

$$\min_{x\in\mathbb{R}^n} f_0(x) \qquad \qquad (f_i:\mathbb{R}^n\to\mathbb{R},\ i=0,\dots,m) \\ \text{often (but not always) continuous, differentiable, ...} \\ \text{subject to} \qquad f_i(x)\leq b_i,\ i=1,\dots,m \\ \text{"constraints": what must be true about x? ("x is feasible")}$$

- Optimal solution x* has smallest value of f₀ among all feasible x
- Q: What if we want to *maximize* something instead?
- A: Just flip the sign of the objective!
- Q: What if we want equality constraints, rather than inequalities?
- A: Include two constraints: $g(x) \le c$ and $-g(x) \le -c$

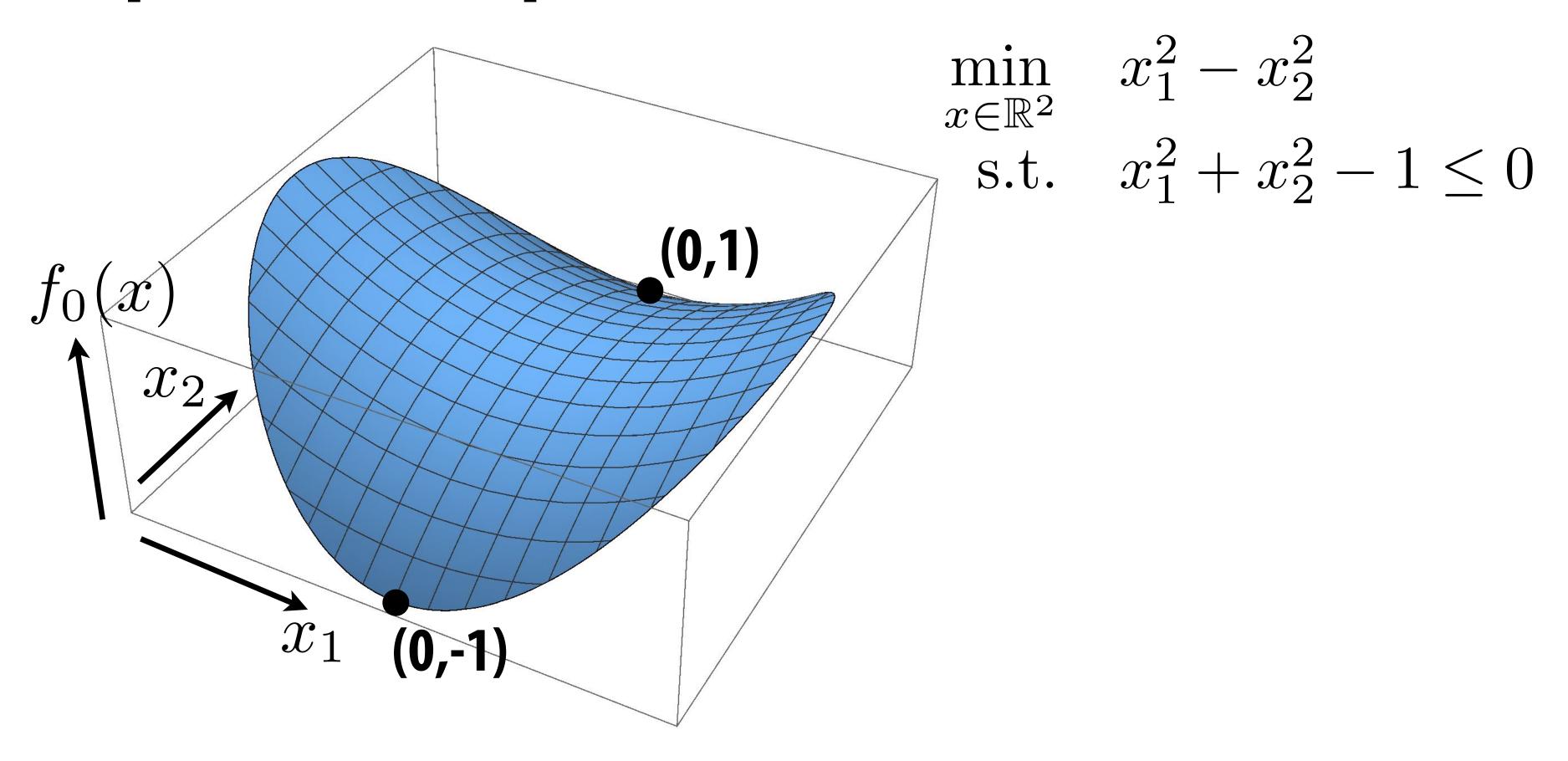
Local vs. global minima

- Global minimum is absolute best among all possibilities
- *Local* minimum is best "among immediate neighbors"



Philosophical question: does a local minimum "solve" the problem?

Optimization problem, visualized



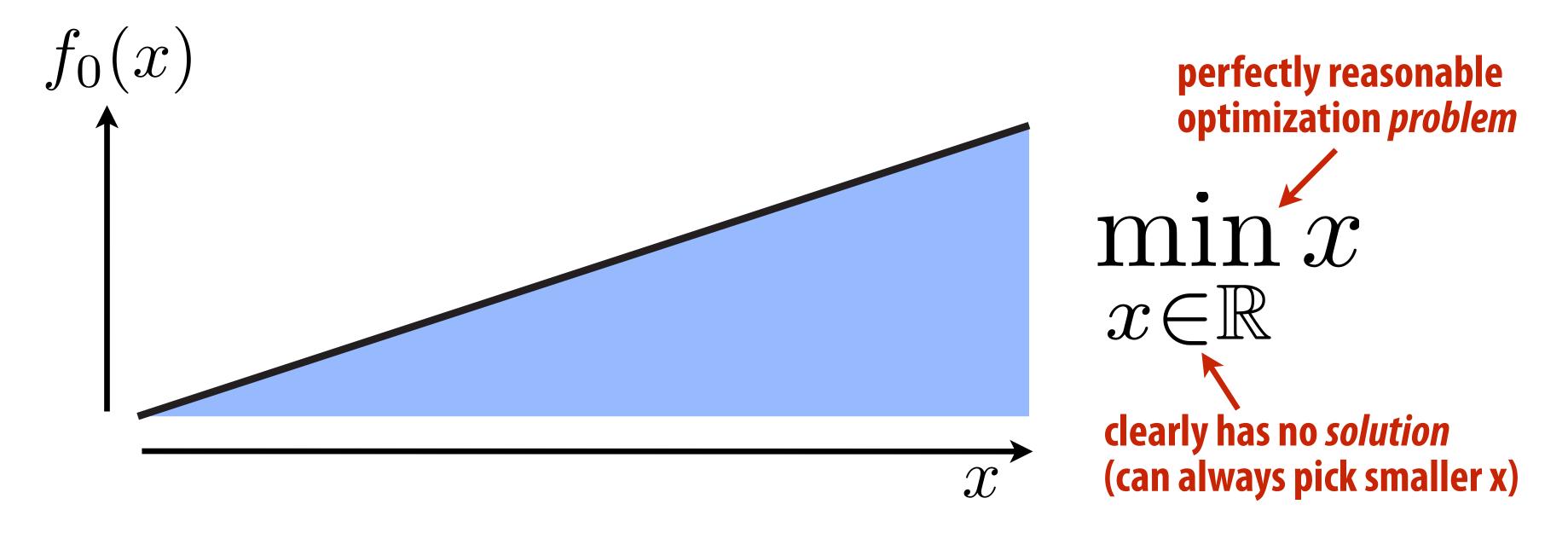
Q: Is this an optimization problem in standard form?

A: Yes

Q: Where is the optimal solution? A: There are two, (0,1), (0,-1)

Existence and uniqueness of minimizers

- Already saw that (global) minimizer is not unique
- Does it always exist? Why?
- Just consider all possibilities and take the smallest one, right?

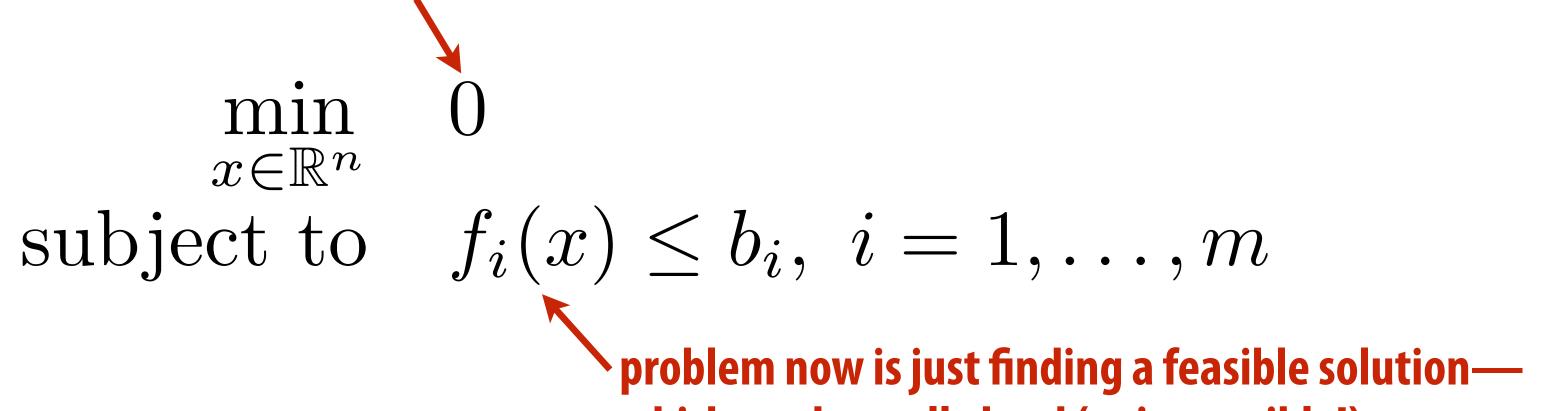


■ WRONG! Not all objectives are bounded from below.

Feasibility

- Ok, but suppose the objective is bounded from below
- Then we can just take the best feasible solution, right?

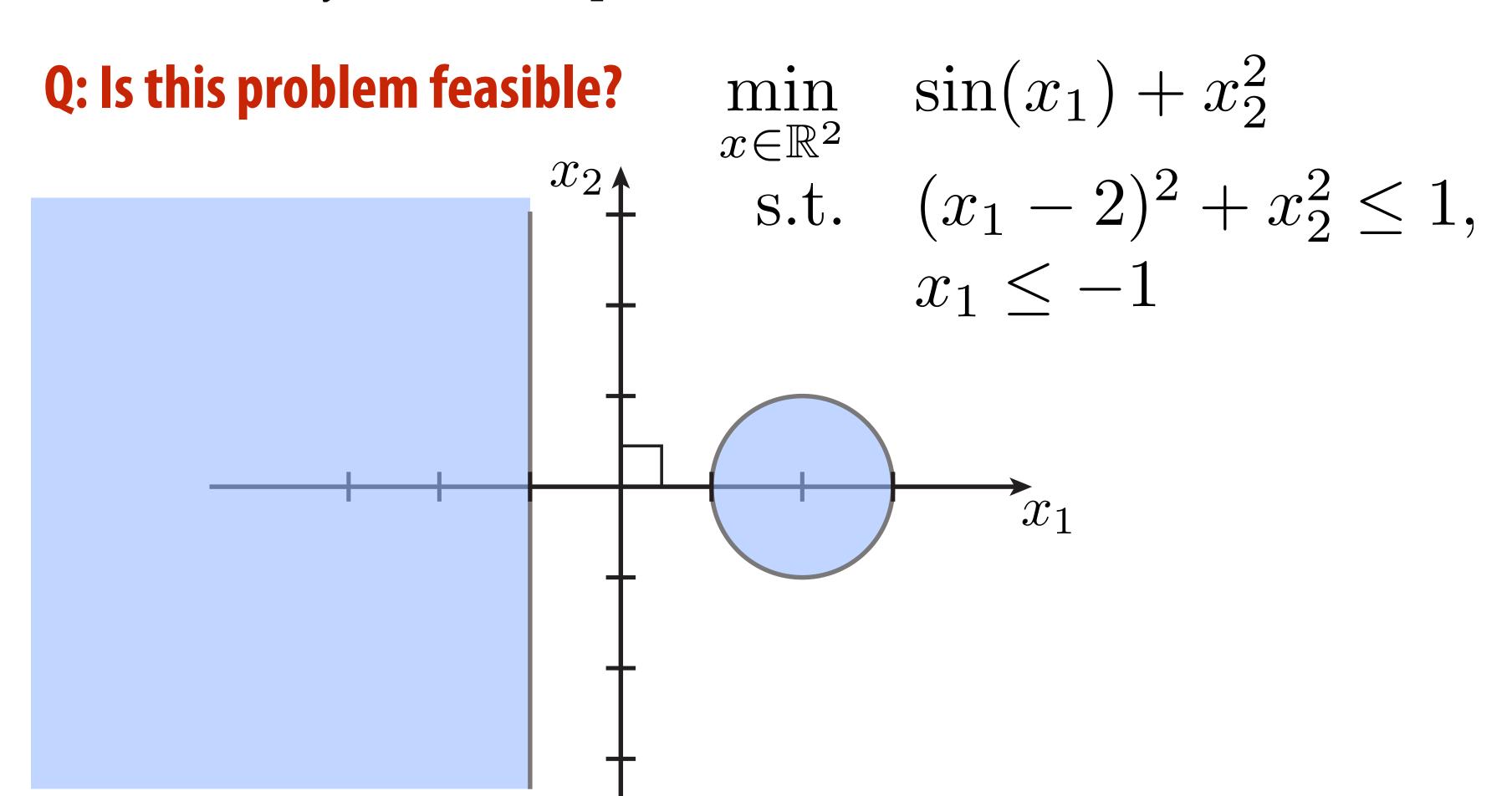
value of objective doesn't depend on x; all feasible solutions are equally good



which can be really hard (or impossible!)

- Not if there aren't any!
- Not all problems have solutions!

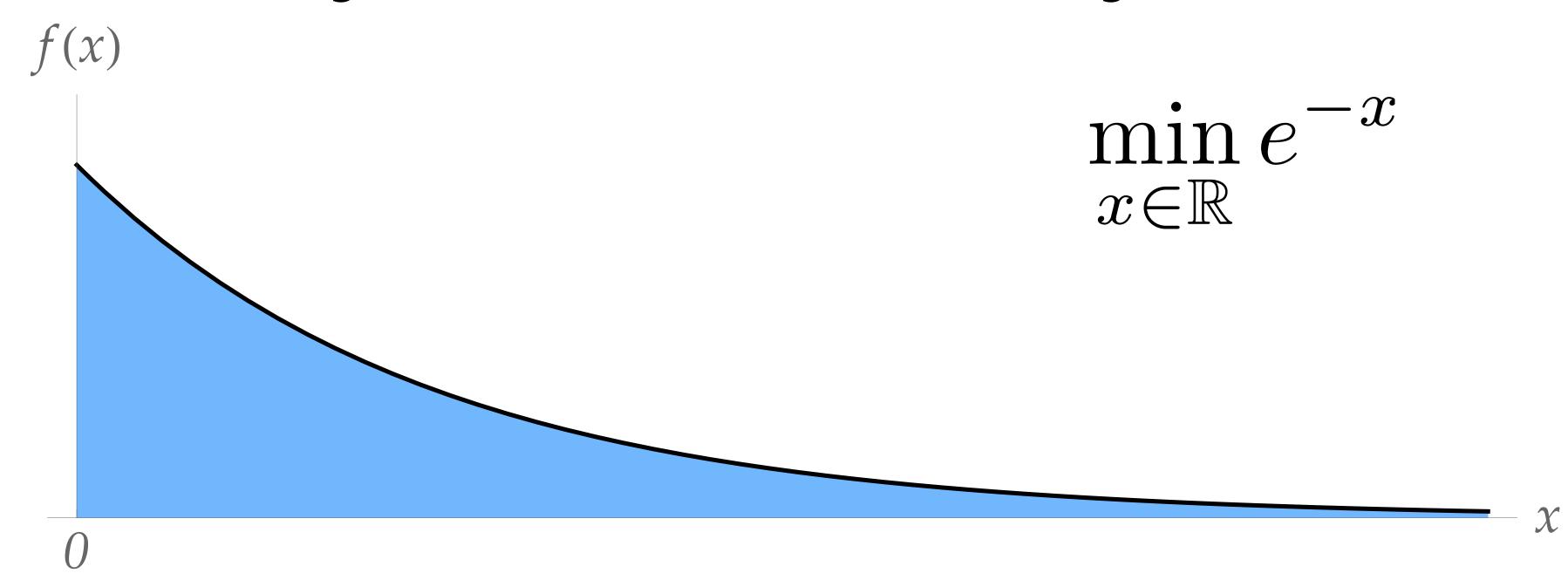
Feasibility - example



A: No—the two sublevel sets (points where $f_i(x) \le 0$) have no common points, i.e., they do not overlap.

Existence and uniqueness of minimizers, cont.

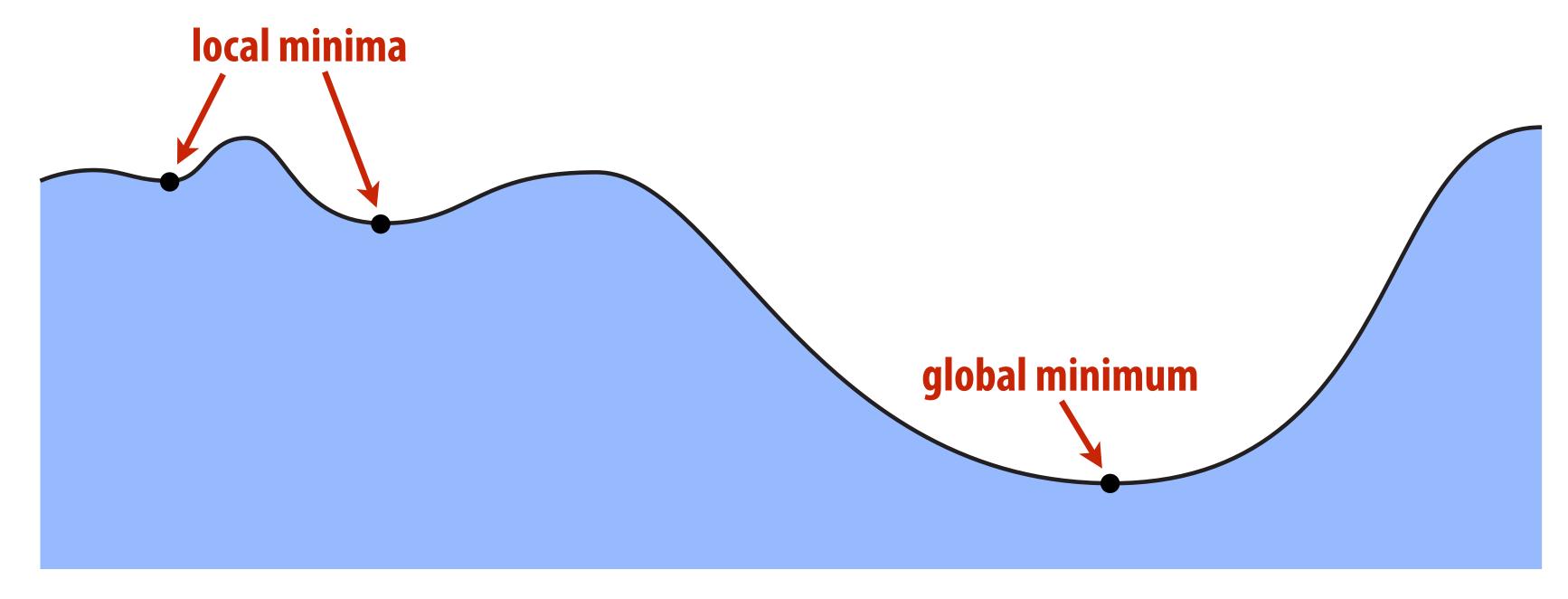
Even being bounded from below is not enough:



No matter how big x is, we never achieve the lower bound (0)

Characterization of minimizers

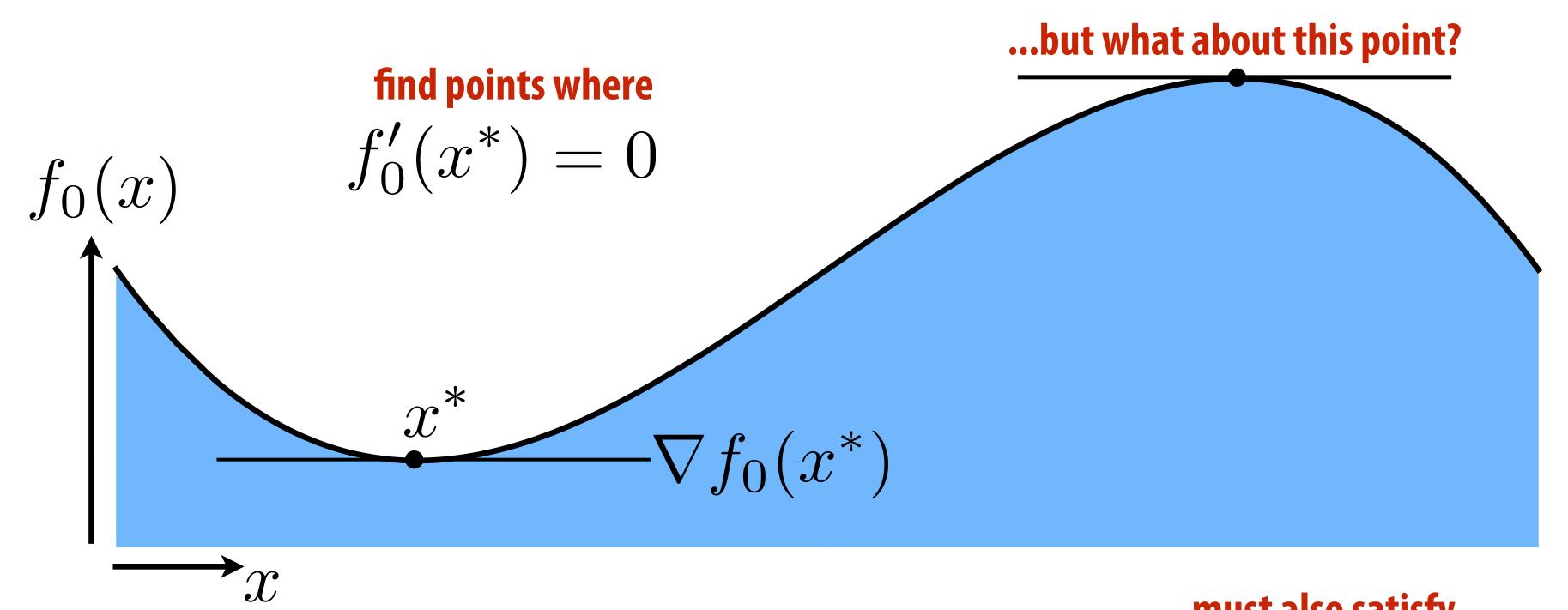
- Ok, so we have some sense of when a minimizer might exist
- But how do we know a given point x is a minimizer?



- Checking if a point is a global minimizer is (generally) hard
- But we can certainly test if a point is a local minimum (ideas?)
- (Note: a global minimum is also a local minimum!)

Characterization of local minima

- Consider an objective f_0 : $R \rightarrow R$. How do you find a minimum?
- (Hint: you may have memorized this formula in high school!)



Also need to check second derivative (how?)

must also satisfy
$$f_0''(x^*) \ge 0$$

- Make sure it's positive
- But what does this all mean for more general functions f_0 ?

Optimality conditions (unconstrained)

- In general, our objective is $f_0: \mathbb{R}^n \to \mathbb{R}$
- How do we test for a local minimum?
- 1st derivative becomes *gradient*; 2nd derivative becomes *Hessian*

$$\nabla f := \begin{bmatrix} \partial f/\partial x_1 \\ \vdots \\ \partial f/\partial x_n \end{bmatrix} \qquad \nabla^2 f := \begin{bmatrix} \frac{\partial^2 f}{\partial x_1^2} & \frac{\partial^2 f}{\partial x_1 \partial x_2} & \cdots & \frac{\partial f}{\partial x_1 \partial x_n} \\ \frac{\partial^2 f}{\partial x_2 \partial x_1} & \frac{\partial^2 f}{\partial x_2^2} & \cdots & \frac{\partial f}{\partial x_2 \partial x_n} \\ \vdots & \vdots & \ddots & \vdots \\ \frac{\partial^2 f}{\partial x_n \partial x_1} & \frac{\partial^2 f}{\partial x_n \partial x_2} & \cdots & \frac{\partial f}{\partial x_n^2} \end{bmatrix}$$
(measures "slope")

HESSIAN (measures "curvature")

Optimality conditions?

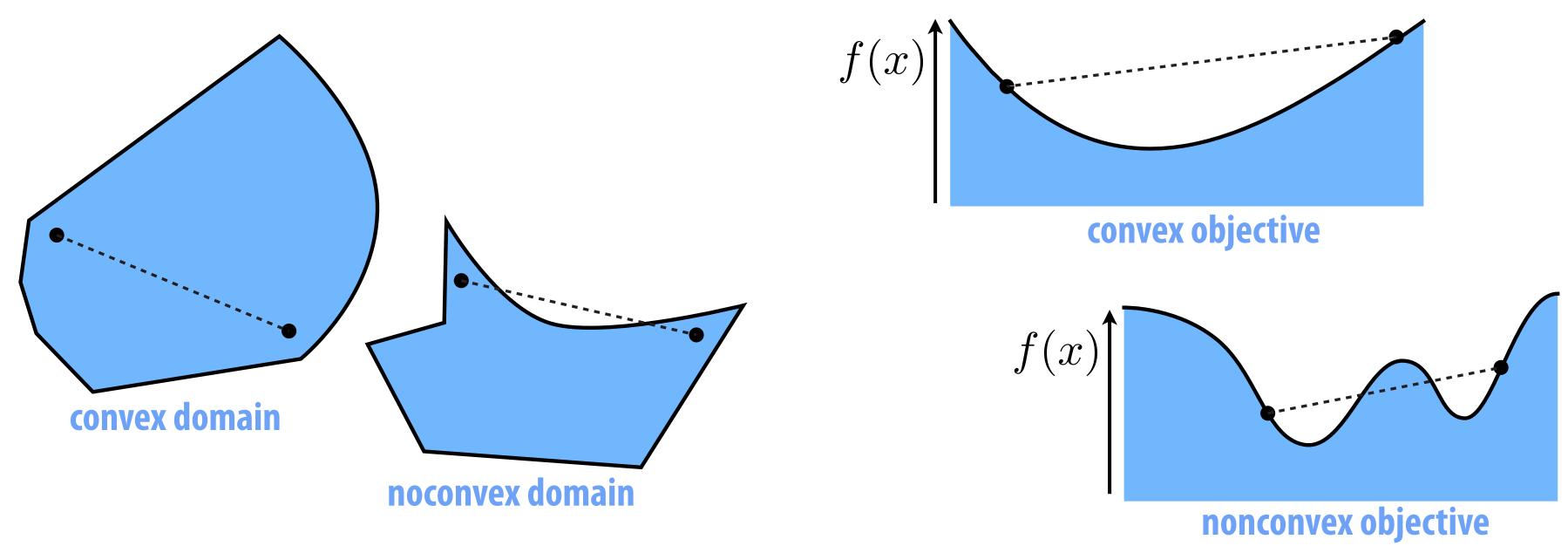
$$\nabla f_0(x^*) = 0$$
1st order

positive semidefinite (PSD)
$$\nabla^2 f_0(x^*) \succeq 0$$
 2nd order

Stanford CS248, Winter 2021

Convex optimization

- Special class of problems that are almost always "easy" to solve (polynomial-time!)
- Problem is convex if it has a convex domain and convex objective



- Why care about convex problems in graphics?
 - can make guarantees about solution (always the best)
 - doesn't depend on initialization (strong convexity)
 - often efficient to solve

Sadly, life is not usually that easy. How do we solve optimization problems in general?

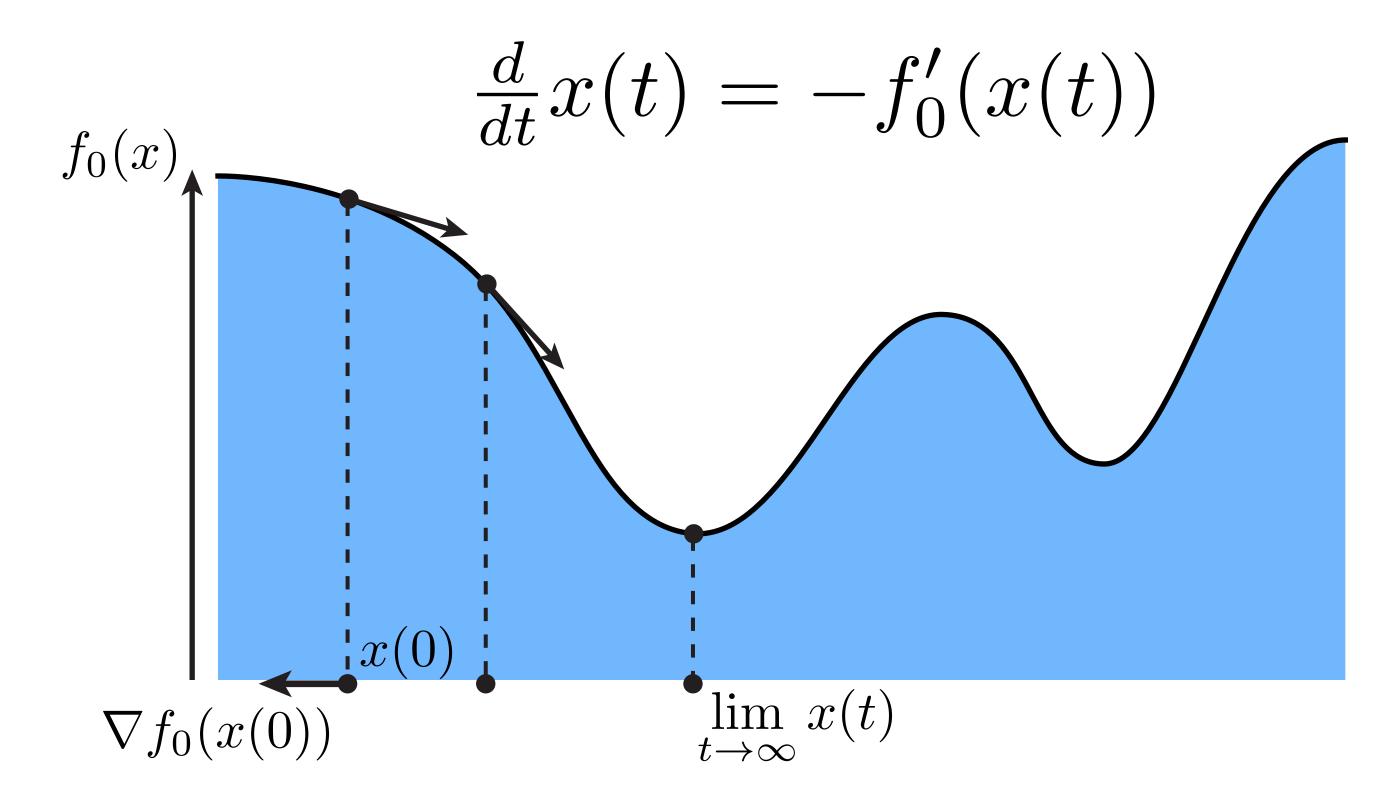
Descent methods

An idea as old as the hills:



Gradient descent (1D)

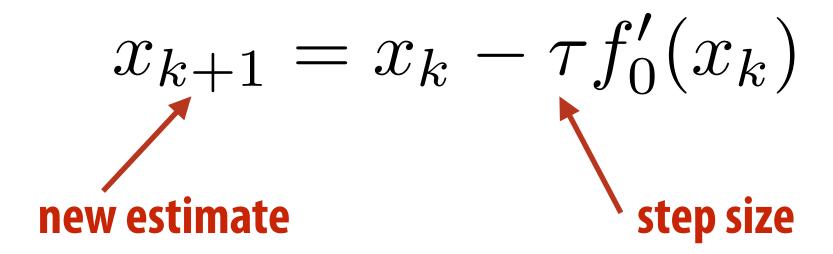
- Basic idea: follow the gradient "downhill" until it's zero
- (Zero gradient was our 1st-order optimality condition)



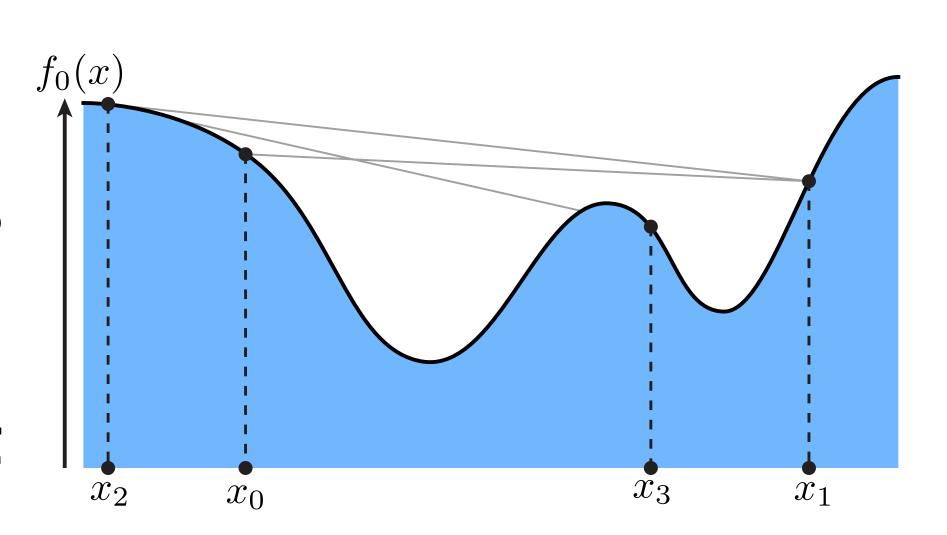
- Do we always end up at a (global) minimum?
- How do we compute gradient descent in practice?

Gradient descent algorithm (1D)

"Walk downhill"



- Q: How do we pick the step size?
- If we're not careful, we'll go zipping all over the place; won't make any progress.



- Basic idea: use "step control" to determine step size based on value of objective and derivatives
- For now we will do something simple: make τ small!

Gradient descent algorithm (n-D)

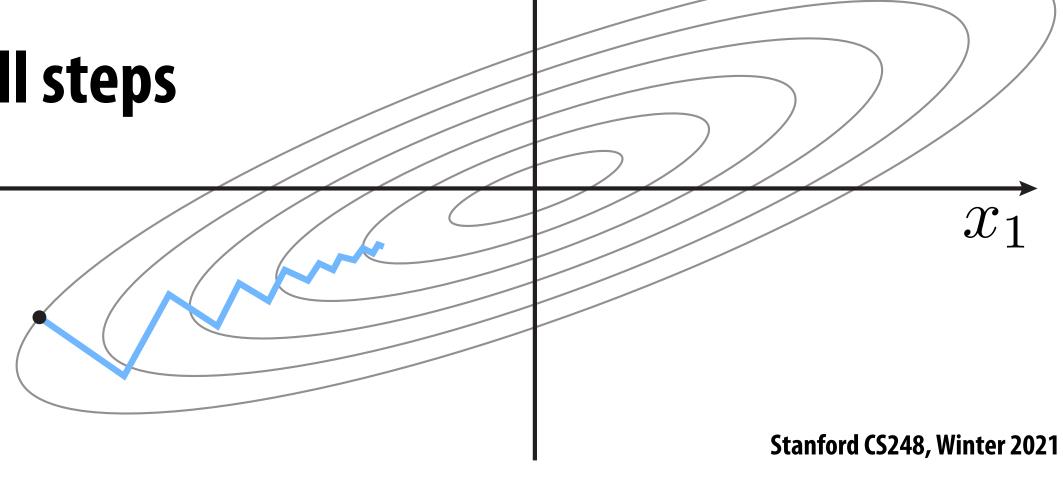
Q: How do we write gradient descent equation in general?

$$\frac{d}{dt}x(t) = -\nabla f_0(x(t))$$

Q: What's the corresponding discrete update?

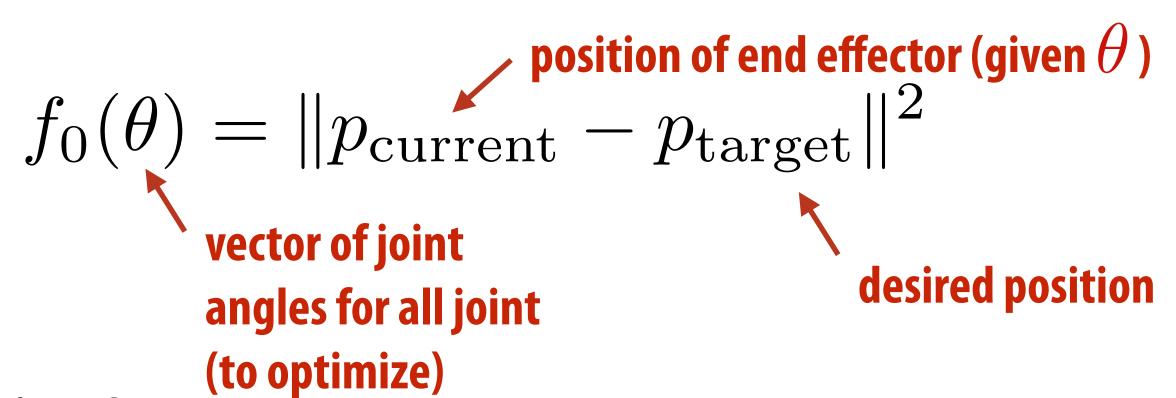
$$x_{k+1} = x_k - \tau \nabla f_0(x_k)$$

- Basic challenge in nD:
 - solution can "oscillate"
 - takes many, many small steps
 - very slow to converge



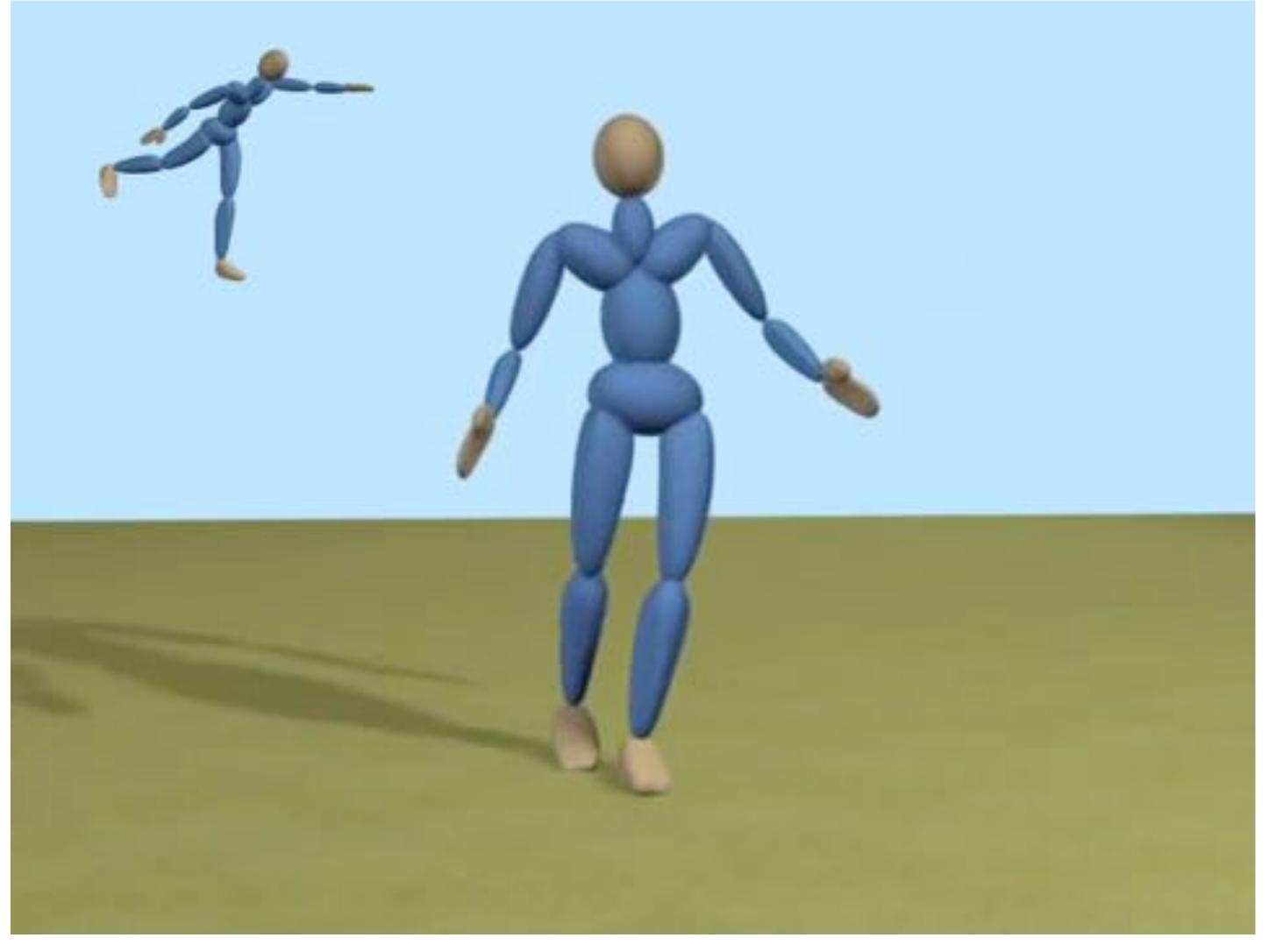
Simple inverse kinematics algorithm

- What is the objective?
 - Distance from end effector position (given current joint parameters) to target position.



- Constraints?
 - Could limit range of motion of a joint
- How to optimize for joint angles:
 - Compute gradient of objective with respect to joint angles
 - Apply gradient descent

Many uses of optimization in animation (and graphics in general)



Sumit Jain, Yuting Ye, and C. Karen Liu, "Optimization-based Interactive Motion Synthesis"

Summary

- Kinematics: how objects move, without regard to forces that create this movement
- Today: multiple ways of obtaining joint motion
 - Direct hand authoring of joint angles
 - Via measurement (motion capture)
 - As a result of solving for angles that yield a particular higher level result (inverse kinematics)

Acknowledgements: thanks to Keenan Crane, Ren Ng, Mark Pauly, Steve Marschner, Tom Funkhouser, James O'Brien for presentation resources