Lecture 17:

Color

Computer Graphics: Rendering, Geometry, and Image Manipulation
Stanford CS248A, Winter 2025

Color is amazing!

Mission Peak, Bay Area

Meow Wolf, Santa Fe, NM

Image credit: Jabin Botsford/The Washington Post/Getty Images (taken from CNN.com)

A Good Dinner (Redwood City)

Vietnam

Sydney Harbor, Australia

Starry Night, Van Gogh

Marilyn Monroe, Andy Warhol

Why do we need to be able to talk precisely about color?

SAMSUNG
QLED 8K
LG
SONY
VIZIO
SANUS
PREMIUM TV W
SAMSUNG
4K Gaming
The Frame
SAMSUNG
TV when it's on.
Art when it's off.
Art Store

What is color?

- Color is a phenomenon of human perception; it is not a universal property of light
- Colors are the perceptual sensations that arise from seeing light of different spectral power distributions
- As you will learn, different wavelengths of light are not “colors”

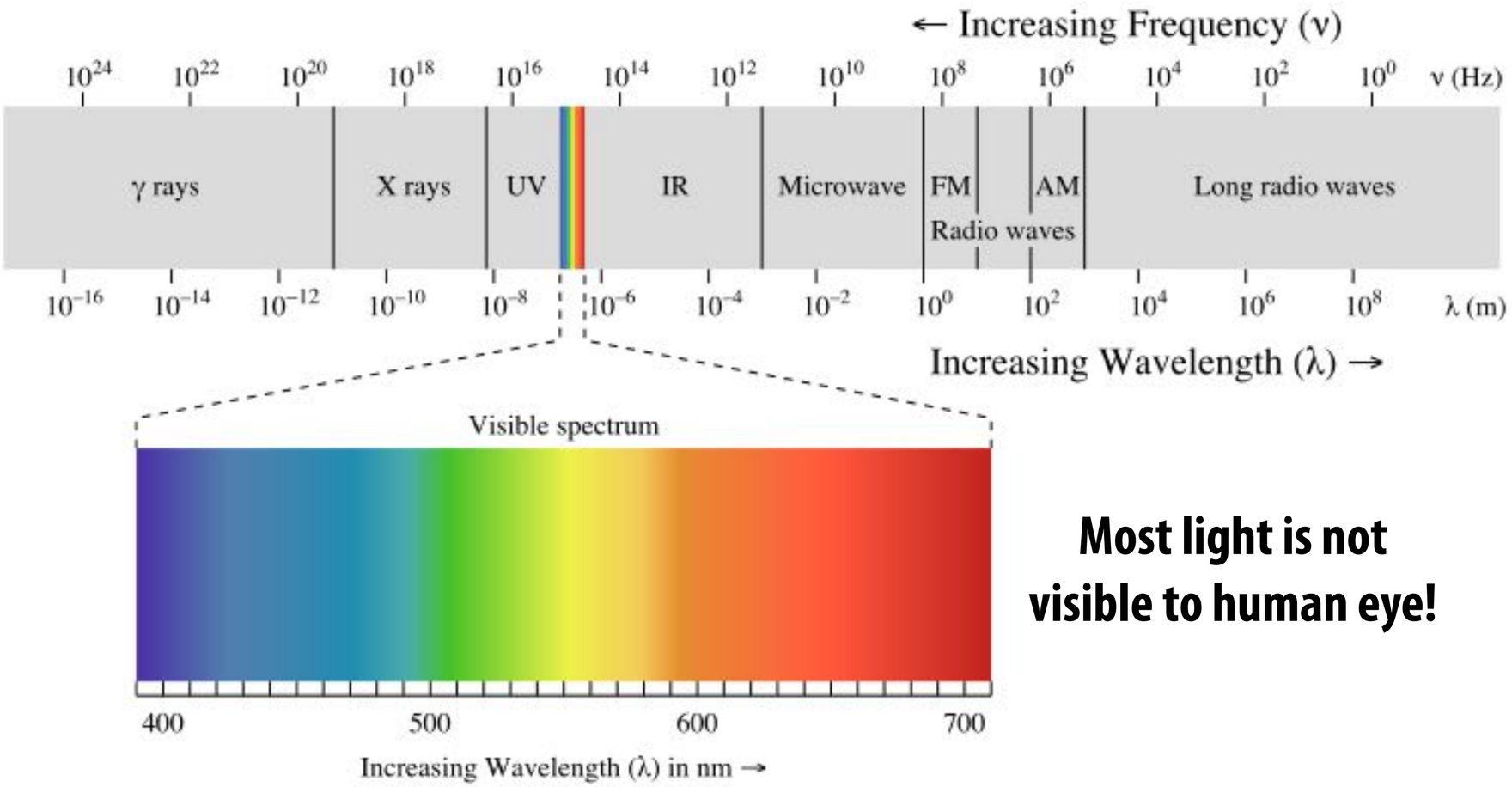
The physical basis of color

(Review: what is light?)

Electromagnetic radiation

Light is electromagnetic radiation (oscillating electromagnetic field)

Perceived color is *related to* frequency of oscillation



Most light is not visible to human eye!

Image credit: Licensed under CC BY-SA 3.0 via Commons
https://commons.wikimedia.org/wiki/File:EM_spectrum.svg#/media/File:EM_spectrum.svg

Spectral power distribution (SPD)

- The amount of light present at each wavelength
- Units:
  - Radiometric units / nanometer (e.g. watts / nm)
  - Can also be unit-less (see below)

- Note: SPD is often visualized in “relative units” scaled to maximum power wavelength when absolute units are not important (the diagrams in this lecture do this)

Spectral power distribution of common light sources

Describes distribution of power (energy/time) by wavelength

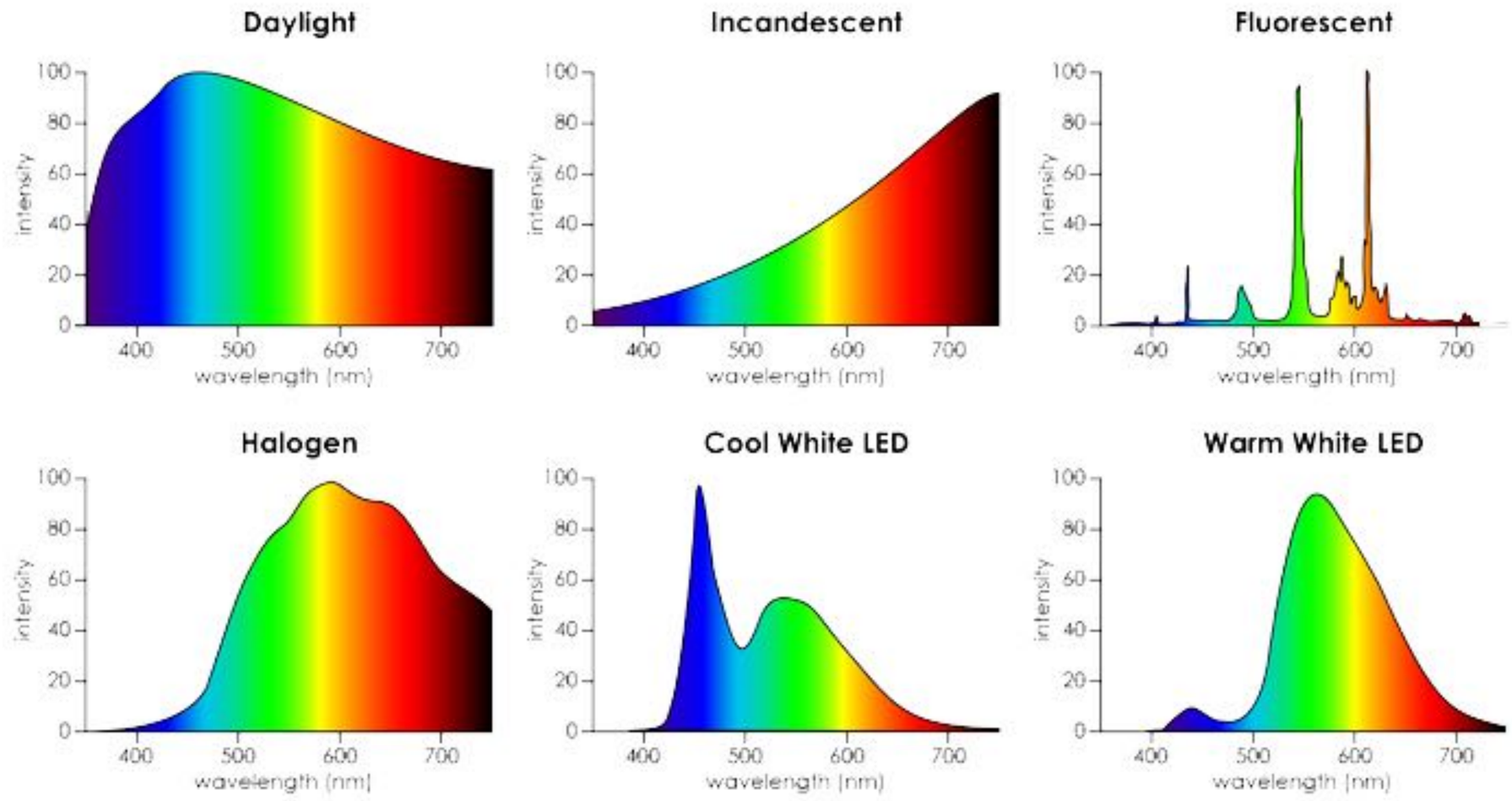
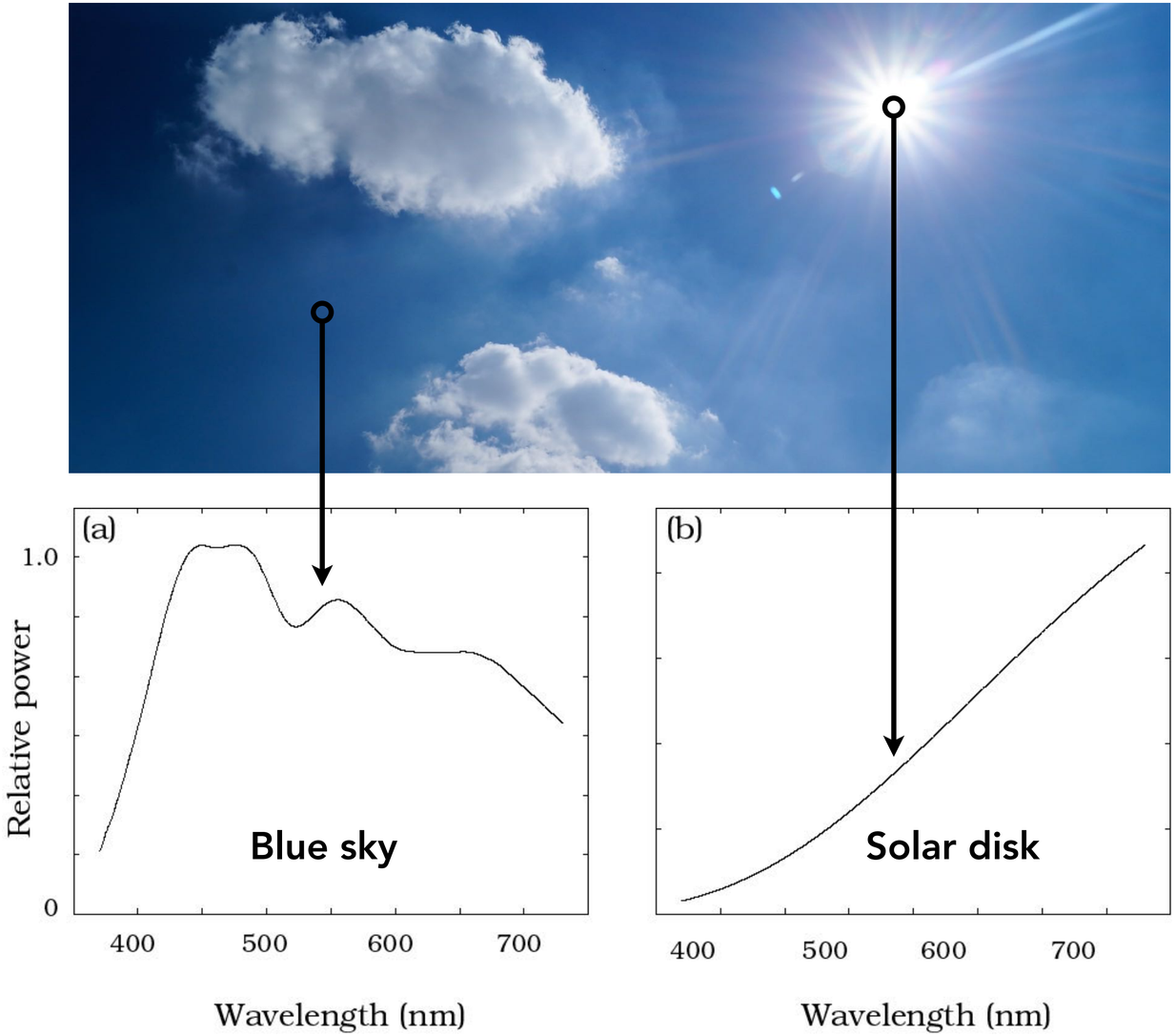


Figure credit:

admesy
ADVANCED MEASUREMENT SYSTEMS

Daylight spectral power distributions vary

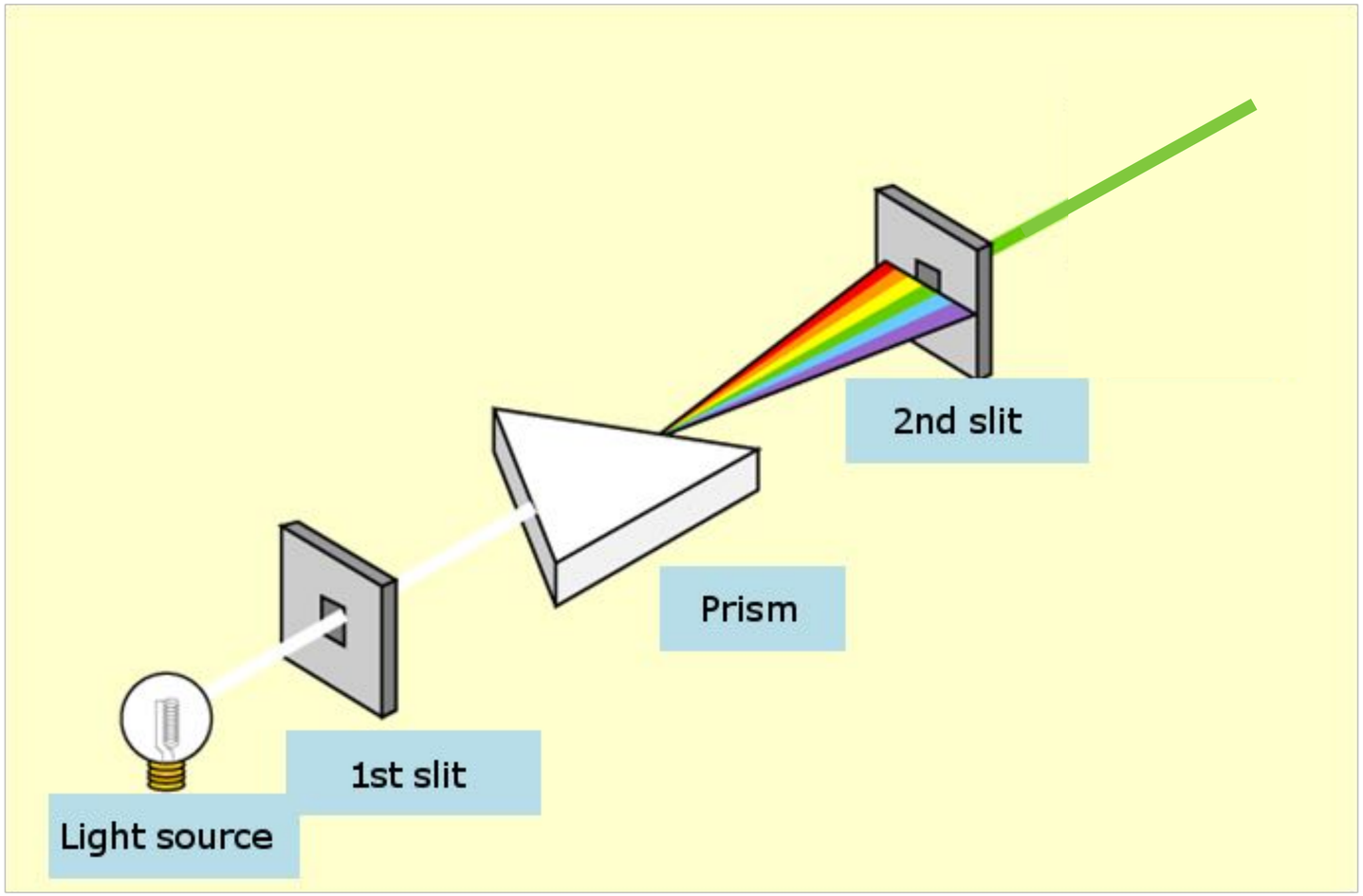


[Brian Wandell]

Measuring the spectral power distribution

credit: Science Media Group.

Monochromator



A monochromator delivers light of a single wavelength from a light source with broad spectrum.
Control which wavelength by angle of prism.

Hegyi et al. "Introduction to Practical Biochemistry"
http://elte.prompt.hu/sites/default/files/tananyagok/IntroductionToPracticalBiochemistry/ch04s07.html

Superposition (linearity) of spectral power distributions

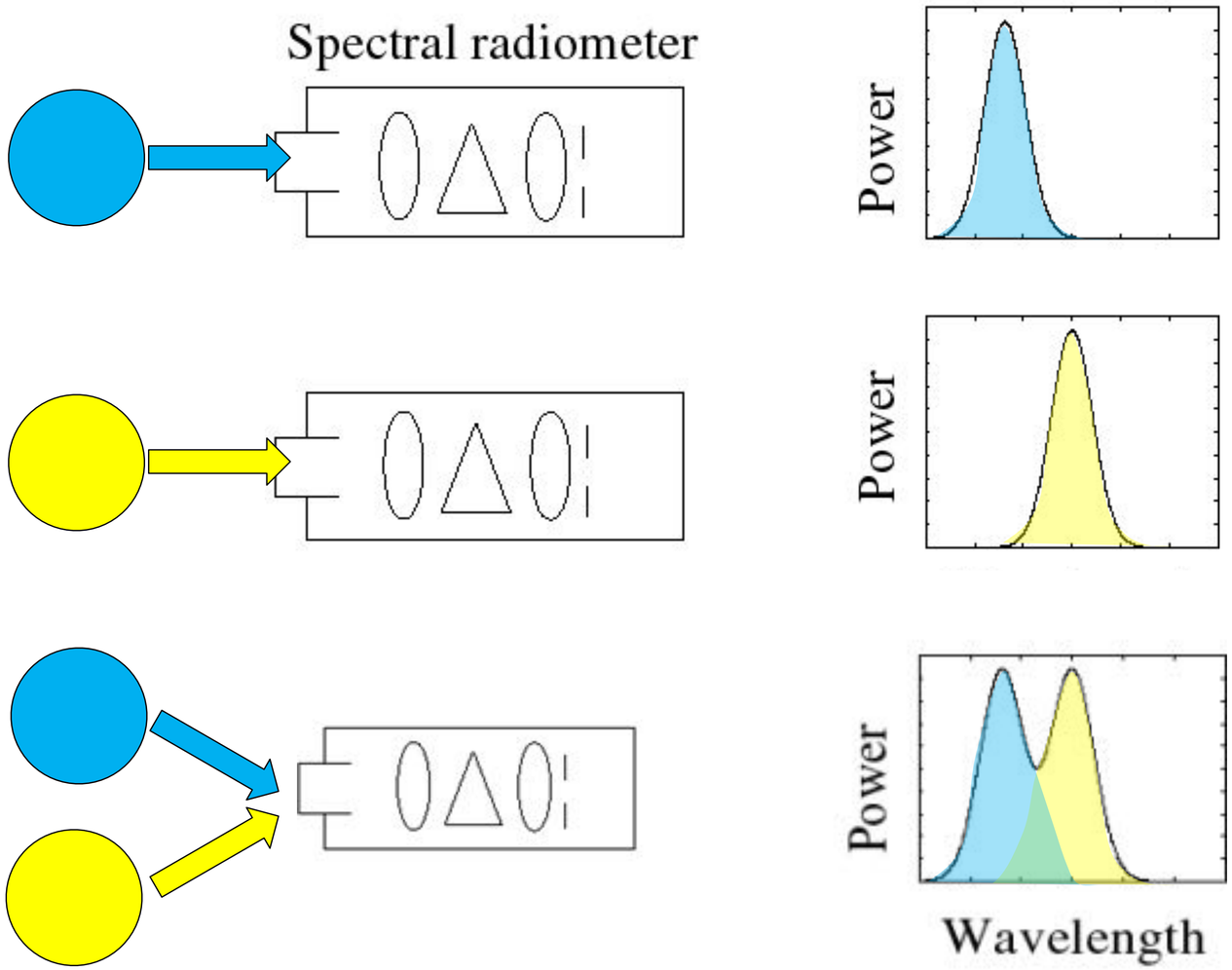
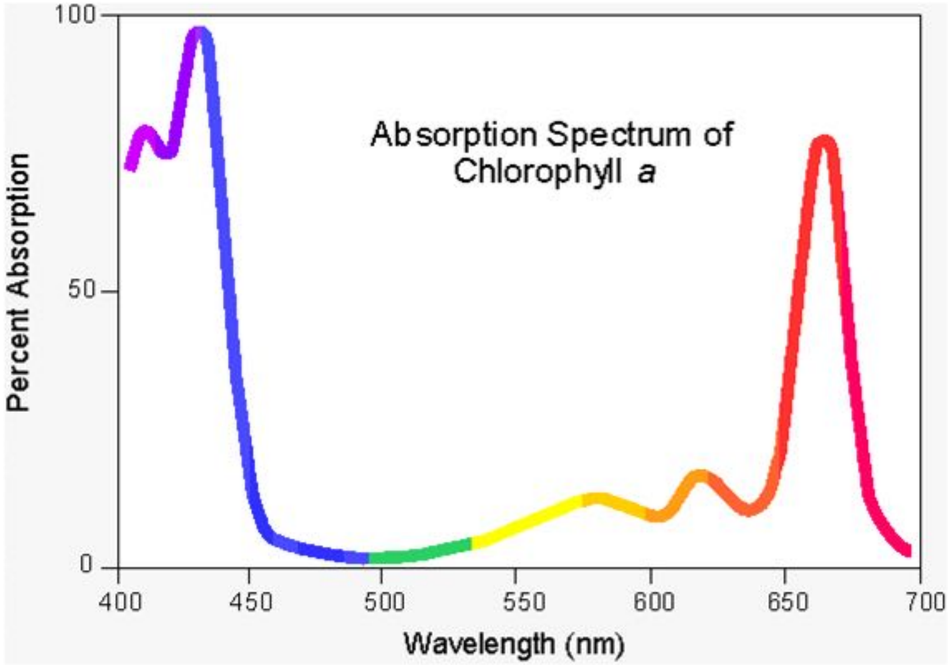


Figure credit: Brian Wandell

Absorption spectrum

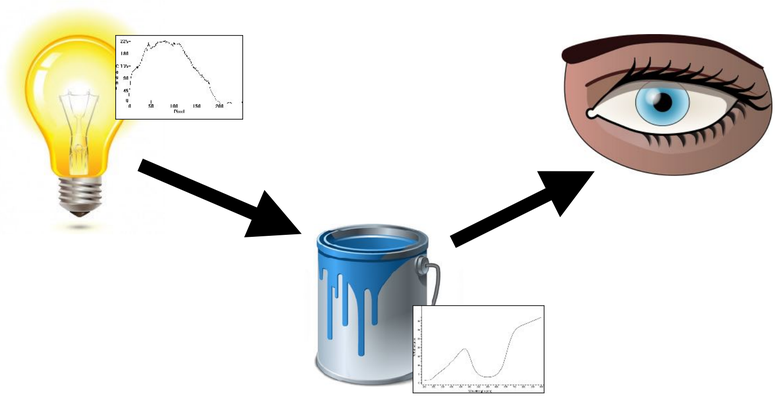
- Emission spectrum is *intensity* as a function of frequency
- Absorption spectrum is *fraction absorbed* as function of frequency



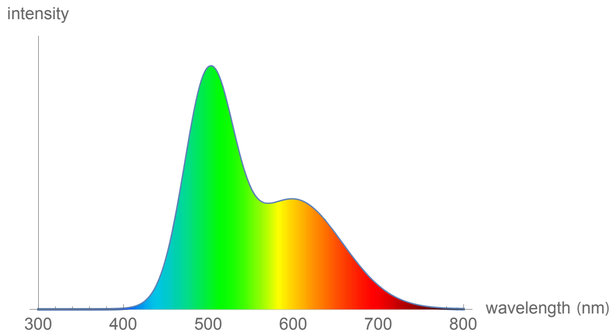
Q: What does an object with this absorption spectrum look like?

Interaction of emission and reflection

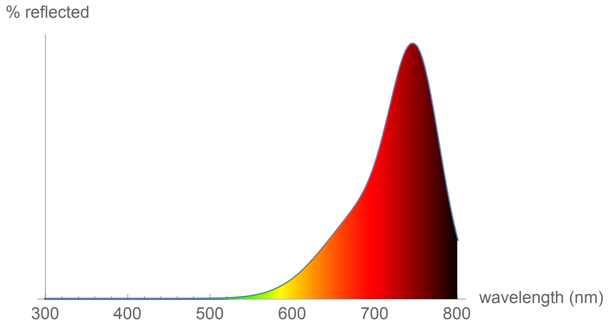
- Consider what happens when light gets reflected from a surface
  - v — frequency of light (Greek "nu")
  - Light source has emission spectrum f(v)
  - Surface has reflection spectrum g(v)
  - Resulting intensity is the *product* f(v)g(v)



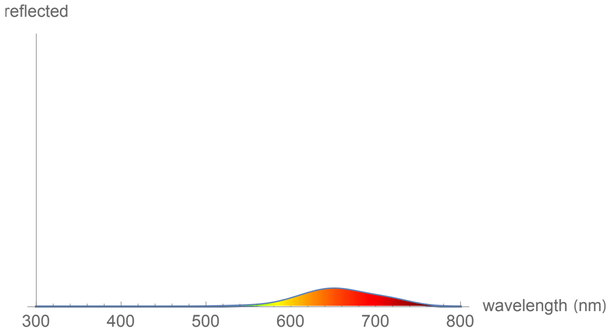
f(v)



g(v)



f(v)g(v)

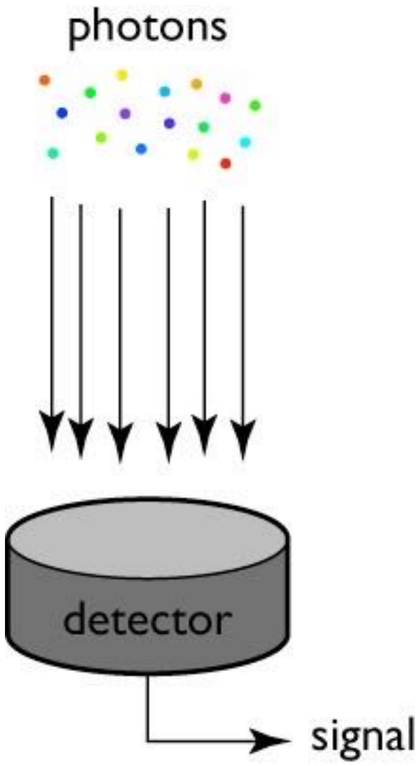


Measuring Light

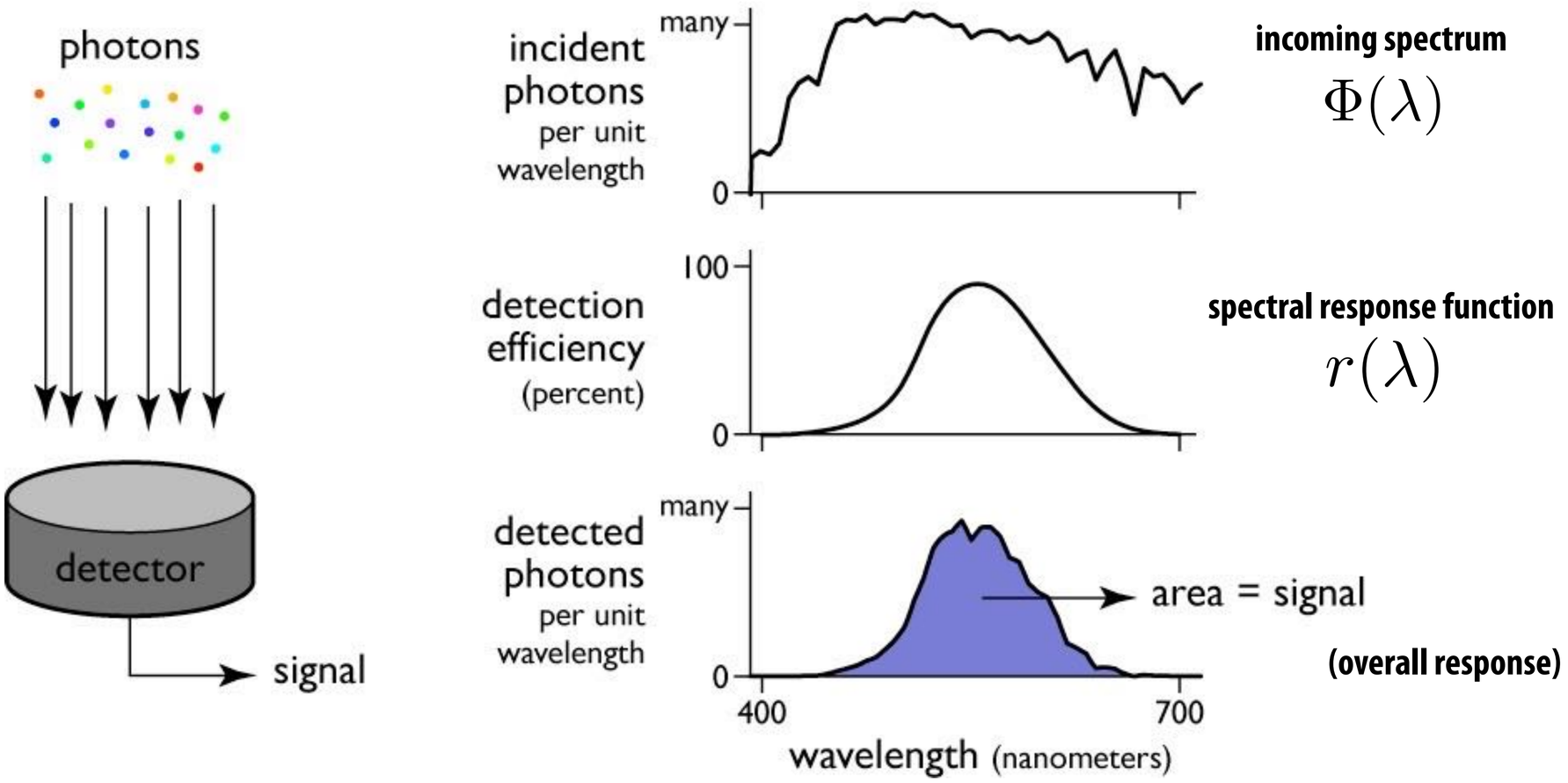
A simple model of a light detector

- Produces a single value (a number) when photons land on it
  - Value depends only on number of photons detected
  - Each photon has a probability of being detected that depends on the wavelength
  - No way to distinguish between signals caused by light of different wavelengths: there is just a number

- This model holds for many detectors:
  - based on semiconductors (e.g., digital cameras)
  - based on visual photopigments (e.g., human eyes)



Simple model of a light detector



$$R = \int_{\lambda} \Phi(\lambda) r(\lambda) d\lambda$$

Figure credit: Steve Marschner

Dimensionality reduction from ∞ to 1

- At the detector:
  - SPD is a function of wavelength (∞ - dimensional signal)
  - Detector output is a scalar value (1 - dimensional signal)

Biological basis of color

The eye

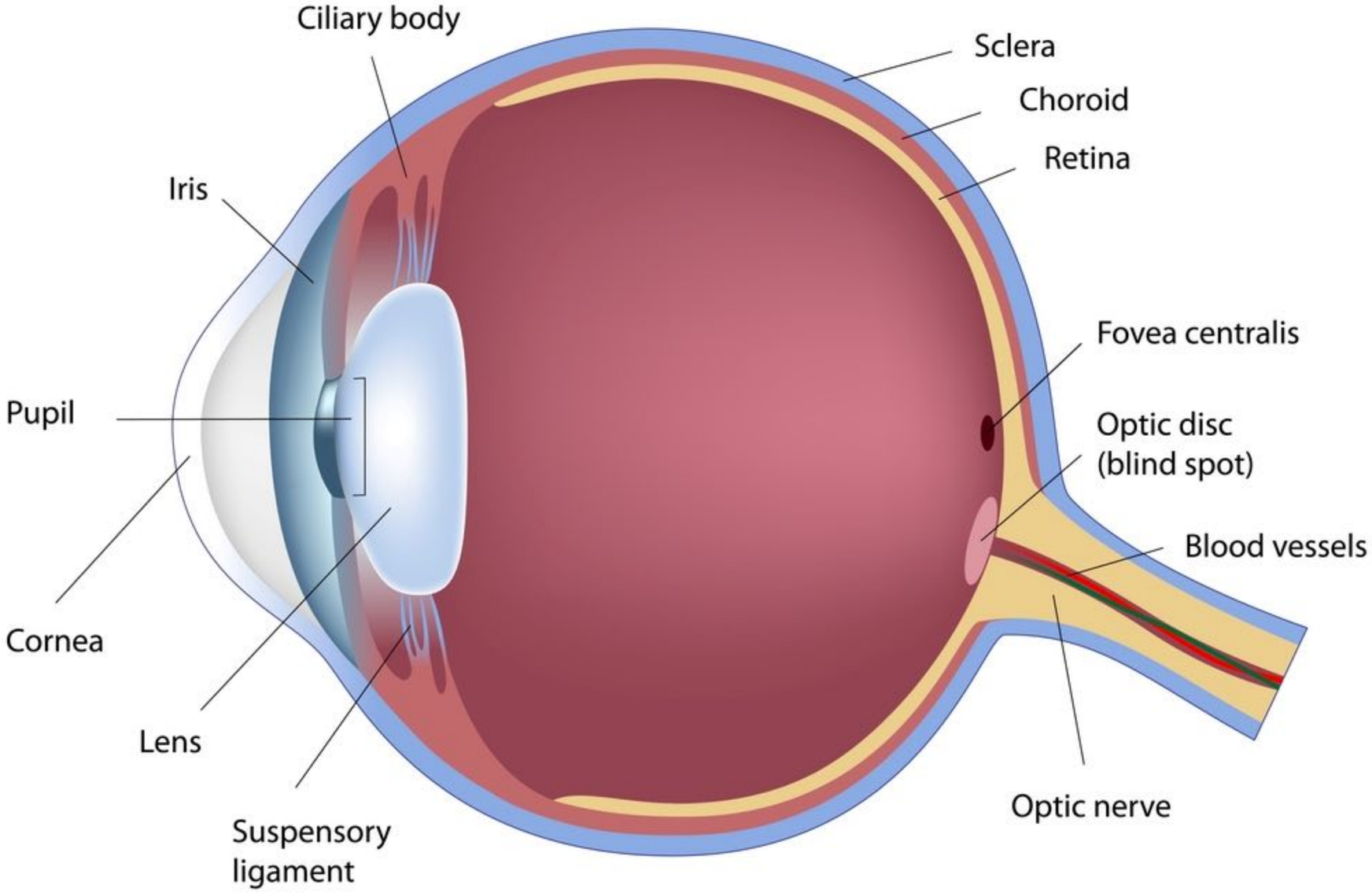


Image credit: Georgia Retina (http://www.garetina.com/about-the-eye)

The eye's photoreceptor cells: rods and cones

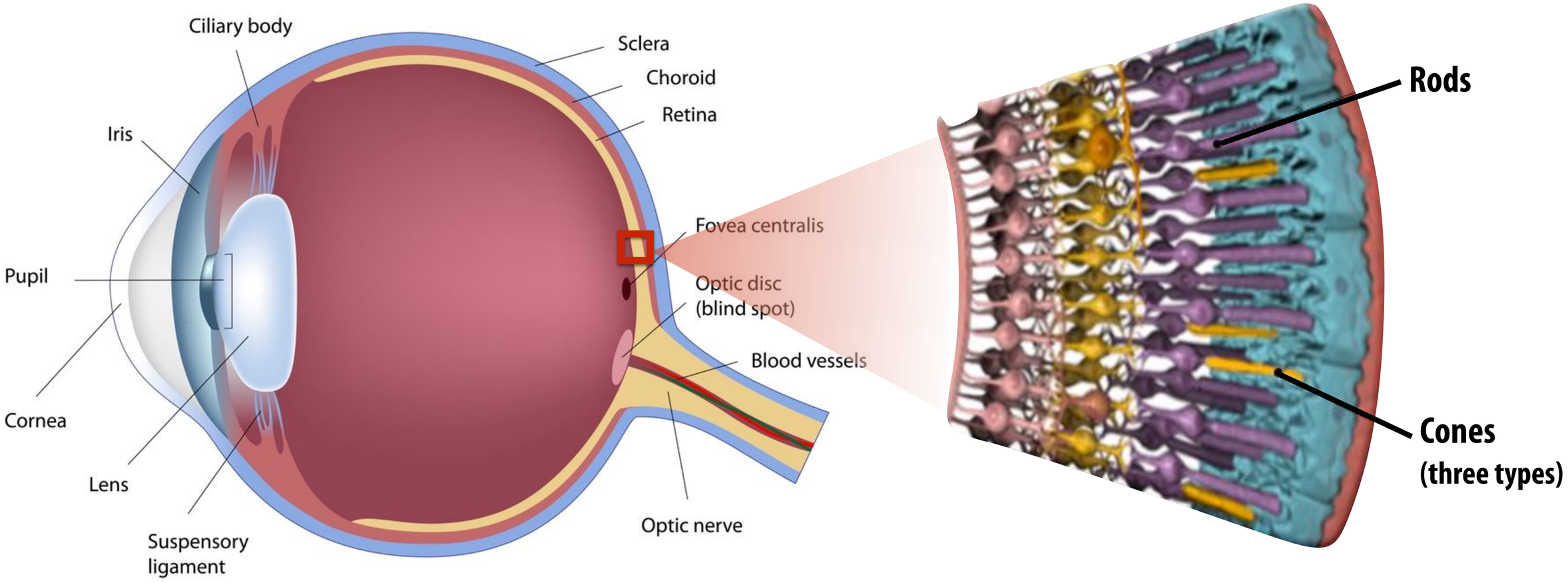


Image credit: http://colorvisionawareness.com/images/pages/eyeDiagram_rodsCones.png

The eye's photoreceptor cells: rods and cones

- Rods are primary receptors under dark viewing conditions (scotopic conditions)
  - Approx. 120 million rods in human eye
  - Sense light intensity (shades of gray, not color)

- Cones are primary receptors under high-light viewing conditions (photopic conditions, e.g., daylight)
  - Approx. 6-7 million cones in the human eye
  - There are three types of cones
  - Each of the three types of cone feature a different "spectral response". This will be critical to color vision (more on this soon…)

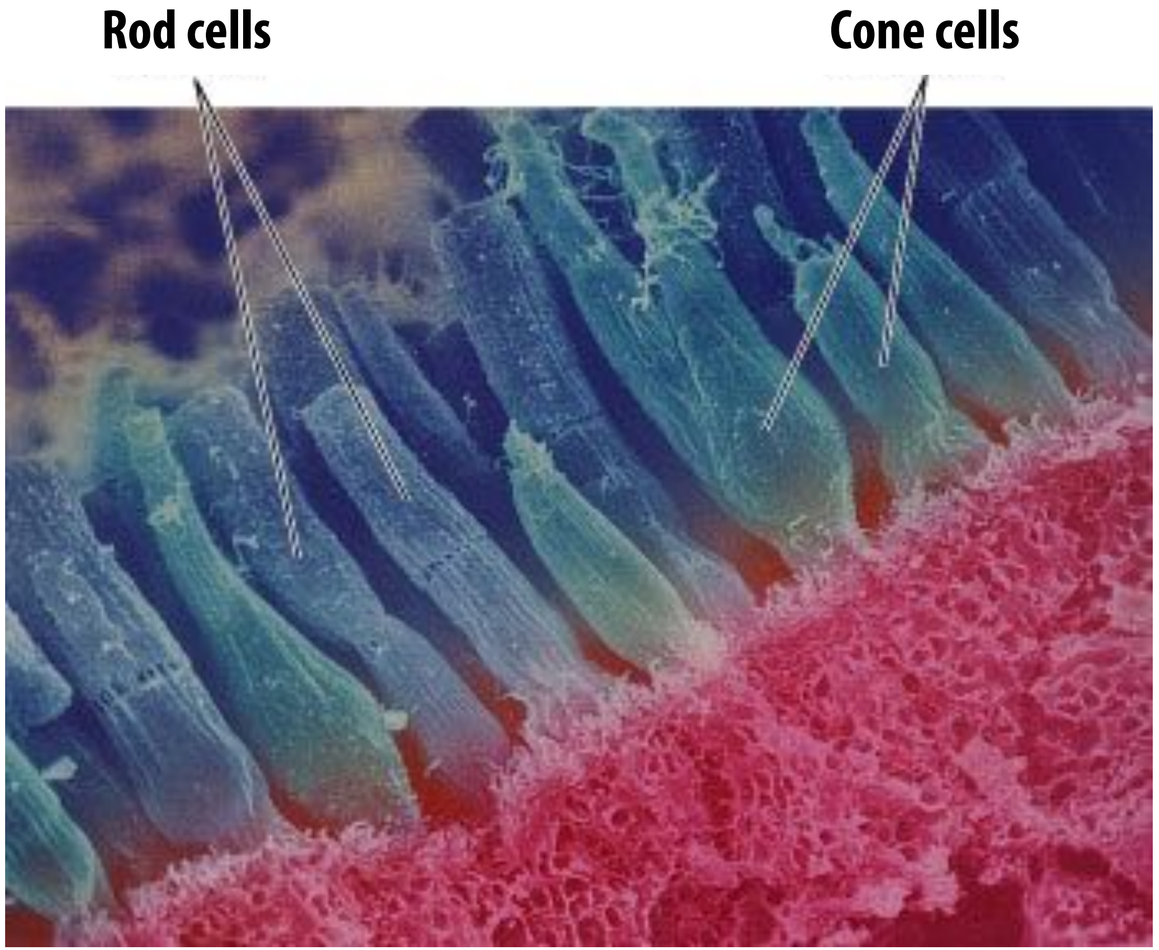
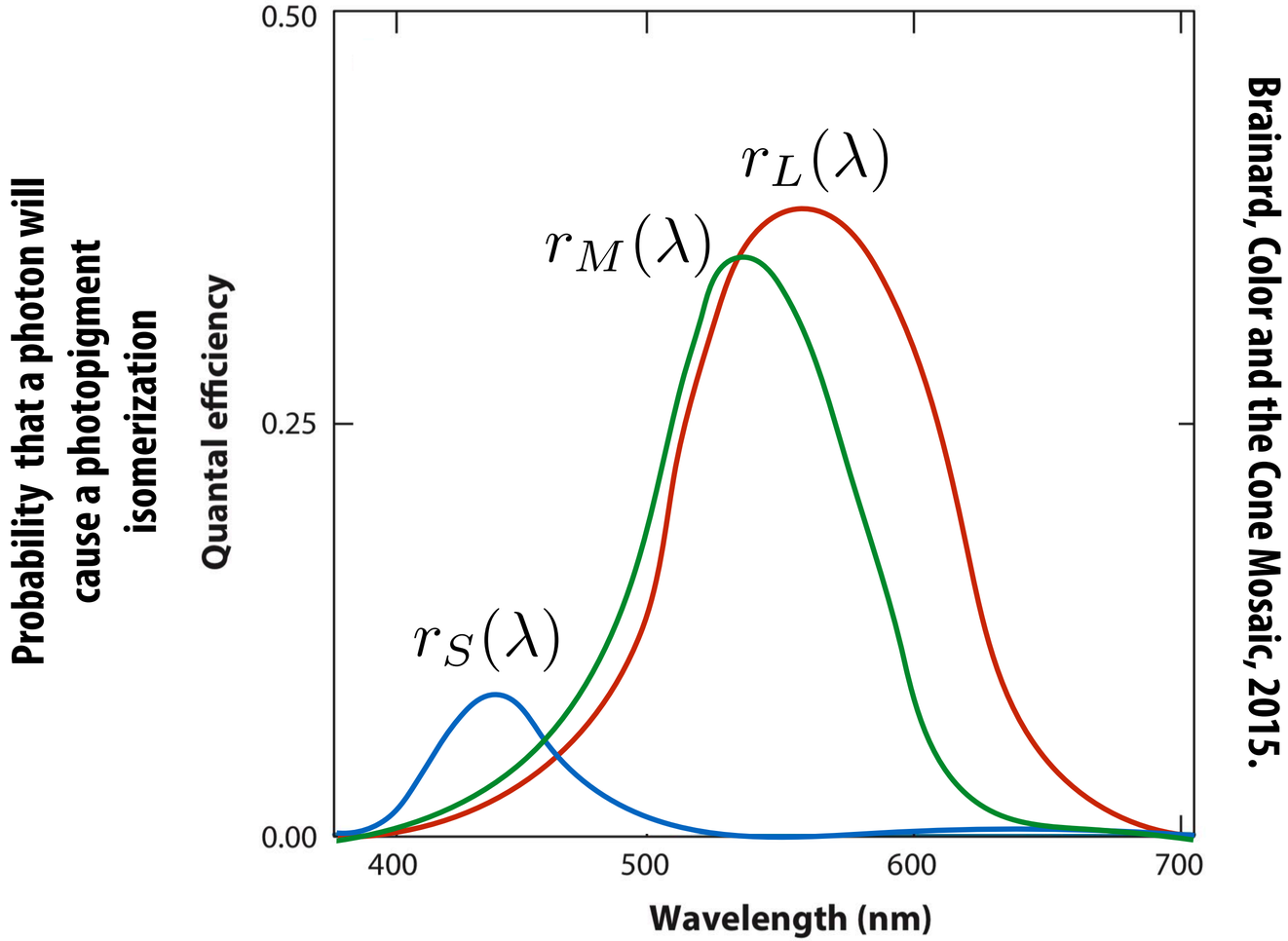


Figure credit: http://ebooks.bfwpub.com/life.php Figure 45.18

Human retinal cone cell response functions (L, M, S types)

Three types of cone cells: S, M, and L

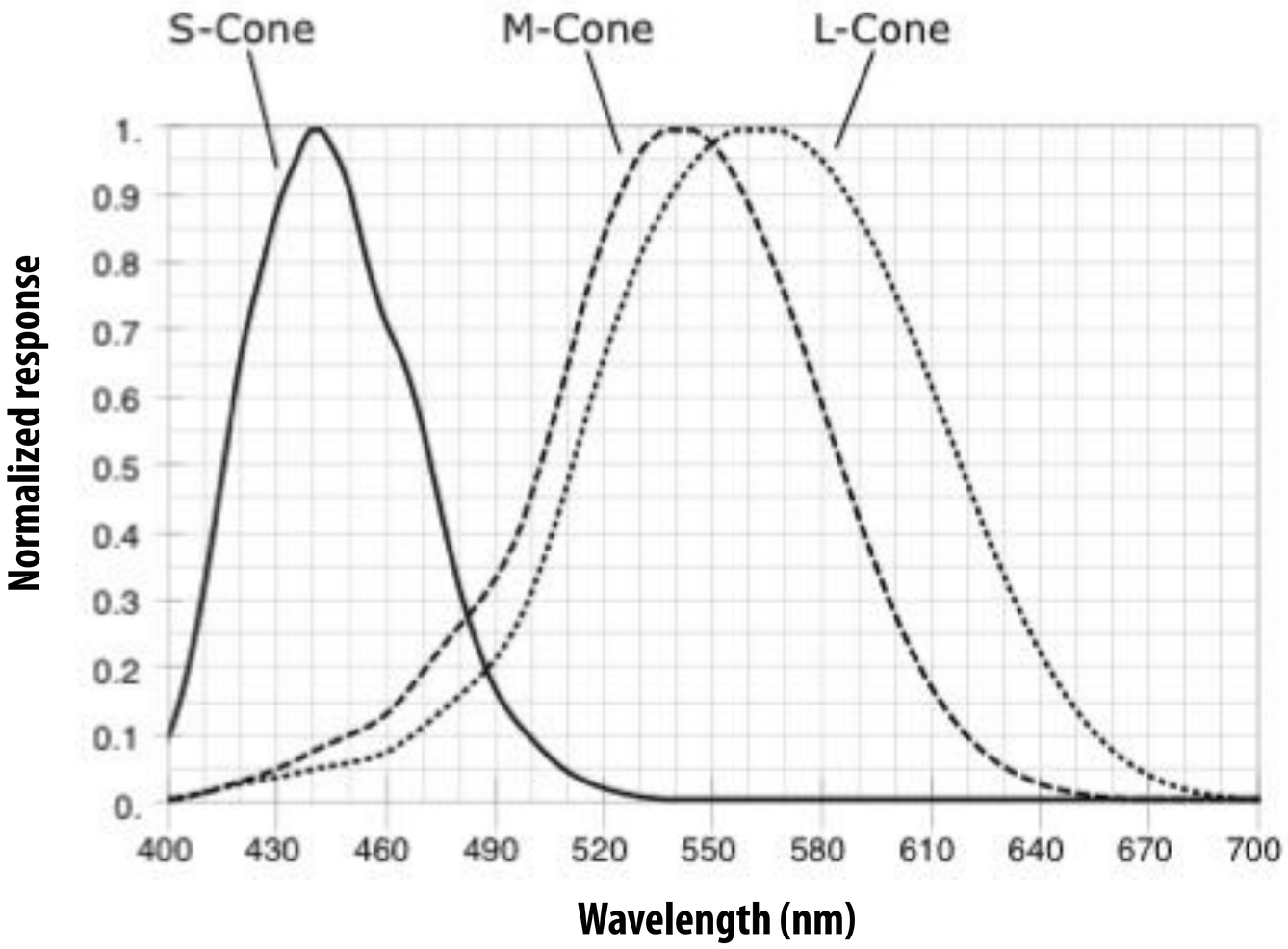
(corresponding to peak response at short, medium, and long wavelengths)



Brainard, Color and the Cone Mosaic, 2015.

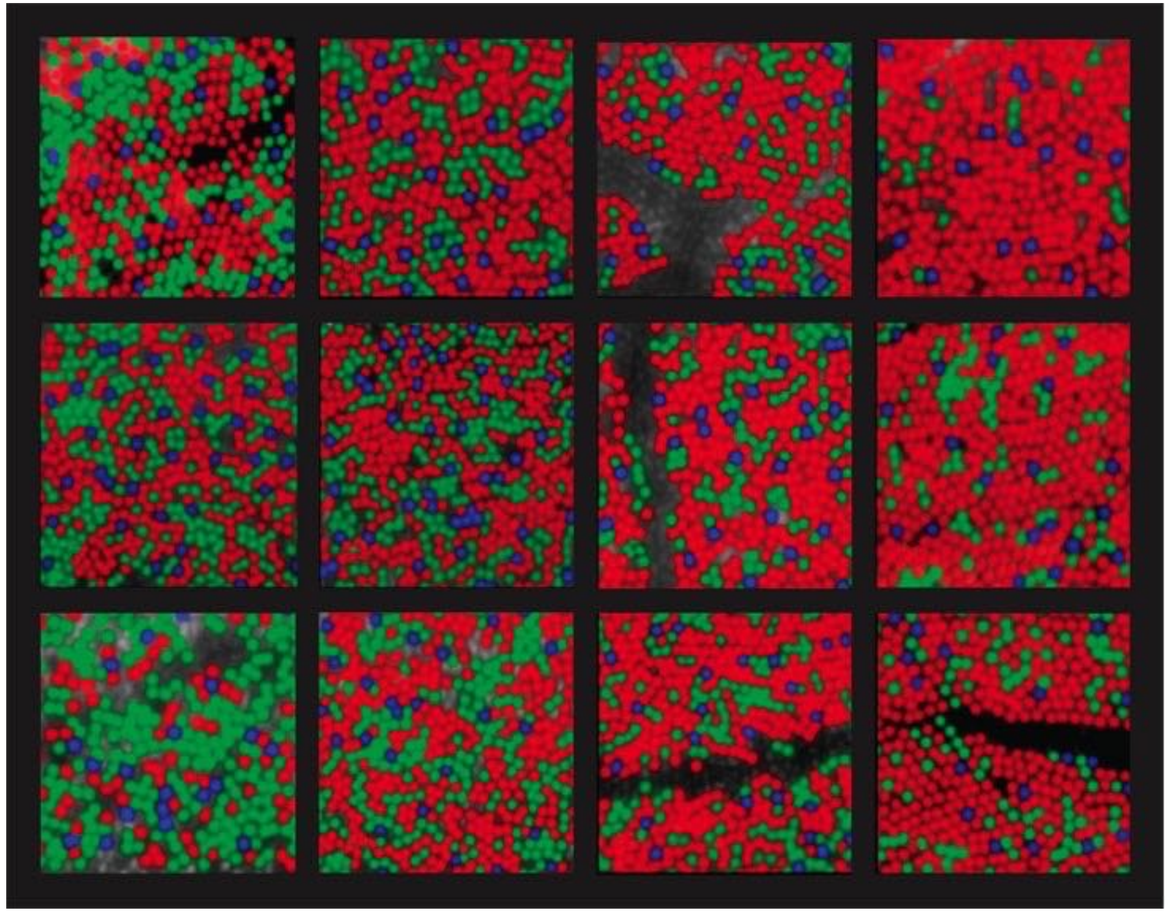
Human retinal cone cell normalized response functions (L, M, S types)

Three types of cone cells: S, M, and L
(corresponding to peak response at short, medium, and long wavelengths)



Fraction of three cone cell types varies widely from human to human

Hofer, H. et al. J. Neurosci. 2005;25:9669-9679



© 2007 Thomson Higher Education

Distribution of cone cells at edge of fovea in 12 different humans with normal color vision.
Note high variability of percentage of different cone cell types. (false color image)

Spectral response of cones

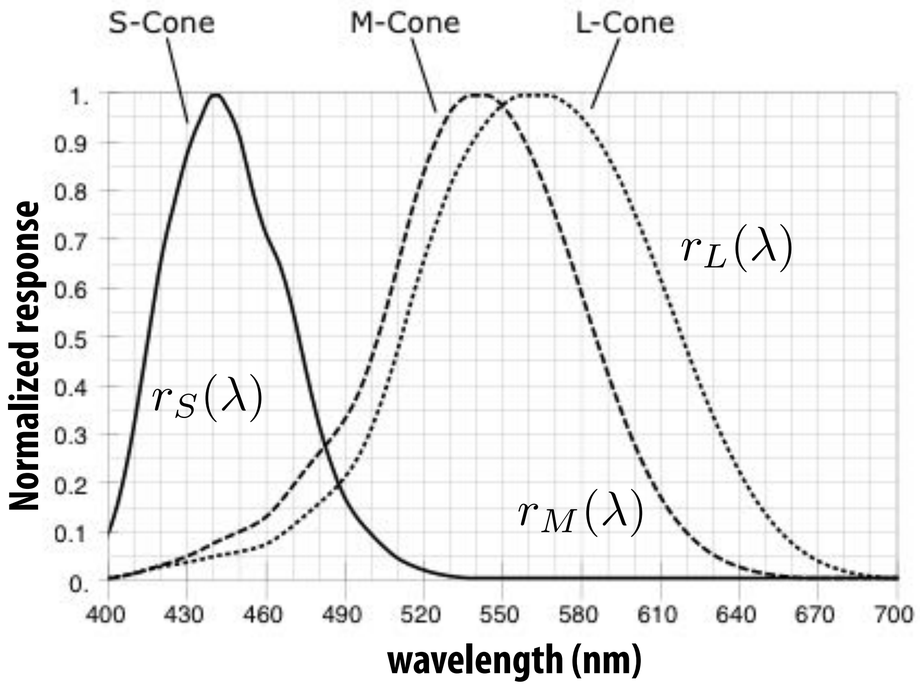
Three types of cones: S, M, and L cones
(corresponding to peak response at short, medium, and long wavelengths)

$$S = \int_\lambda \Phi(\lambda) r_S(\lambda) d\lambda$$

$$M = \int_\lambda \Phi(\lambda) r_M(\lambda) d\lambda$$

$$L = \int_\lambda \Phi(\lambda) r_L(\lambda) d\lambda$$

Response functions for S, M, and L cones



In other words:
Your eye measures three values: S, M, L

LMS responses plotted as 3D color space

- Visualization of "spectral locus" of human cone cells' response to monochromatic light (light with energy in a single wavelength) as points in 3D space.

- This is a plot of the S, M, L response functions as a point in 3D space.

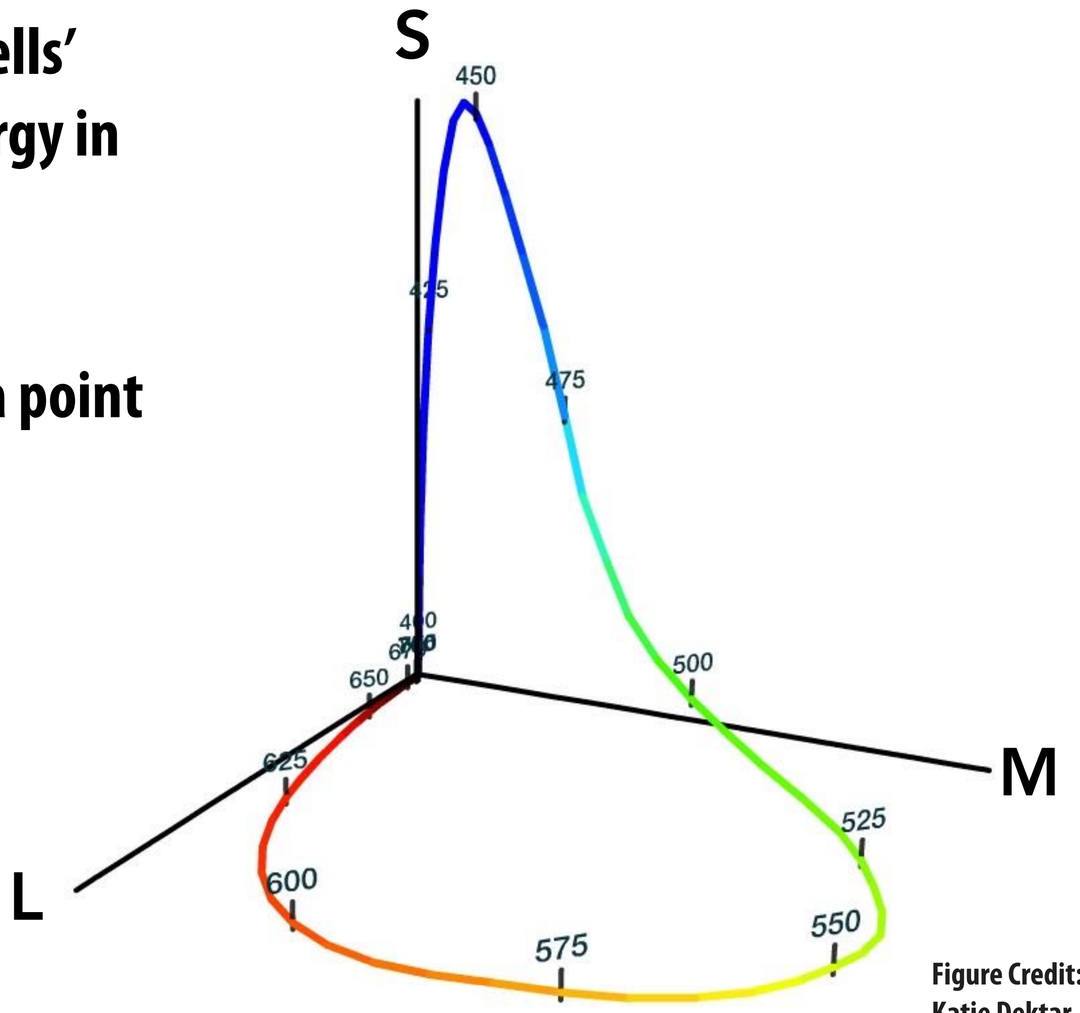


Figure Credit:
Katie Dektar

Spectral response of cones (discrete form)

Three types of cones: S, M, and L cones (corresponding to peak response at short, medium, and long wavelengths)

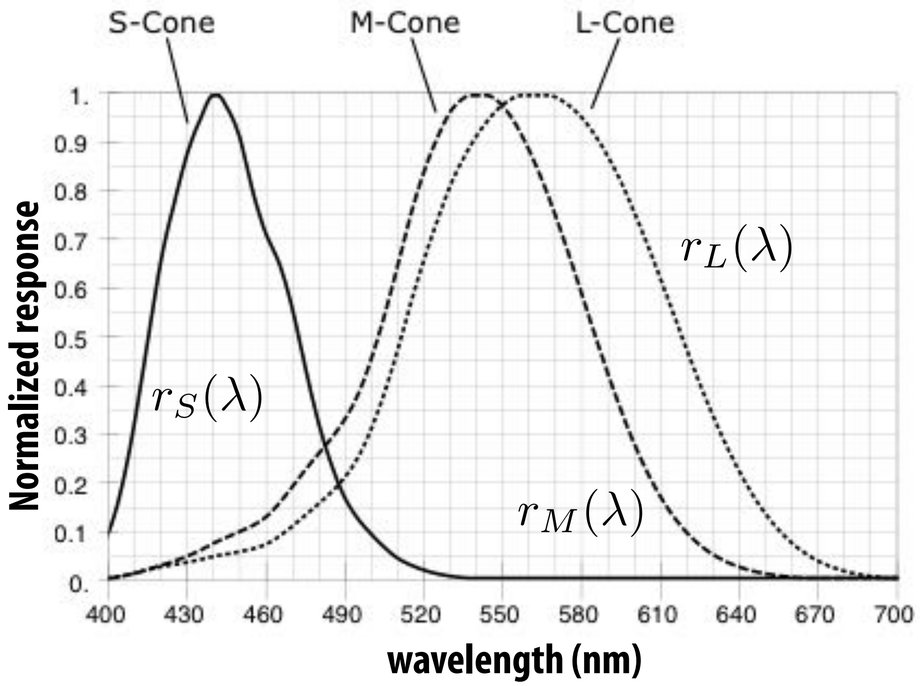
Discrete form: written as vector dot products:
(now using vector *s* to denote discrete representation of SPD $\Phi(\lambda)$)

$$S = r_S \cdot s$$
$$M = r_M \cdot s$$
$$L = r_L \cdot s$$

Matrix formulation:

$$\begin{bmatrix} S \\ M \\ L \end{bmatrix} = \begin{bmatrix} \text{---} & r_S & \text{---} \\ \text{---} & r_M & \text{---} \\ \text{---} & r_L & \text{---} \end{bmatrix} \begin{bmatrix} | \\ s \\ | \end{bmatrix}$$

Response functions for S, M, and L cones

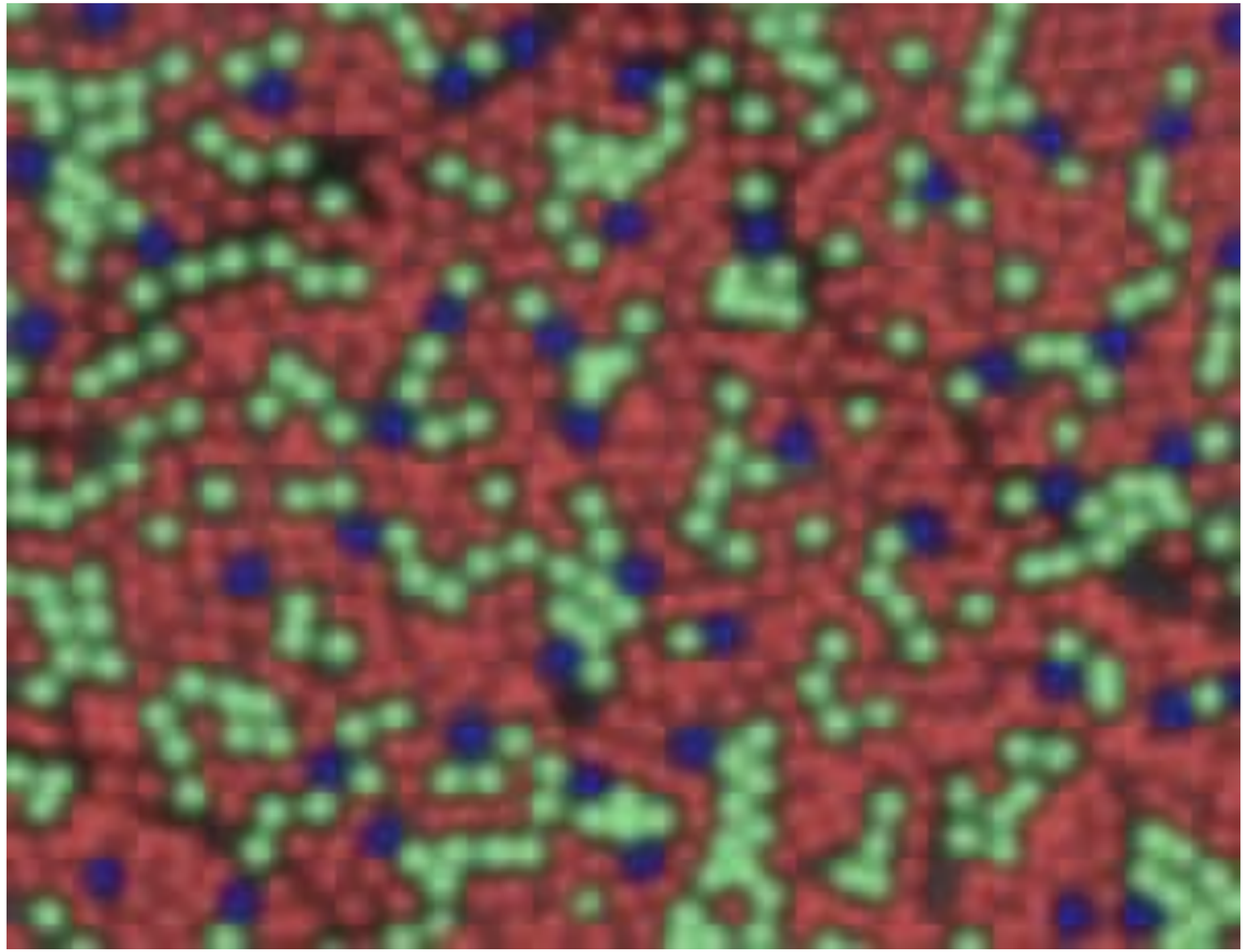


Example: spectral response of human cone cells

Goal: at each pixel, choose scalar R, G, B values for display to perceptually match the real world color

The scene

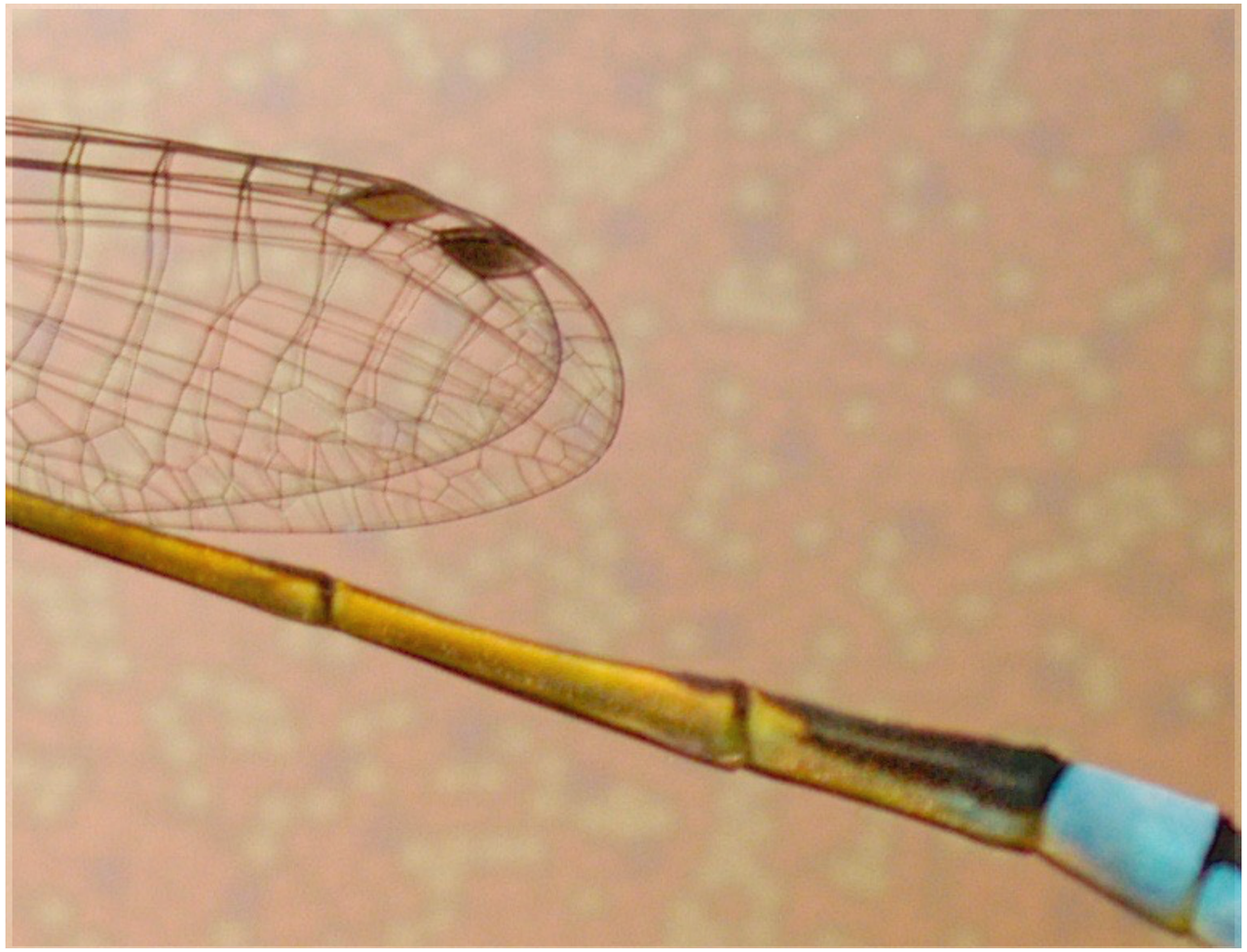
Example: spectral response of human cone cells



Scene projected onto retina

Credit: Sabesan, http://depts.washington.edu/sabaolab/

Example: spectral response of human cone cells



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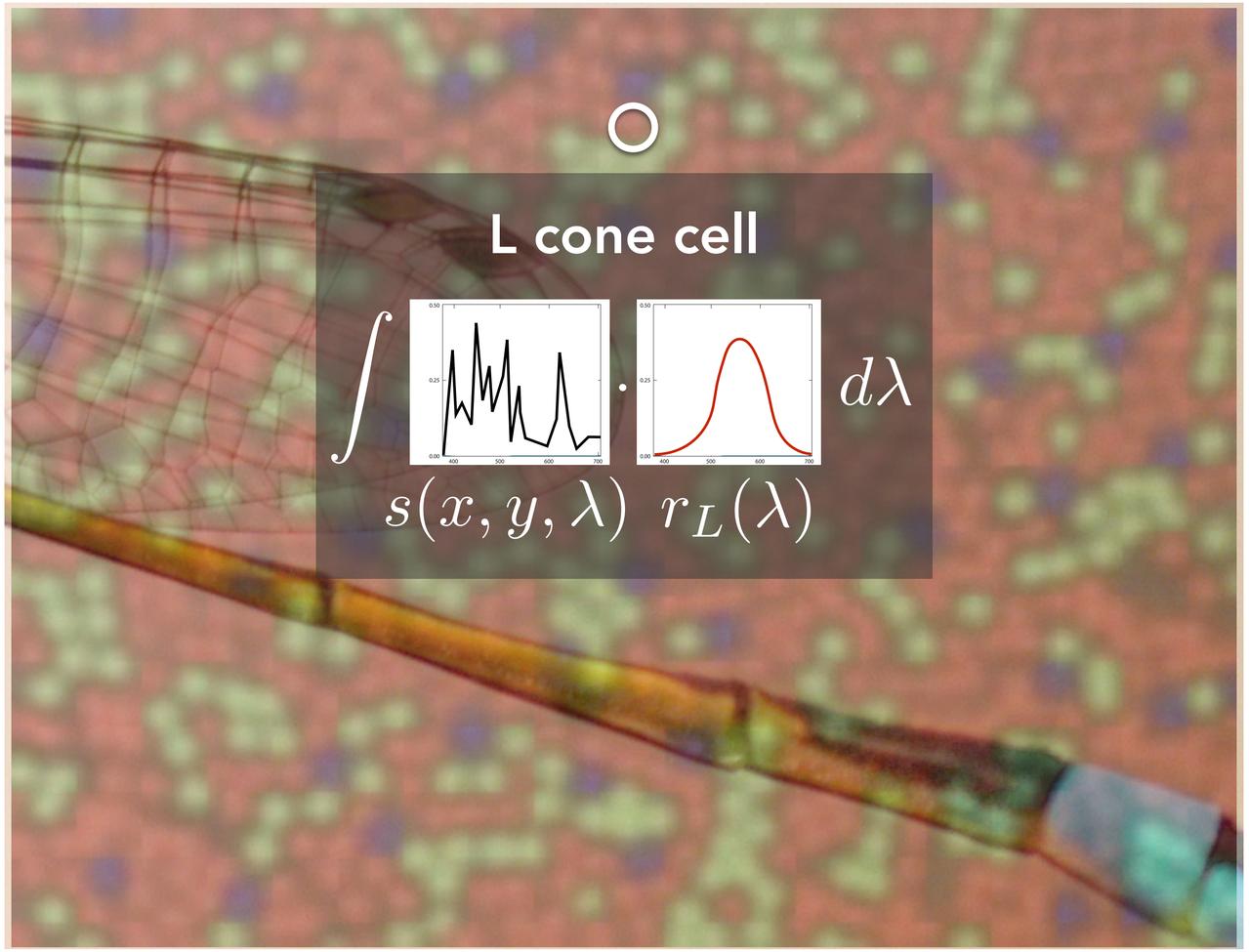

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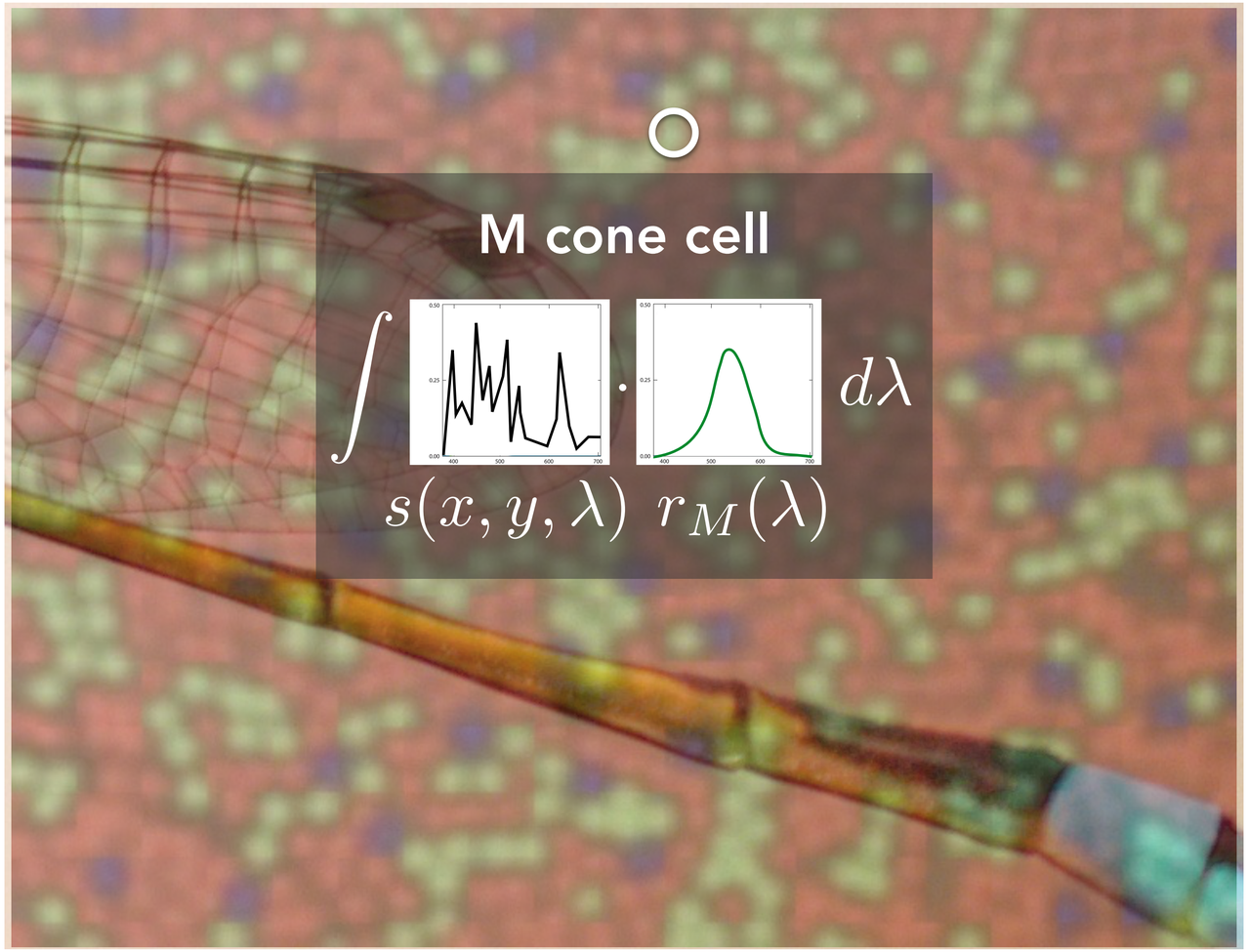
Example: spectral response of human cone cells



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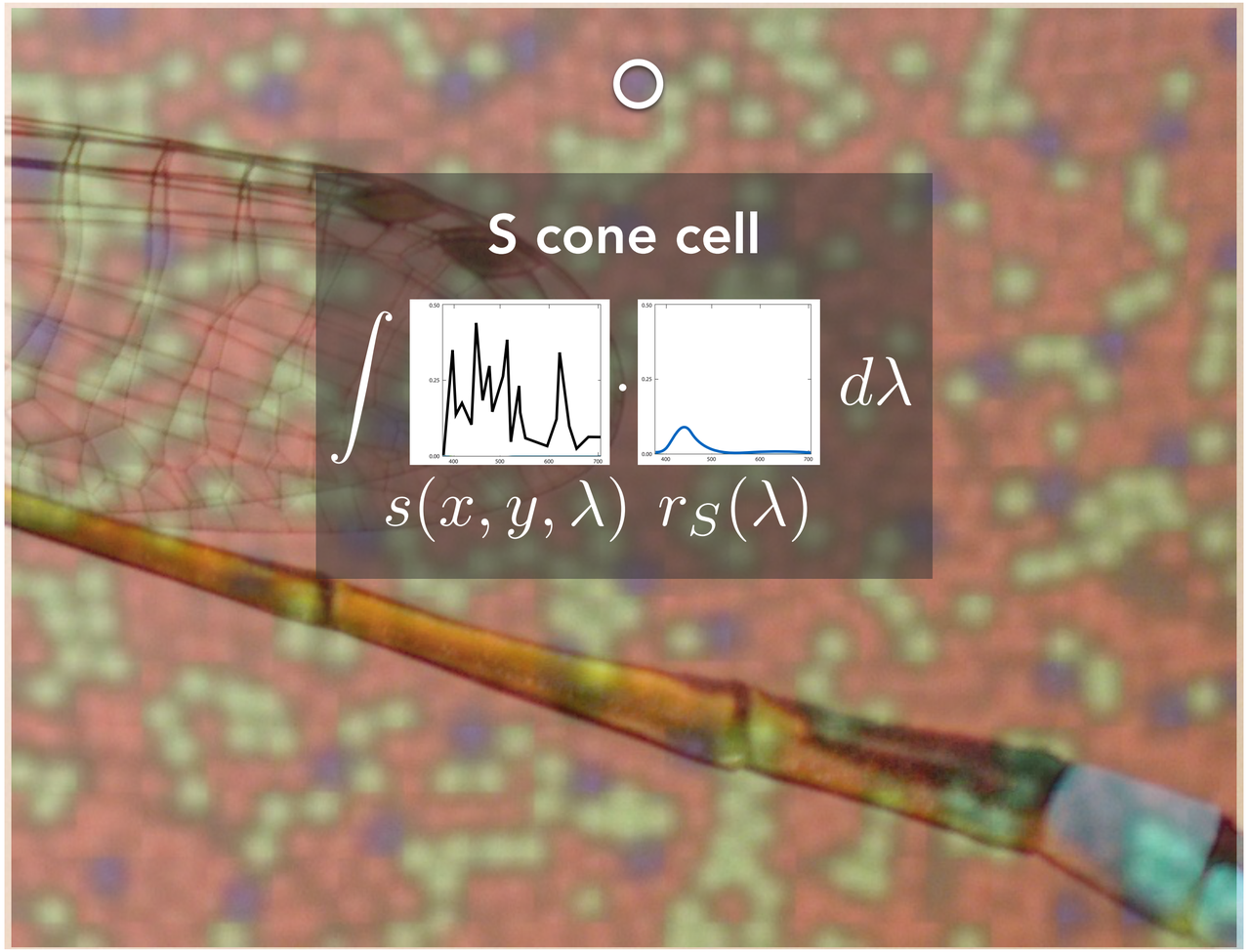


Credit: Sabesan, http://depts.washington.edu/sabaolab/

Dimensionality reduction from ∞ to 3

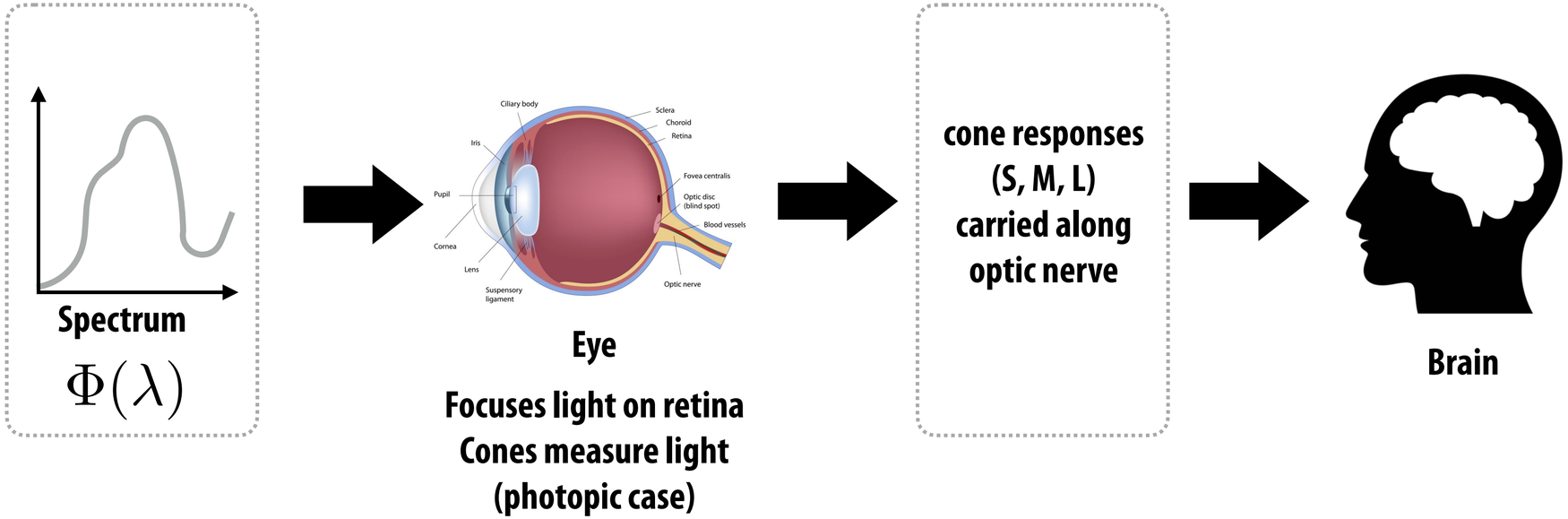
- At each point on the human retina:
  - Spectral power distribution is a function of wavelength (∞ - dimensional signal)
  - 3 types of cones near that position produce three scalar values (3 - dimensional signal)

- What about 2D images?
  - The dimensionality reduction described above is happening at every 2D position in our visual field

The human visual system

- Human eye does not directly measure the spectrum of incoming light
  - a.k.a. the brain does not receive "a spectrum" from the eye

- The eye measures three response values = (S, M, L). The result of integrating the incoming spectrum against response functions of S, M, L-cones



Metamerism

Metamers

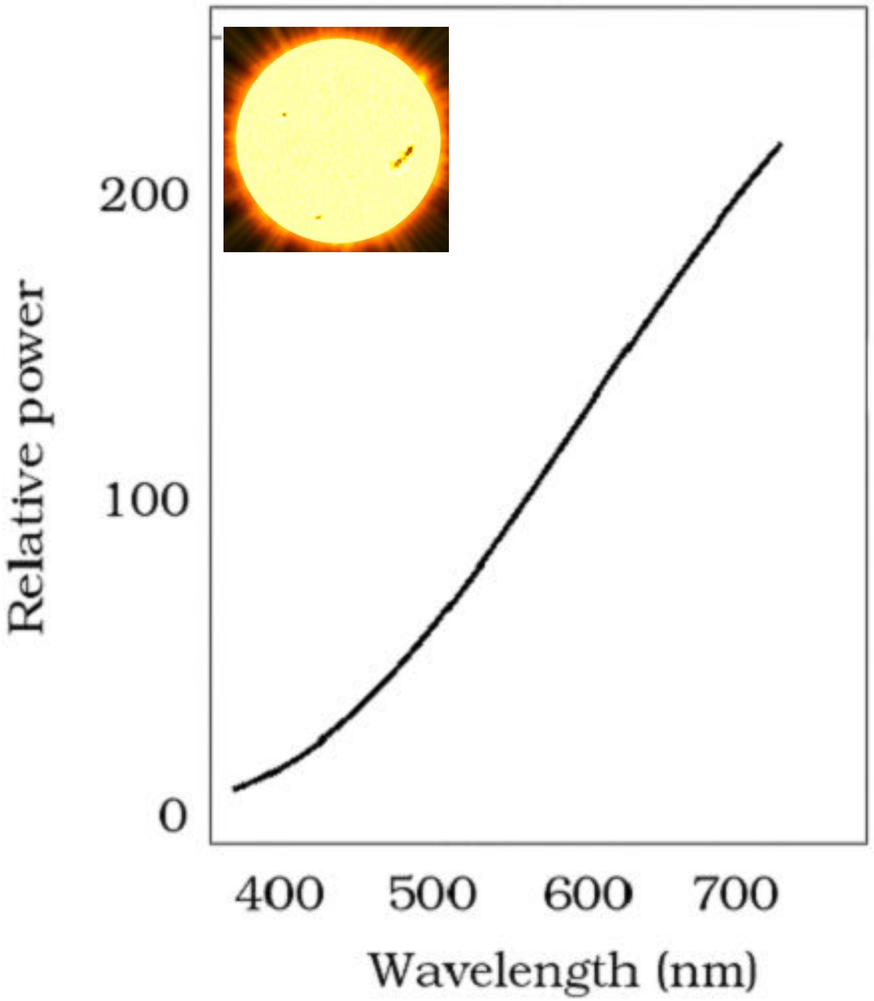
- Metameters are two different spectra (∞-dim) that project to the same (S,M,L) (3-dim) response.
  - These will appear to have the same color to a human

- The existence of metamers is critical to color reproduction
  - It means a computer display does not have to reproduce the full spectrum of a real world scene for it to be perceived to look like the scene
  - It just needs to produce a metamer of the real spectrum
  - Example: display with pixels of only three colors can produce a metamer for the perceived color of a real-world scene

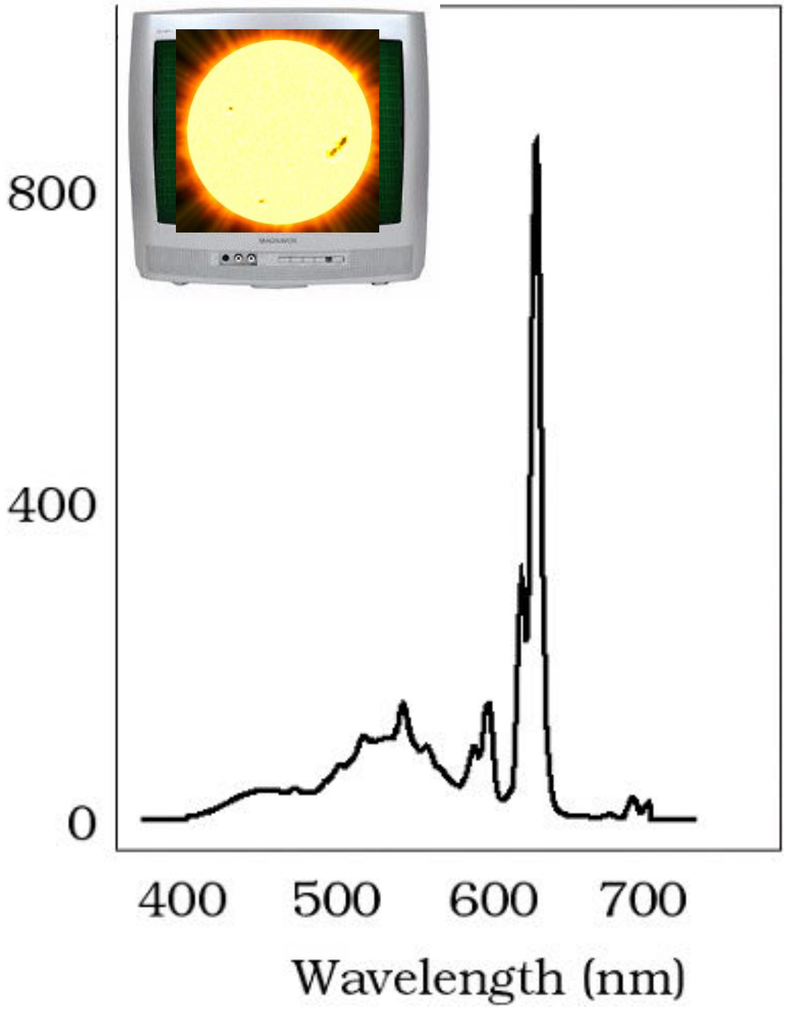
Metamerism

Color matching is an important illusion that is understood quantitatively

Real world SPD



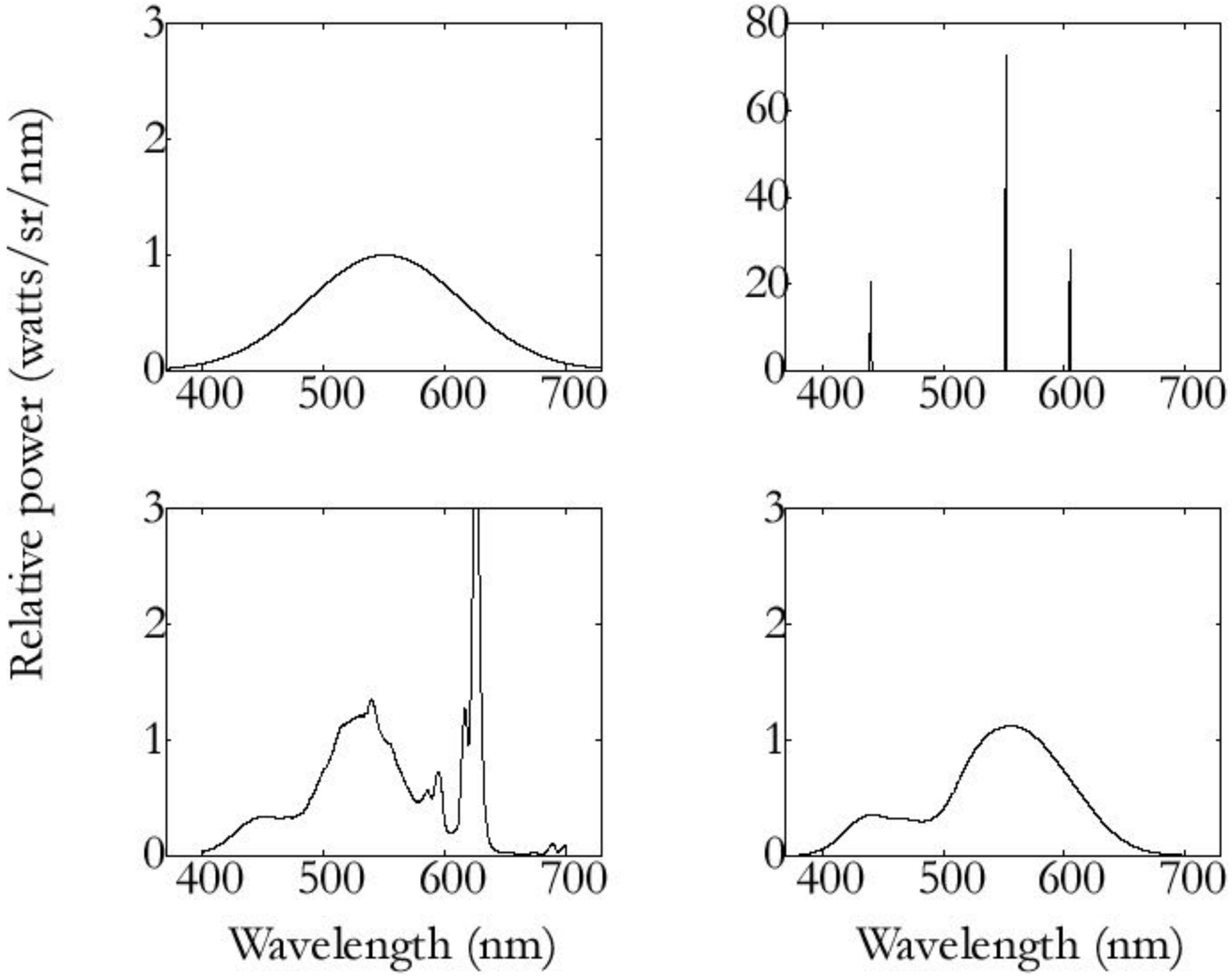
SPD of display



Brian Wandell

Metamerism is a big effect

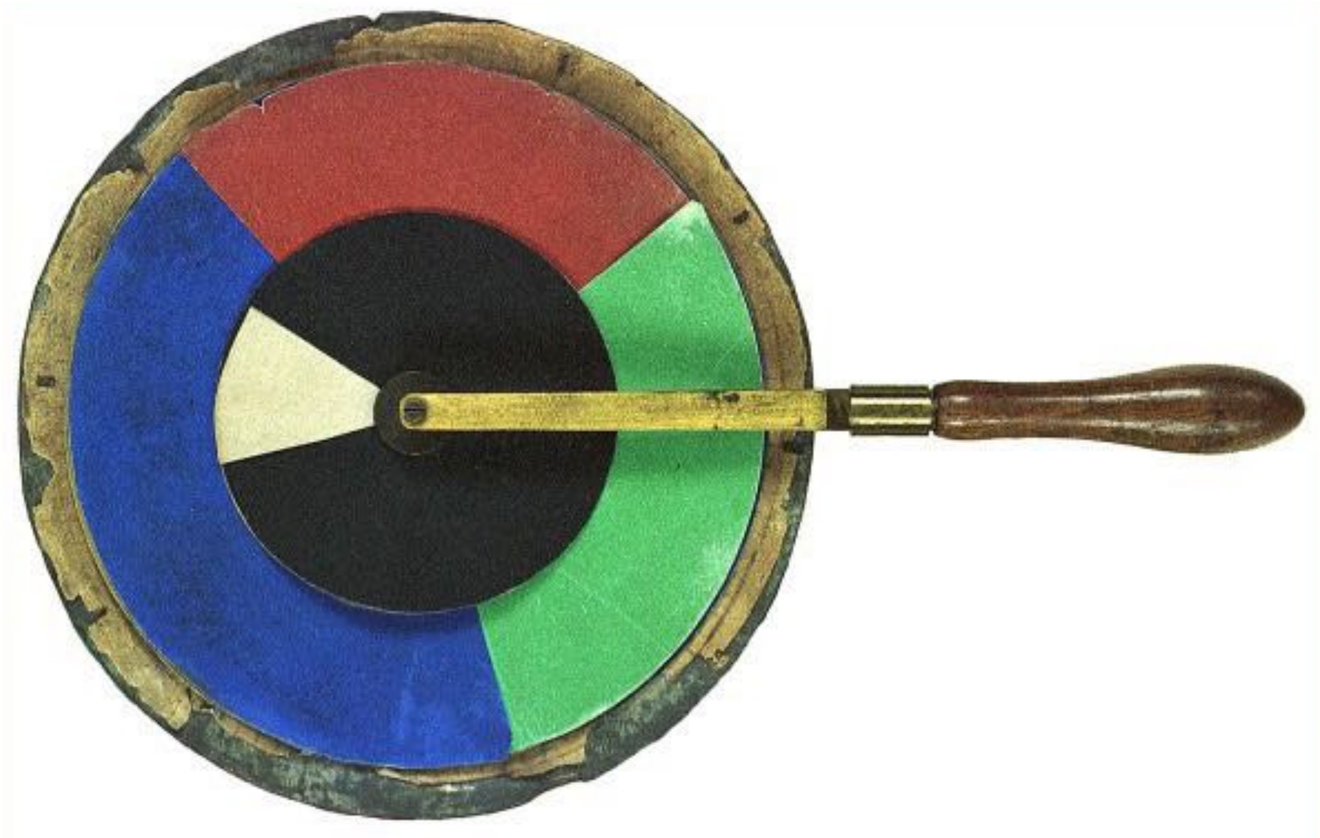
These four different spectrum are metamers (they produce the same response)



Brian Wandell

Searching for a basis for colors: Color matching experiment

Maxwell's crucial color matching experiment

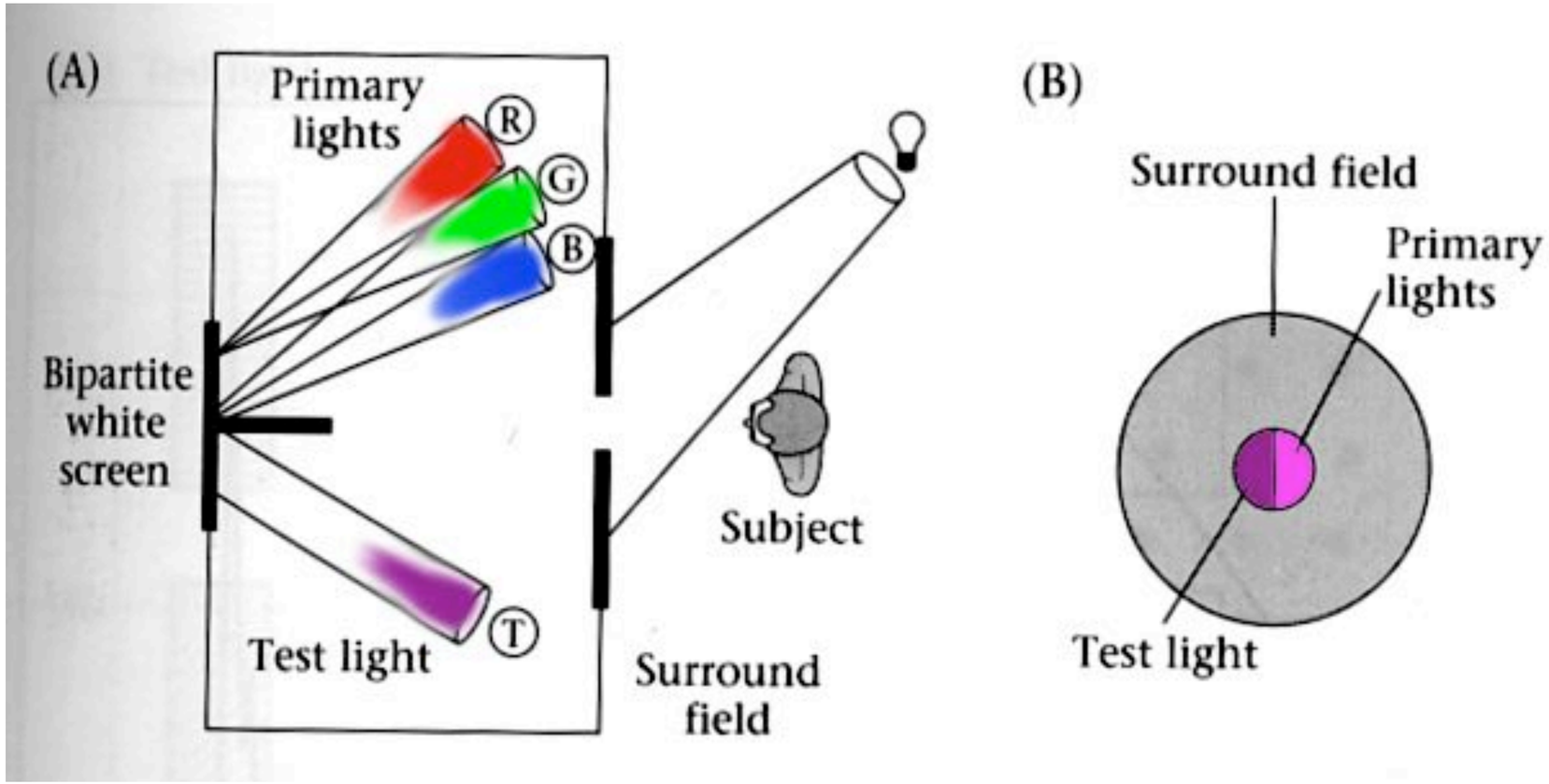


http://designblog.rietveldacademie.nl/?p=68422

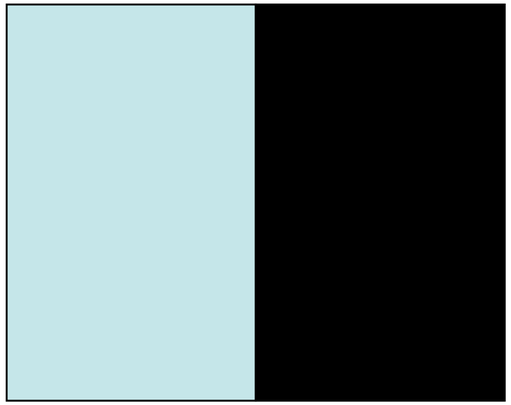
Portrait: http://rsta.royalsocietypublishing.org/content/366/1871/1685

Color matching experiment

- Same idea as spinning top, fancier implementation (Maxwell did this too)
- Show human subject a test light spectrum
- Subject mixes "primaries" until the result matches the appearance of the test light
- The primaries need not be RGB

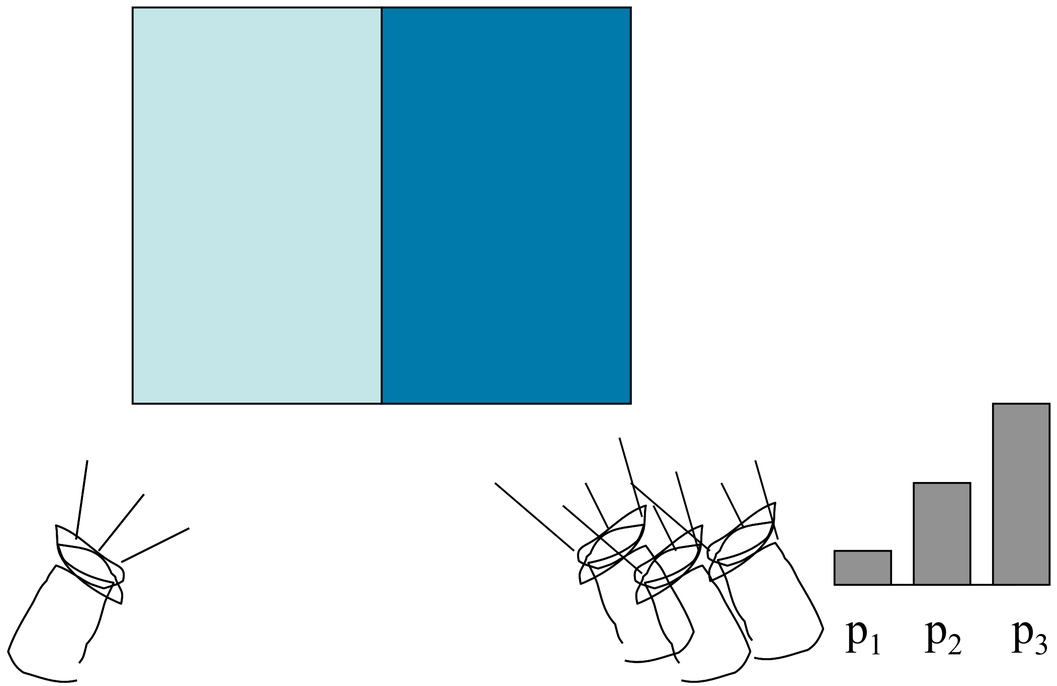


Example experiment



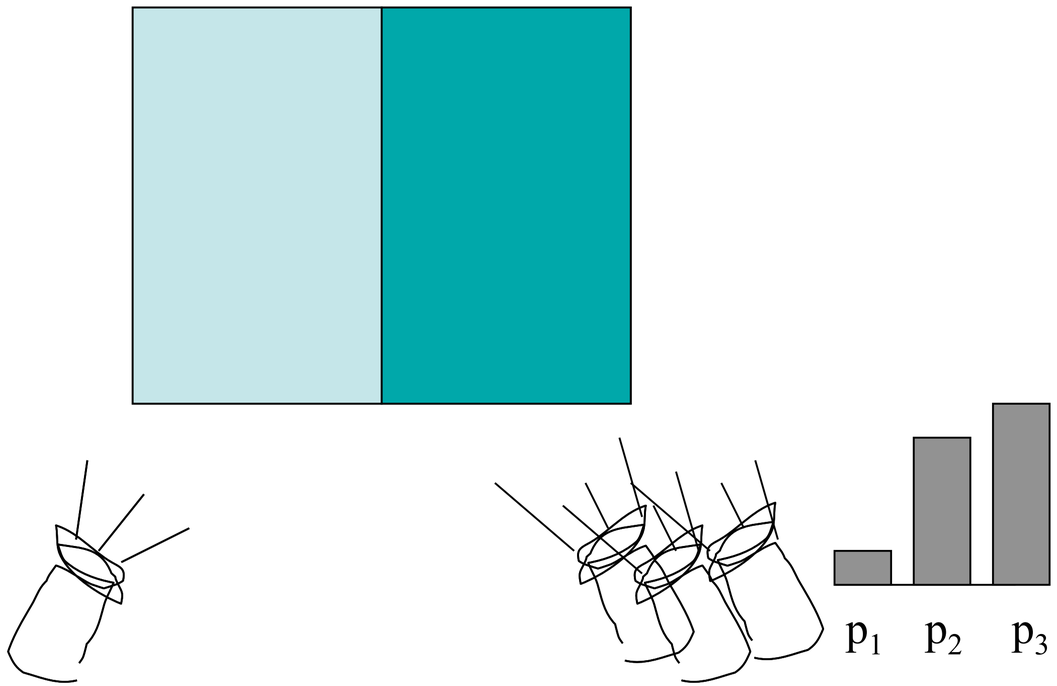
Slide from Durand
and Freeman 06

Example experiment



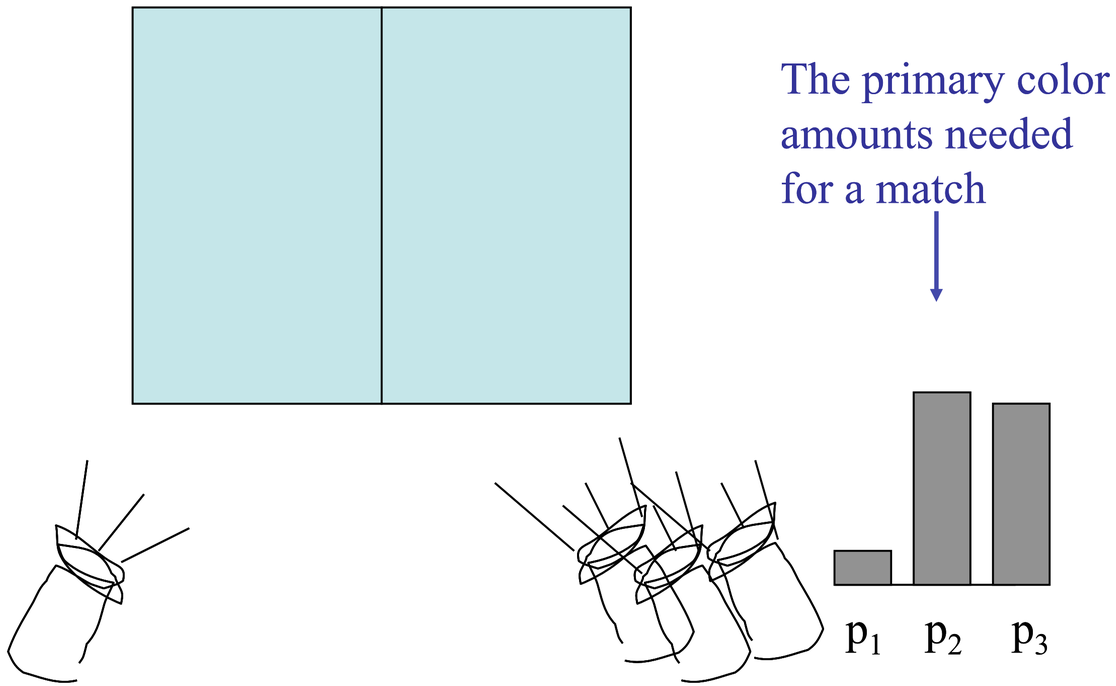
Slide from Durand and Freeman 06

Example experiment



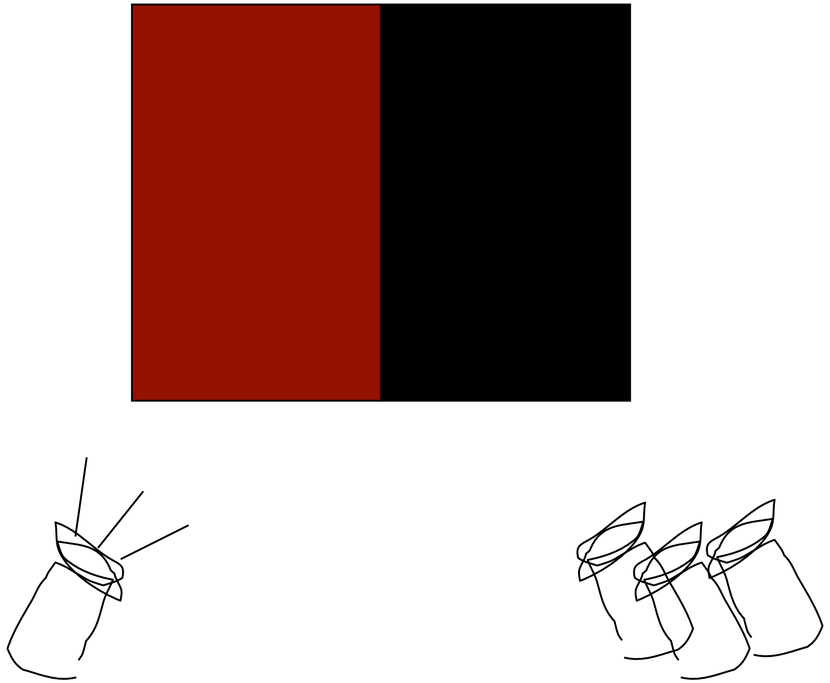
Slide from Durand
and Freeman 06

Example experiment



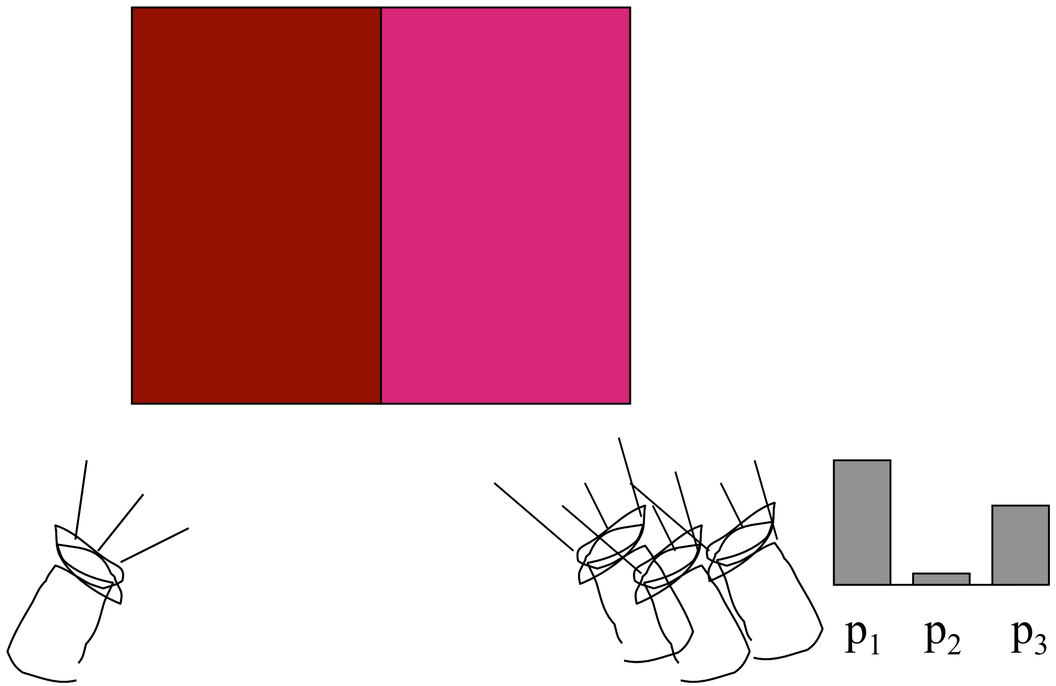
Slide from Durand and Freeman 06

Experiment 2: out of gamut target



Slide from Durand
and Freeman 06

Experiment 2: out of gamut target



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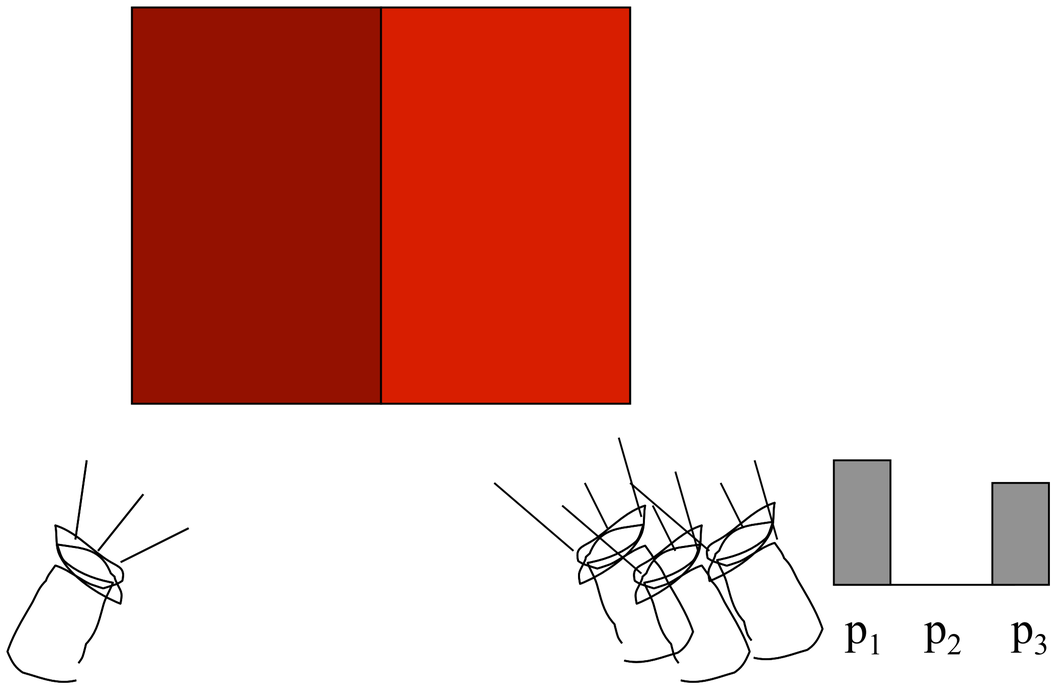
and Freeman 06

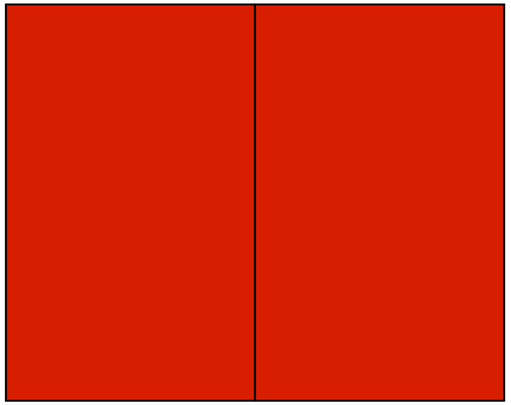
Experiment 2: out of gamut target



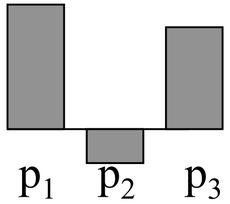
Slide from Durand and Freeman 06

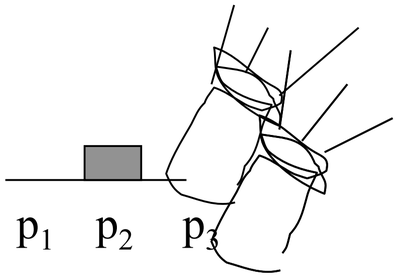
Experiment 2: out of gamut target

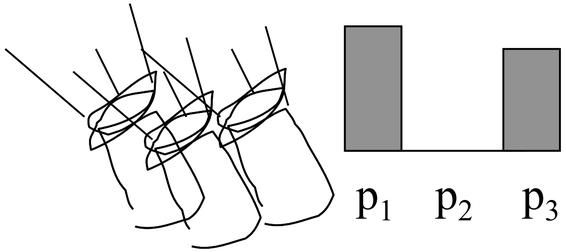
We say a "negative" amount of p_2 was needed to make the match, because we added it to the test color's side.



The primary color amounts needed for a match:



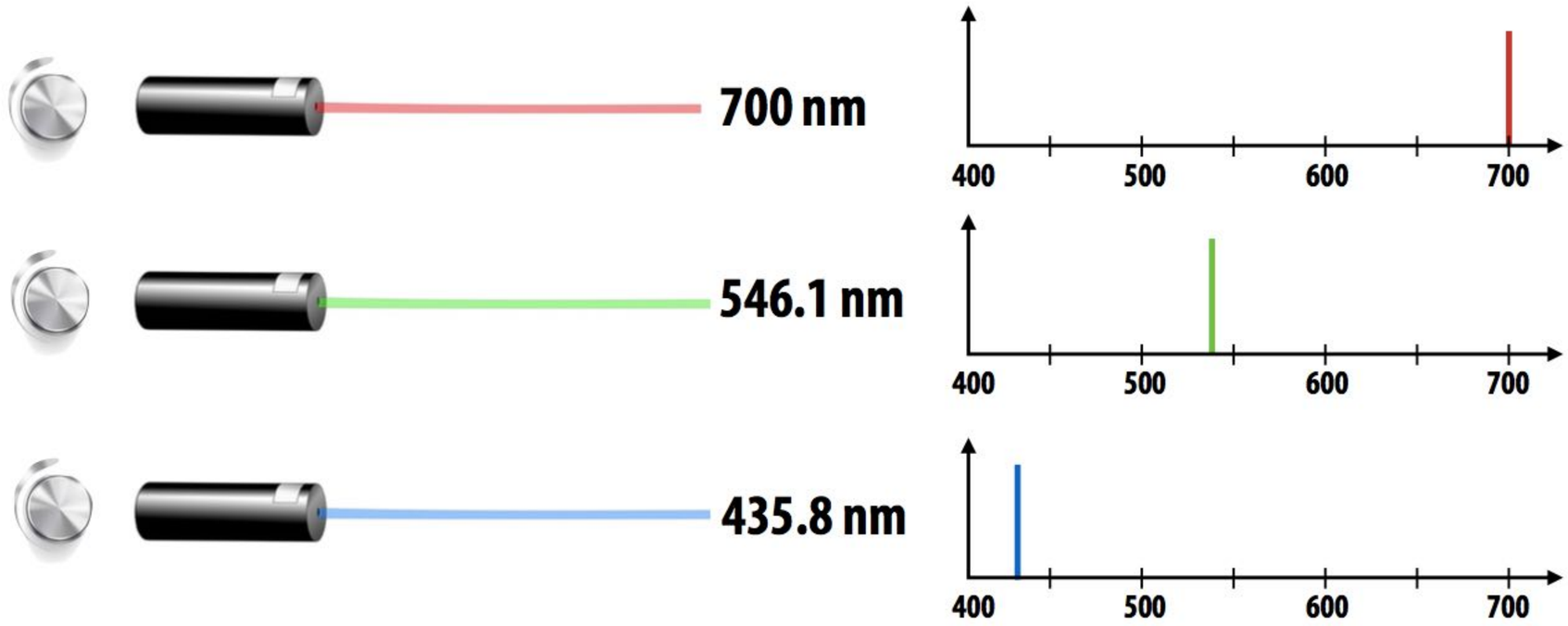




Slide from Durand and Freeman 06

CIE RGB color matching experiment

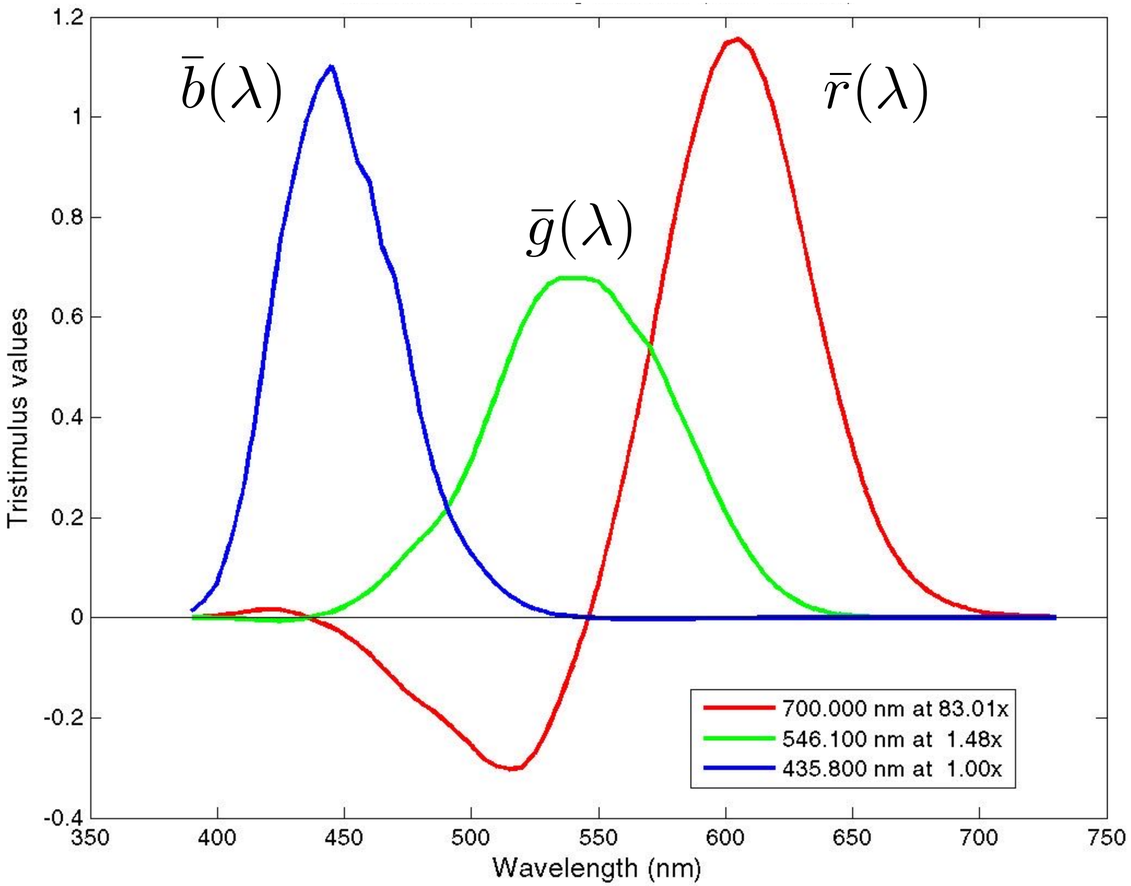
Same setup as additive color matching before, but primaries are monochromatic light (single wavelength) of the following wavelengths (defined by CIE RGB standard)



The test light is also a monochromatic light

CIE RGB color matching functions

This graph plots how much of each CIE RGB primary light must be combined to match the appearance of a monochromatic light of the wavelength given on x-axis



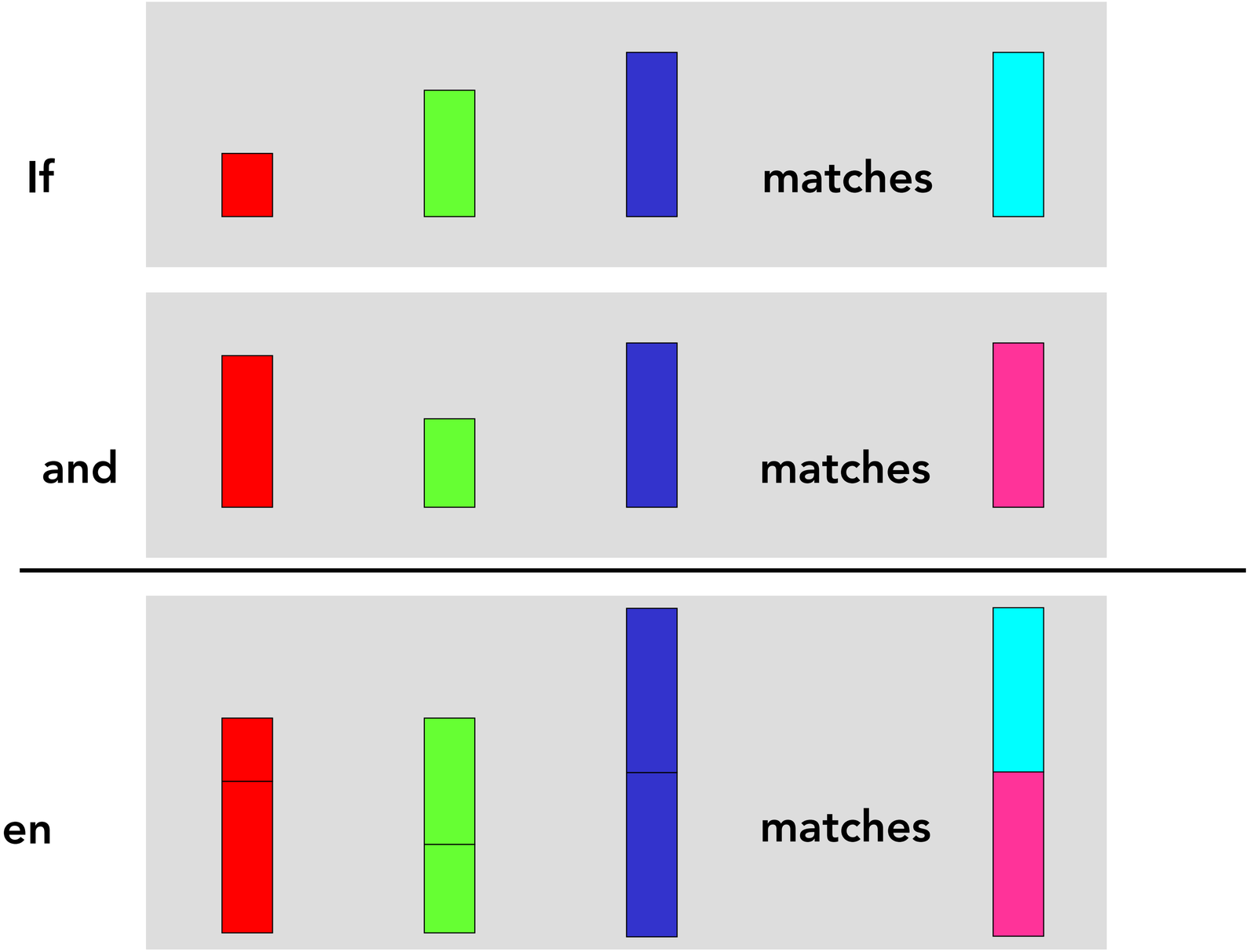
Careful: these graphs are color matching curves. They are not response curves, or the spectra of primaries!

Clarification

- The previous slide plots the results of the color matching experiment for the CIE red, green, and blue laser primaries
  - That is: the figure plots how much of <u>each primary light source</u> is needed to create a spectrum that *appears* to be the same color as a monochromatic reference light
  - Repeating the experiment for many different monochromatic light sources of different wavelengths is moving along the X-axis, yielding the measurements for the curve in the figure
  - So the color of any monochromatic light is represented as a 3-vector, which can be interpreted as how much of each primary is used to make the color

- Do not confuse these plots with the responses of S,M,L cones to monochromatic light… which was plotted earlier in the lecture
  - The color matching experiment works because the output of the visual system has dimensionality 3 (a.k.a. metameters that are the combination of three primaries exist), but the color matching experiment is not directly measuring the response of S,M,L cones.

The color matching experiment is linear



Brian Wandell

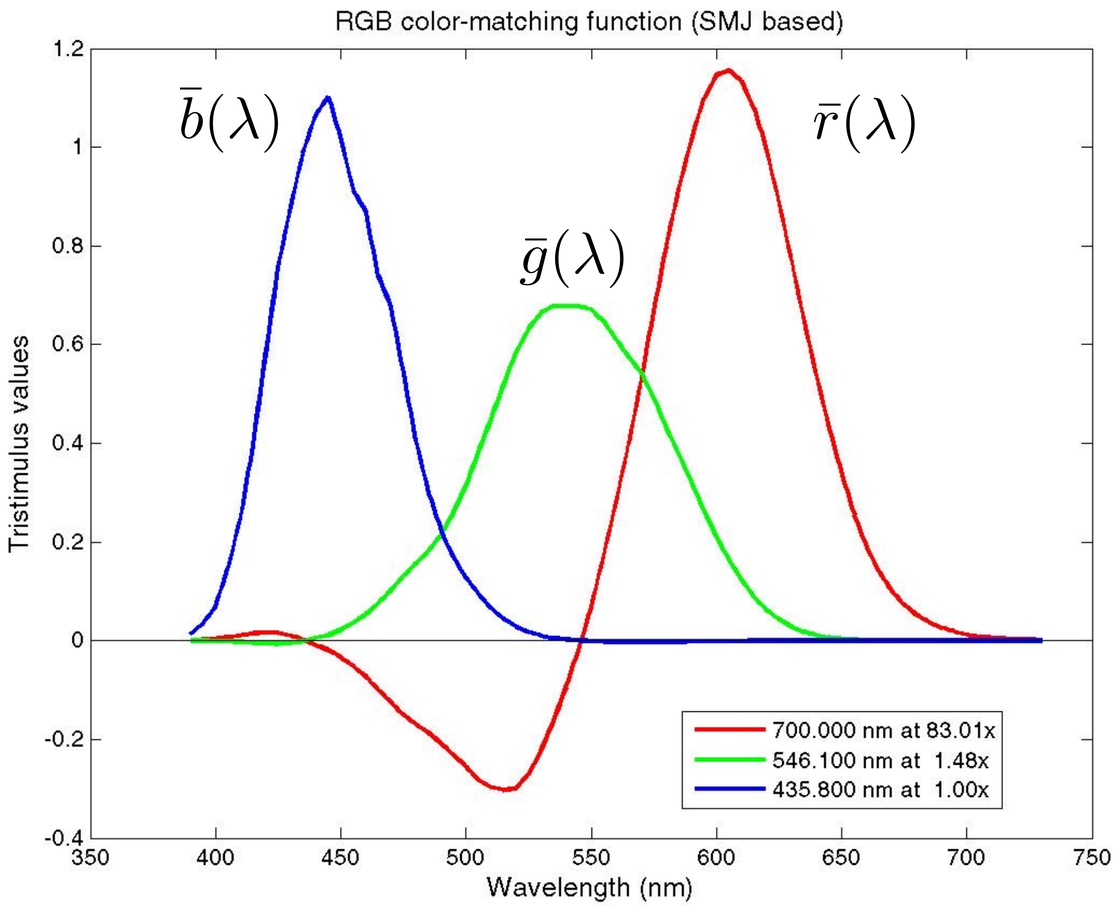
Color reproduction with matching functions

For any spectrum s, the perceived color is matched by the following formulas for scaling the CIE RGB primaries

$$R_{\text{CIE RGB}} = \int_\lambda s(\lambda)\bar{r}(\lambda)\,d\lambda$$

$$G_{\text{CIE RGB}} = \int_\lambda s(\lambda)\bar{g}(\lambda)\,d\lambda$$

$$B_{\text{CIE RGB}} = \int_\lambda s(\lambda)\bar{b}(\lambda)\,d\lambda$$



Careful: these graphs are color matching curves: they are not response curves or primary spectra!

Color reproduction with matching functions

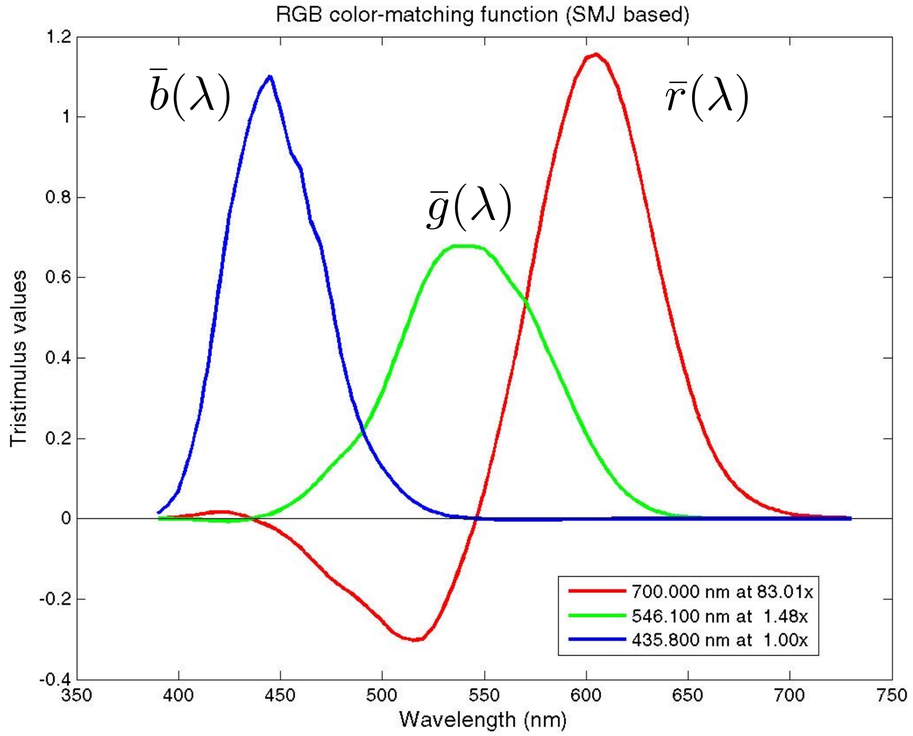
For any spectrum s, the perceived color is matched by the following formulas for scaling the CIE RGB primaries

Written as vector dot products:

$$R_{\text{CIE RGB}} = s \cdot \bar{r}$$
$$G_{\text{CIE RGB}} = s \cdot \bar{g}$$
$$B_{\text{CIE RGB}} = s \cdot \bar{b}$$

Matrix formulation:

$$\begin{bmatrix} R \\ G \\ B \end{bmatrix}_{\text{CIE RGB}} = \begin{bmatrix} — & \bar{r} & — \\ — & \bar{g} & — \\ — & \bar{b} & — \end{bmatrix} \begin{bmatrix} | \\ s \\ | \end{bmatrix}$$

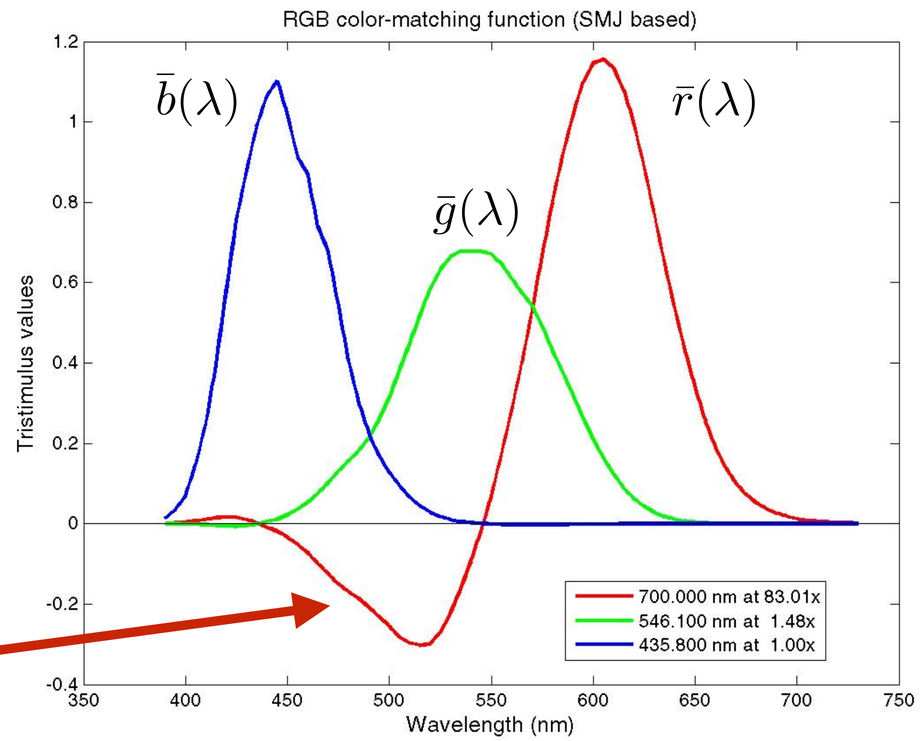


Careful: these graphs are color matching curves: they are not response curves or primary spectra!

Negative red primary?

- There is no positive combination of red, blue, green lasers that yields color that appears the same to a human as monochromatic light of 500 nm ("blue-greenish" light)

- But adding red primary to 500 nm target light yields light whose color can be matched by a combination of blue and green primaries.



Wait a minute: negative red?

Tristimulus Theory of Color

Displays producing color

- Given a set of primary lights, each with its own spectral distribution (e.g. R,G,B display pixels):

$$s_R(\lambda),\ s_G(\lambda),\ s_B(\lambda)$$

- We can adjust the brightness of these lights and add them together to produce a linear subspace of spectral distribution:

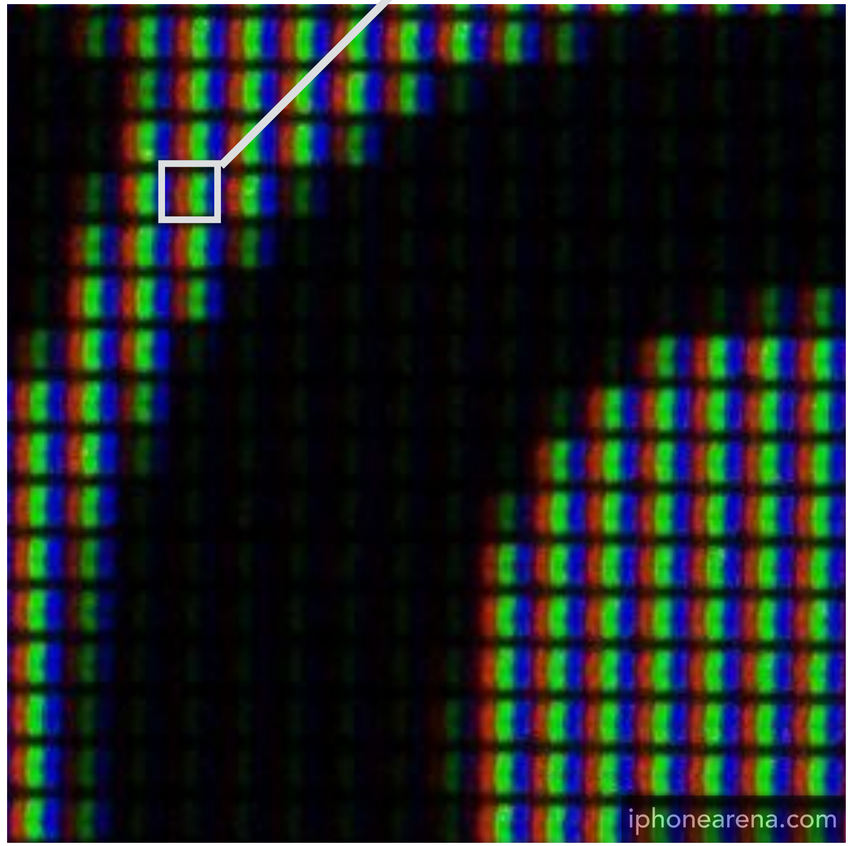
$$R\, s_R(\lambda) + G\, s_G(\lambda) + B\, s_B(\lambda)$$

- The color is now described by the scalar values:

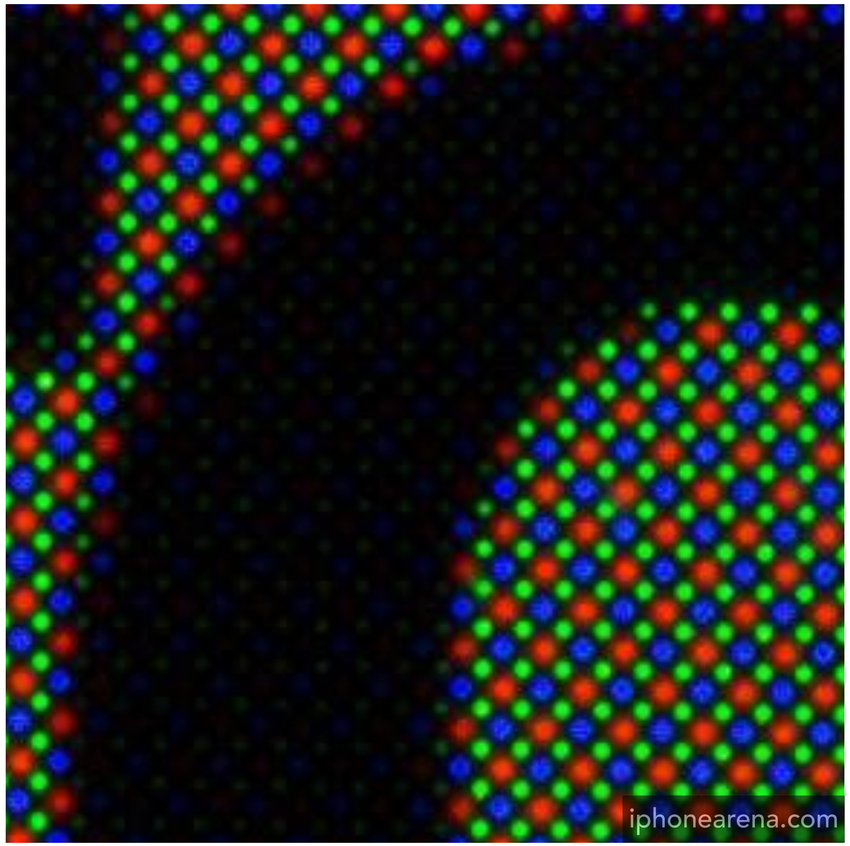
$$R,\ G,\ B$$

Recall: real LCD screen pixels (closeup)

One pixel



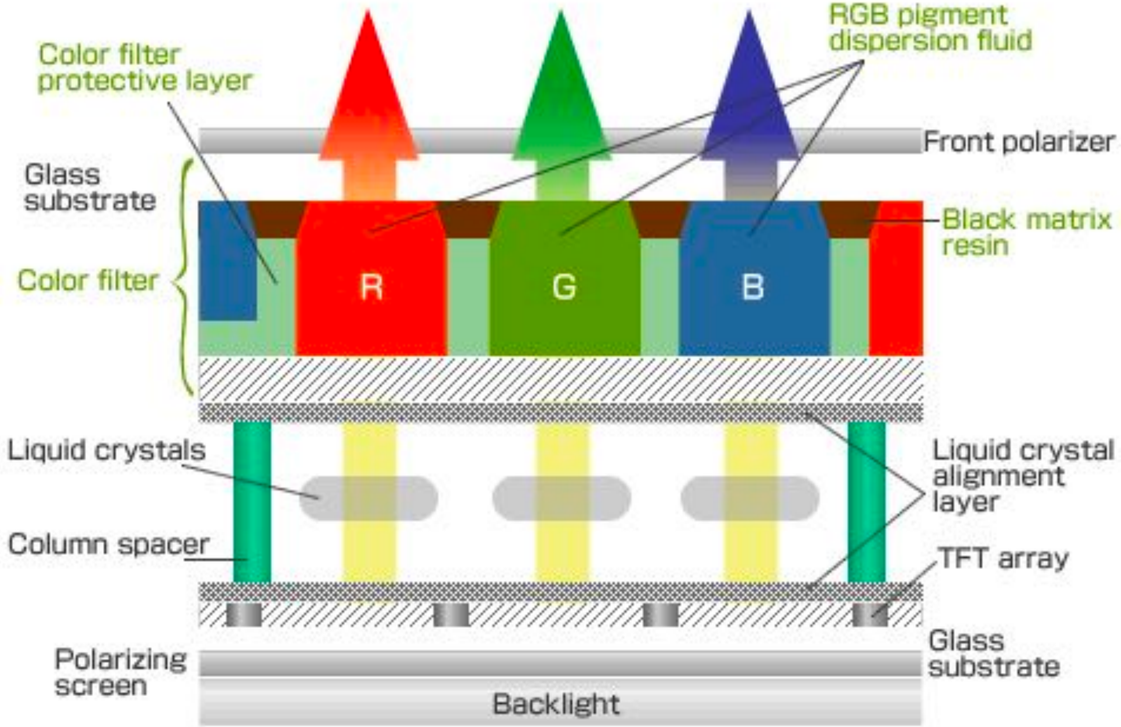
iPhone 6S



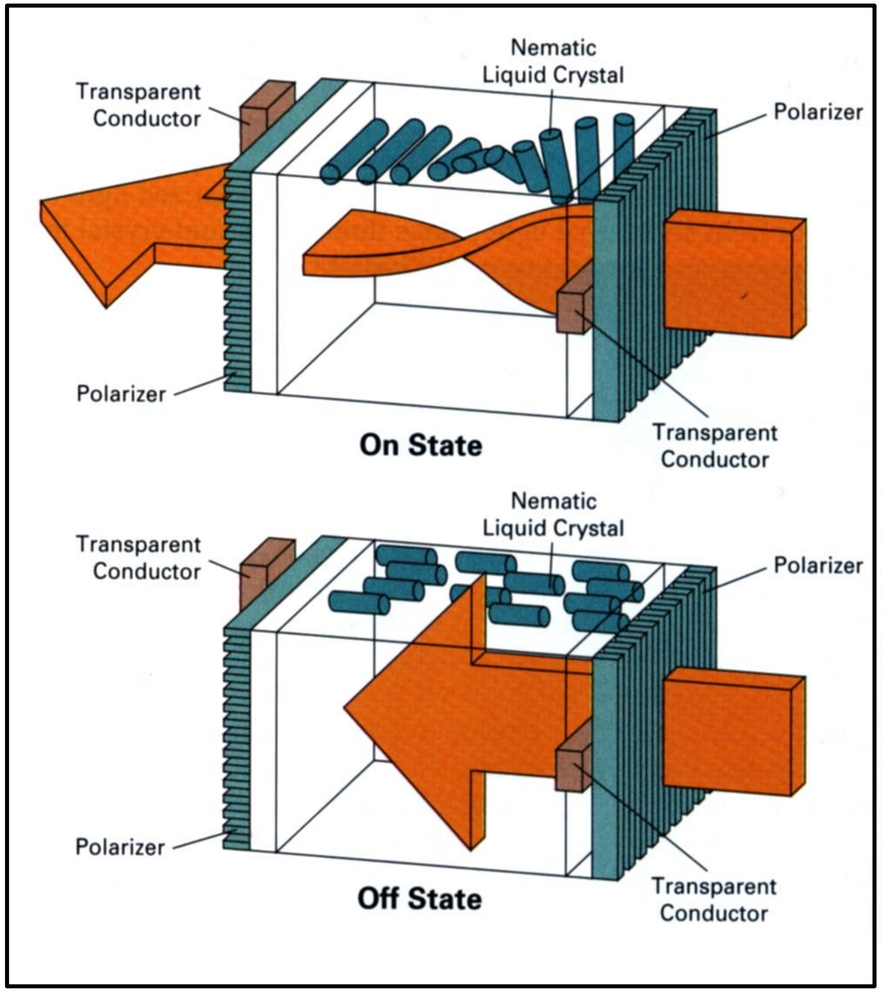
Galaxy S5

Notice R, G, B sub-pixel geometry.
Effectively three lights at each (x,y) location.

Color LCD display



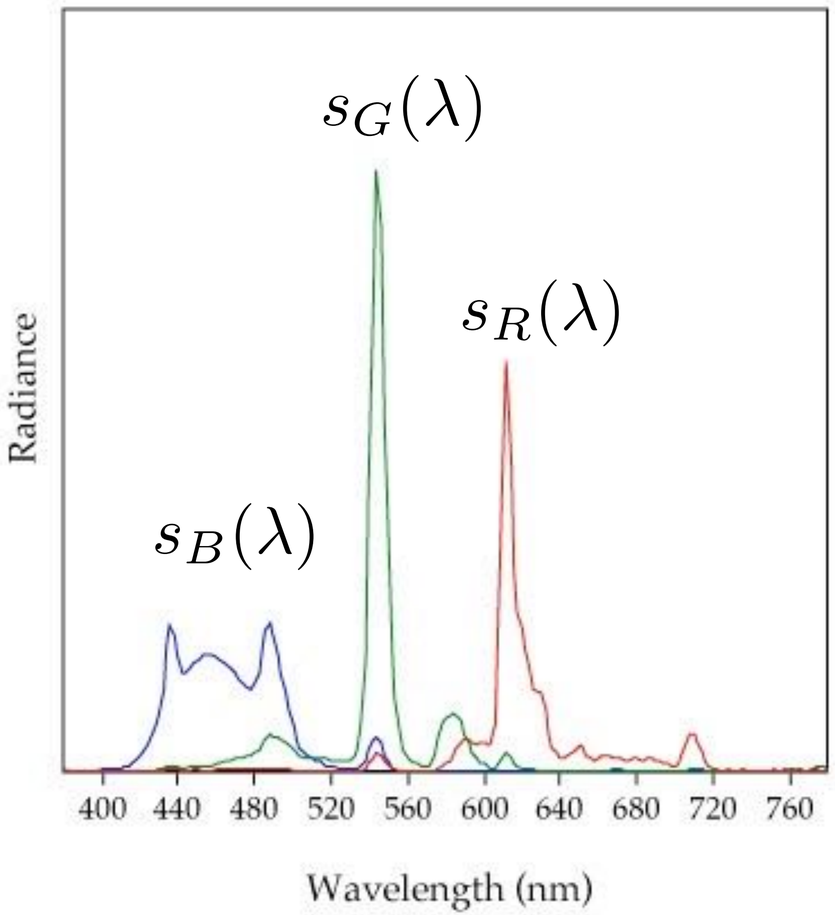
Block or transmit backlight by twisting polarization



[Image credit: H&B fig. 2-16]

[Image credit: NOF Corporation: https://www.nof.co.jp/english/business/display/product01.html]

Example primaries: LCD display



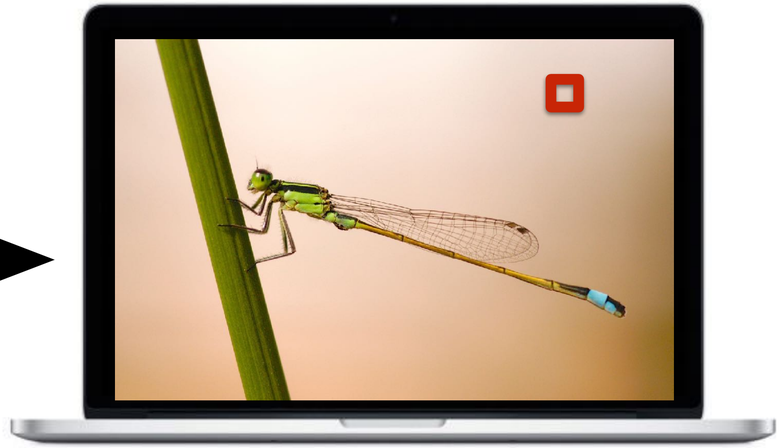
[Fairchild 97]

Spectrum of display primaries (the curves) is determined by display backlight and LCD color filters

Color reproduction problem

- Goal: at each pixel, choose R, G, B values for display so that the output color matches the appearance of the target color in the real world.

Target spectrum
(what is seen in real world)



Display outputs spectrum

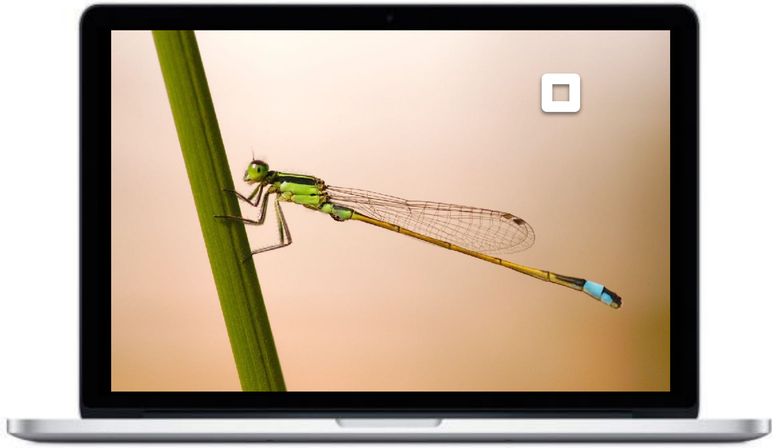
$$R\, s_R(\lambda) + G\, s_G(\lambda) + B\, s_B(\lambda)$$

Color reproduction as linear algebra

Spectrum produced by display given values R,G,B:

$$s_{\text{disp}}(\lambda) = R\, s_R(\lambda) + G\, s_G(\lambda) + B\, s_B(\lambda)$$

$$\Longrightarrow \begin{bmatrix} | \\ s_{\text{disp}} \\ | \end{bmatrix} = \begin{bmatrix} | & | & | \\ s_R & s_G & s_B \\ | & | & | \end{bmatrix} \begin{bmatrix} R \\ G \\ B \end{bmatrix}$$



Color reproduction as linear algebra

- **What color do we perceive when we look at the display?**

$$
\begin{bmatrix} S \\ M \\ L \end{bmatrix}_{\text{disp}} = \begin{bmatrix} — & r_S & — \\ — & r_M & — \\ — & r_L & — \end{bmatrix} \begin{bmatrix} | \\ s_{\text{disp}} \\ | \end{bmatrix}
$$

$$
= \begin{bmatrix} — & r_S & — \\ — & r_M & — \\ — & r_L & — \end{bmatrix} \begin{bmatrix} | & | & | \\ s_R & s_G & s_B \\ | & | & | \end{bmatrix} \begin{bmatrix} R \\ G \\ B \end{bmatrix}
$$

We want this displayed spectrum to be a metamer for the real-world target spectrum.

Color reproduction as linear algebra

Color perceived for display spectra with values R,G,B

$$\begin{bmatrix} S \\ M \\ L \end{bmatrix}_{\text{disp}} = \begin{bmatrix} — & r_S & — \\ — & r_M & — \\ — & r_L & — \end{bmatrix} \begin{bmatrix} | & | & | \\ s_R & s_G & s_B \\ | & | & | \end{bmatrix} \begin{bmatrix} R \\ G \\ B \end{bmatrix}$$

Color perceived for real scene spectra, s

$$\begin{bmatrix} S \\ M \\ L \end{bmatrix}_{\text{real}} = \begin{bmatrix} — & r_S & — \\ — & r_M & — \\ — & r_L & — \end{bmatrix} \begin{bmatrix} | \\ s \\ | \end{bmatrix}$$

How do we reproduce the color of s?

Set these lines equal and solve for R,G,B as a function of s!

Color reproduction as linear algebra

Solution:

$$\begin{bmatrix} — & r_S & — \\ — & r_M & — \\ — & r_L & — \end{bmatrix} \begin{bmatrix} | & | & | \\ s_R & s_G & s_B \\ | & | & | \end{bmatrix} \begin{bmatrix} R \\ G \\ B \end{bmatrix} = \begin{bmatrix} — & r_S & — \\ — & r_M & — \\ — & r_L & — \end{bmatrix} \begin{bmatrix} | \\ s \\ | \end{bmatrix}$$

$$\Longrightarrow \begin{bmatrix} R \\ G \\ B \end{bmatrix} = \left(\begin{bmatrix} — & r_S & — \\ — & r_M & — \\ — & r_L & — \end{bmatrix} \begin{bmatrix} | & | & | \\ s_R & s_G & s_B \\ | & | & | \end{bmatrix} \right)^{-1} \begin{bmatrix} — & r_S & — \\ — & r_M & — \\ — & r_L & — \end{bmatrix} \begin{bmatrix} | \\ s \\ | \end{bmatrix}$$

Color reproduction as linear algebra

Solution (form #1):

$$\underset{1\text{x}3}{\begin{bmatrix} R \\ G \\ B \end{bmatrix}} = \underbrace{\left(\underset{N\text{x}3}{\begin{bmatrix} — & r_S & — \\ — & r_M & — \\ — & r_L & — \end{bmatrix}} \underset{3\text{x}N}{\begin{bmatrix} | & | & | \\ s_R & s_G & s_B \\ | & | & | \end{bmatrix}} \right)^{-1}}_{3\text{x}3} \underbrace{\underset{N\text{x}3}{\begin{bmatrix} — & r_S & — \\ — & r_M & — \\ — & r_L & — \end{bmatrix}} \underset{1\text{x}N}{\begin{bmatrix} | \\ s \\ | \end{bmatrix}}}_{1\text{x}3}$$

Solution (form #2):

$$\underset{1\text{x}3}{RGB} = \underbrace{(\underset{N\text{x}3}{\mathbf{M}_{SML}} \underset{3\text{x}N}{\mathbf{M}_{RGB}})^{-1} \underset{N\text{x}3}{\mathbf{M}_{SML}}}_{N\text{x}3} \underset{1\text{x}N}{s}$$

Color reproduction as linear algebra

Solution (form #3):

$$\begin{bmatrix} R \\ G \\ B \end{bmatrix} = \underbrace{\begin{bmatrix} r_S \cdot s_R & r_S \cdot s_G & r_S \cdot s_B \\ r_M \cdot s_R & r_M \cdot s_G & r_M \cdot s_B \\ r_L \cdot s_R & r_L \cdot s_G & r_L \cdot s_B \end{bmatrix}^{-1} \begin{bmatrix} — & r_S & — \\ — & r_M & — \\ — & r_L & — \end{bmatrix}}_{\text{Nx3}} \begin{bmatrix} | \\ s \\ | \end{bmatrix}$$

This Nx3 matrix contains, as row vectors,
"color matching functions"
associated with the primary lights s_R, s_G, s_B.

Color reproduction issue: no negative light

- R,G,B values must be positive
  - Display primaries can't emit negative light
  - But solution formulas can certainly produce negative R,G,B values

- What do negative R,G,B values mean?
  - Display can't physically reproduce the desired color
  - Desired color is outside the display's "color gamut" (more on this later)

Color Representation

Color spaces

- Need three numbers to specify a color
  - But what three numbers?
  - A color space is an answer to this question

- Common example: color space defined by a display
  - Define colors by what R, G, B scalar values will produce them on your monitor
    - Output spectra $s = rR + gG + bB$ for some display primary spectra r, g, b
  - This a device dependent representation of color: if I choose R,G,B by looking at my display and send those values to you, you may not see the same color on your display (which might have different primaries, etc.)

Standard color spaces

- Standardized RGB (sRGB)
  - Makes a particular monitor's primaries the RGB standard
  - Other color devices simulate that monitor by calibration
  - sRGB is usable as an interchange color space; widely adopted today

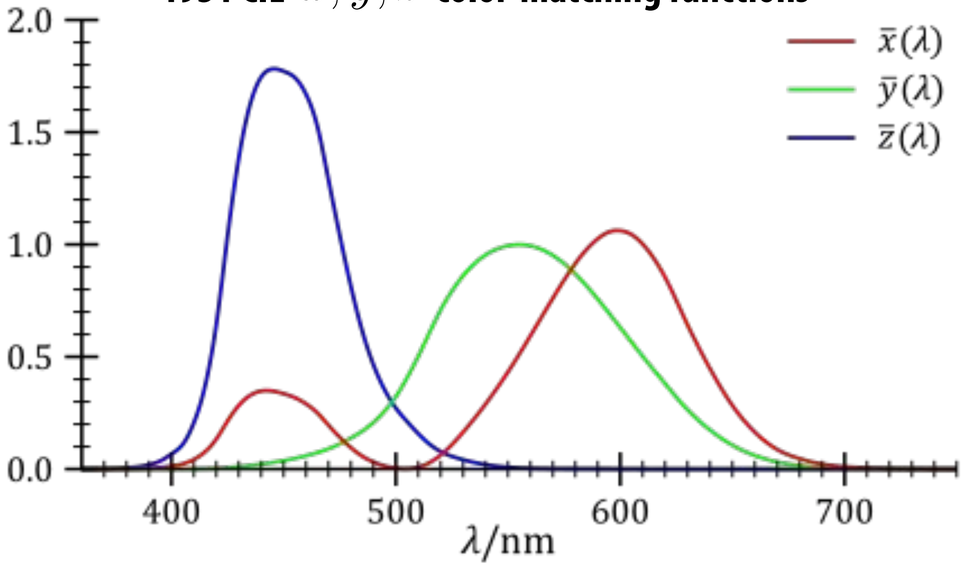
A "universal" color space: CIE XYZ

- Imaginary set of standard color primaries X, Y, Z

- Designed such that
  - X, Y, Z span all observable colors
  - Matching functions are strictly positive
  - Y is luminance (brightness absent color)

- "Imaginary" because the spectrum of the X,Y,Z primaries corresponding to these color matching functions are negative at some wavelengths

1931 CIE $\overline{x}, \overline{y}, \overline{z}$ color-matching functions



Careful: these graphs are color matching curves, not spectra!

For any spectrum $\Phi(\lambda)$, can express spectrum as weighted combination of primaries. Weights (X,Y,Z) given by:

$$X = k \int_\lambda \Phi(\lambda)\overline{x}(\lambda)d\lambda$$

$$Y = k \int_\lambda \Phi(\lambda)\overline{y}(\lambda)d\lambda$$

$$Z = k \int_\lambda \Phi(\lambda)\overline{z}(\lambda)d\lambda$$

[Image credit: Wikipedia]

Mathematically: just a change of basis

- By definition, all observable monochromatic spectra are positive points in XYZ space, so can convert a color's representation (in space defined by realizable primaries like RGB) to XYZ via a linear transform:
  - Consider display with 3 primaries (primaries need not be monochromatic light)
  - Compute XYZ coords of light emitted by display when providing it (1,0,0), (0,1,0), (0,0,1)
  - Light generated by display is linear combination of these vectors (non-negative weights)

color of R primary ([1,0,0] on display) $= R_x\mathbf{X} + R_y\mathbf{Y} + R_z\mathbf{Z}$

color of G primary ([0,1,0] on display) $= G_x\mathbf{X} + G_y\mathbf{Y} + G_z\mathbf{Z}$

color of B primary ([0,1,0] on display) $= B_x\mathbf{X} + B_y\mathbf{Y} + B_z\mathbf{Z}$

$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \begin{bmatrix} R_x & G_x & B_x \\ R_y & G_y & B_y \\ R_z & G_z & B_z \end{bmatrix} \begin{bmatrix} R \\ G \\ B \end{bmatrix}$$

XYZ representation

color in space of display primaries

- Example: Converting from CIE RGB to CIE XYZ:

$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \frac{1}{0.17697} \begin{bmatrix} 0.49 & 0.31 & 0.20 \\ 0.17687 & 0.81240 & 0.01063 \\ 0.00 & 0.01 & 0.99 \end{bmatrix} \begin{bmatrix} R \\ G \\ B \end{bmatrix}$$

Brightness

- The color matching experiments measure how a human observer perceives color. The goal was to match the perceived color of one spectrum with a new spectrum (a metamer) formed via the combination of three primaries.

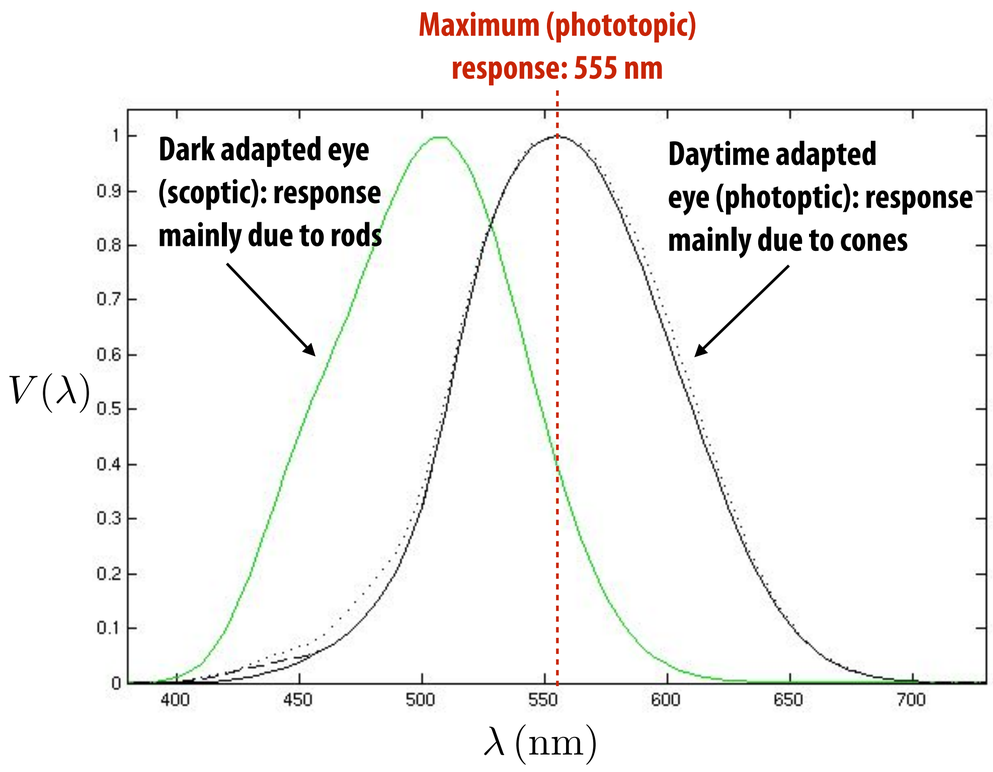
- We can also ask the question, given lights with two different colors but equal power, how bright do the lights look?

Luminance (brightness)

- Product of radiance and the eye's luminous efficiency

$$Y = \int \Phi(\lambda) V(\lambda) \, \mathrm{d}\lambda$$

- Luminous efficiency is measure of how bright light at a given wavelength is perceived by a human (due to the eye's response to light at that wavelength)



- How to measure the eye's response curve $V(\lambda)$?
  - Adjust power of monochromatic light source of wavelength λ until it matches the brightness of reference 555 nm source (photopic case)
  - Notice: the sensitivity of photopic eye is maximized at ~ 555 nm

https://upload.wikimedia.org/wikipedia/commons/a/a0/Luminosity.png

LMS responses plotted as 3D color space

- Visualization of "spectral locus" of human cone cells' response to monochromatic light (light with energy in a single wavelength) as points in 3D space.

- This is a plot of the S, M, L response functions as a point in 3D space.

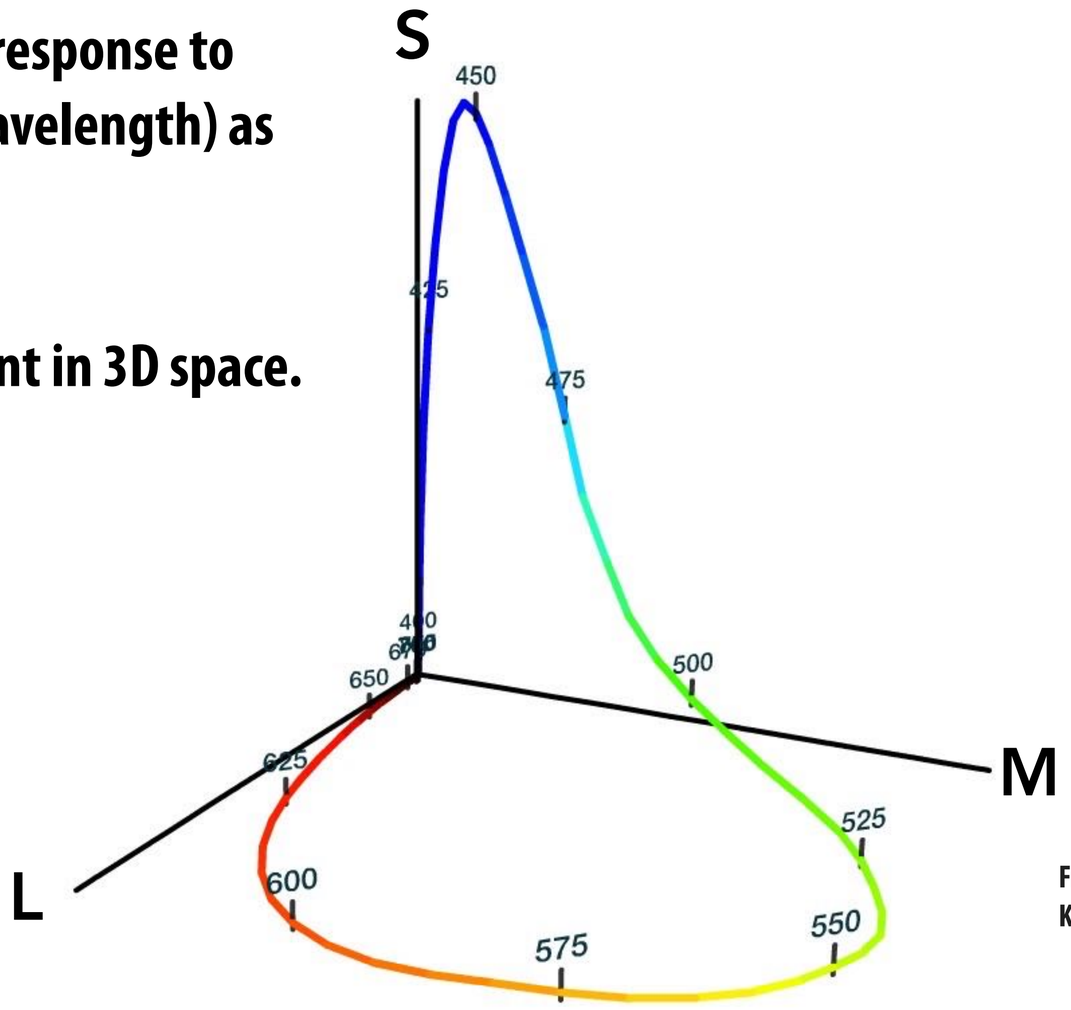
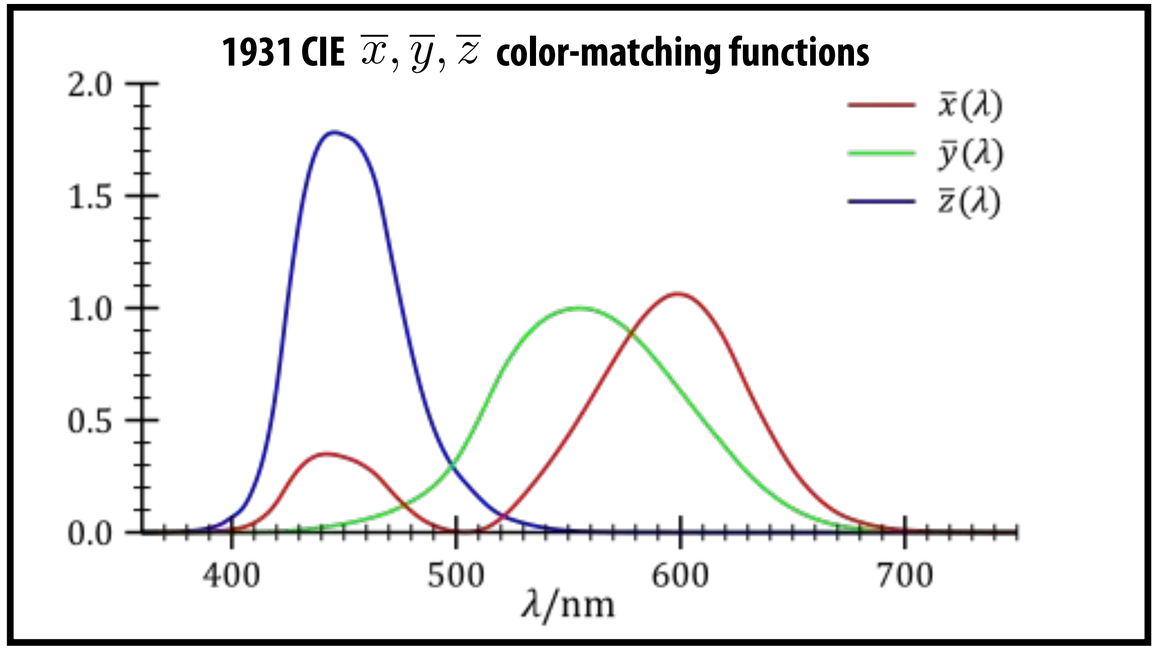


Figure Credit:
Katie Dektar

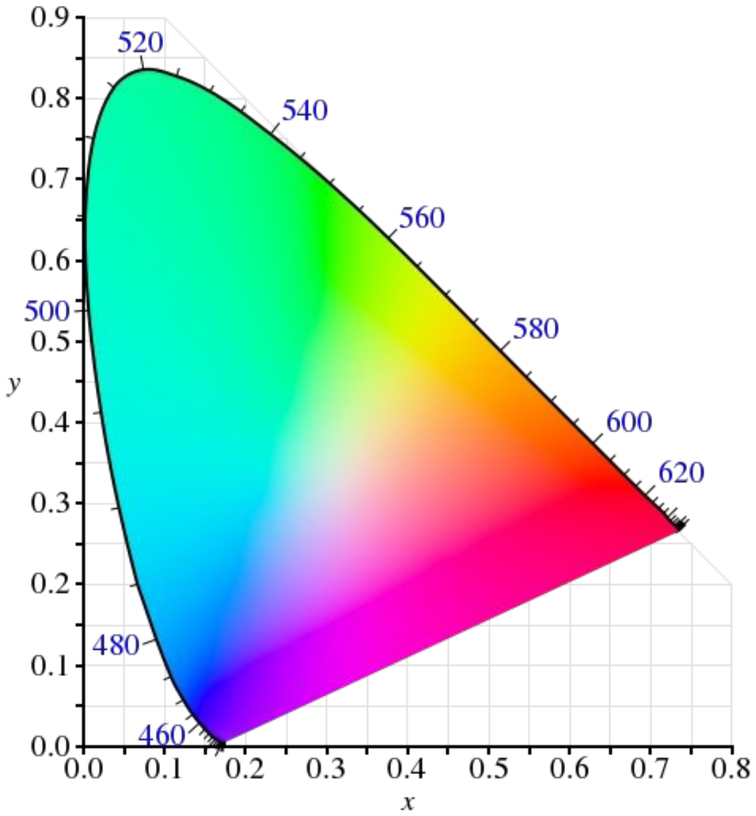
Now consider XYZ responses as curve in 3D space



Separating luminance, chromaticity

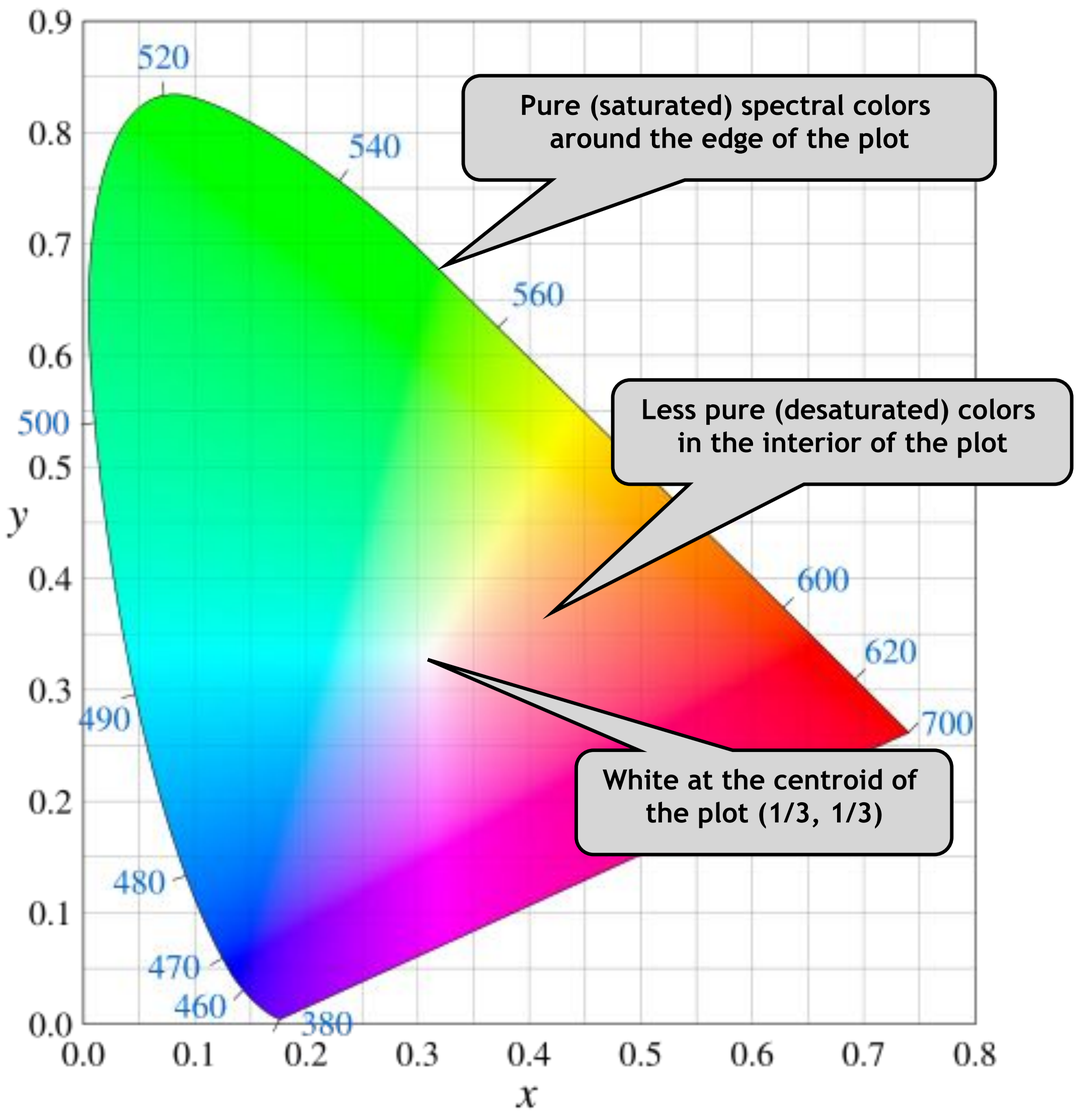
- **Luminance: Y**
- **Chromaticity: x, y, z, defined as**

$$x = \frac{X}{X+Y+Z}$$
$$y = \frac{Y}{X+Y+Z}$$
$$z = \frac{Z}{X+Y+Z}$$



- since $x + y + z = 1$, we only need to record two of the three
- usually choose x and y, leading to (x, y, Y) coords

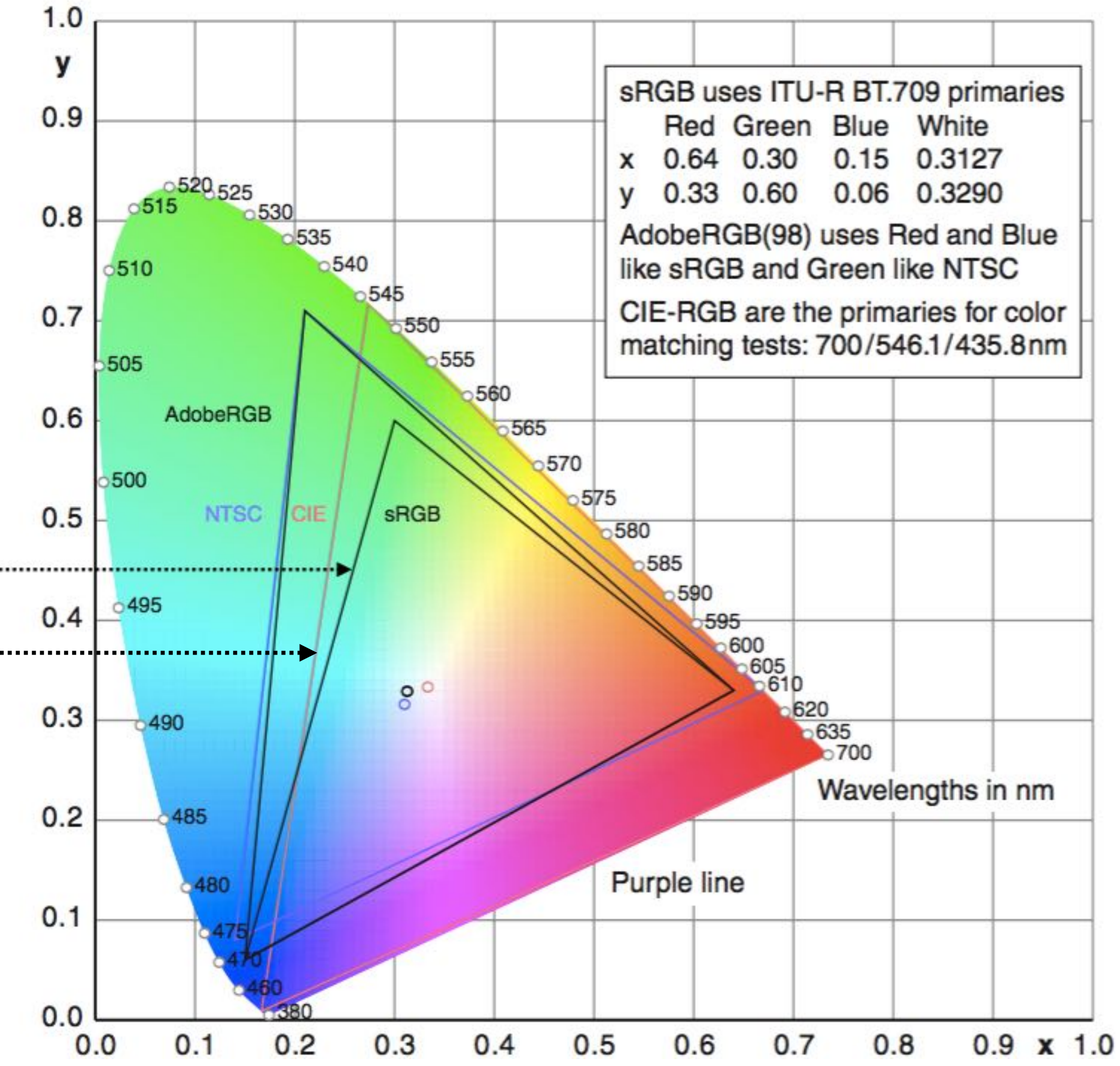
CIE chromaticity diagram



Color Gamut

sRGB is a common color space used throughout the internet

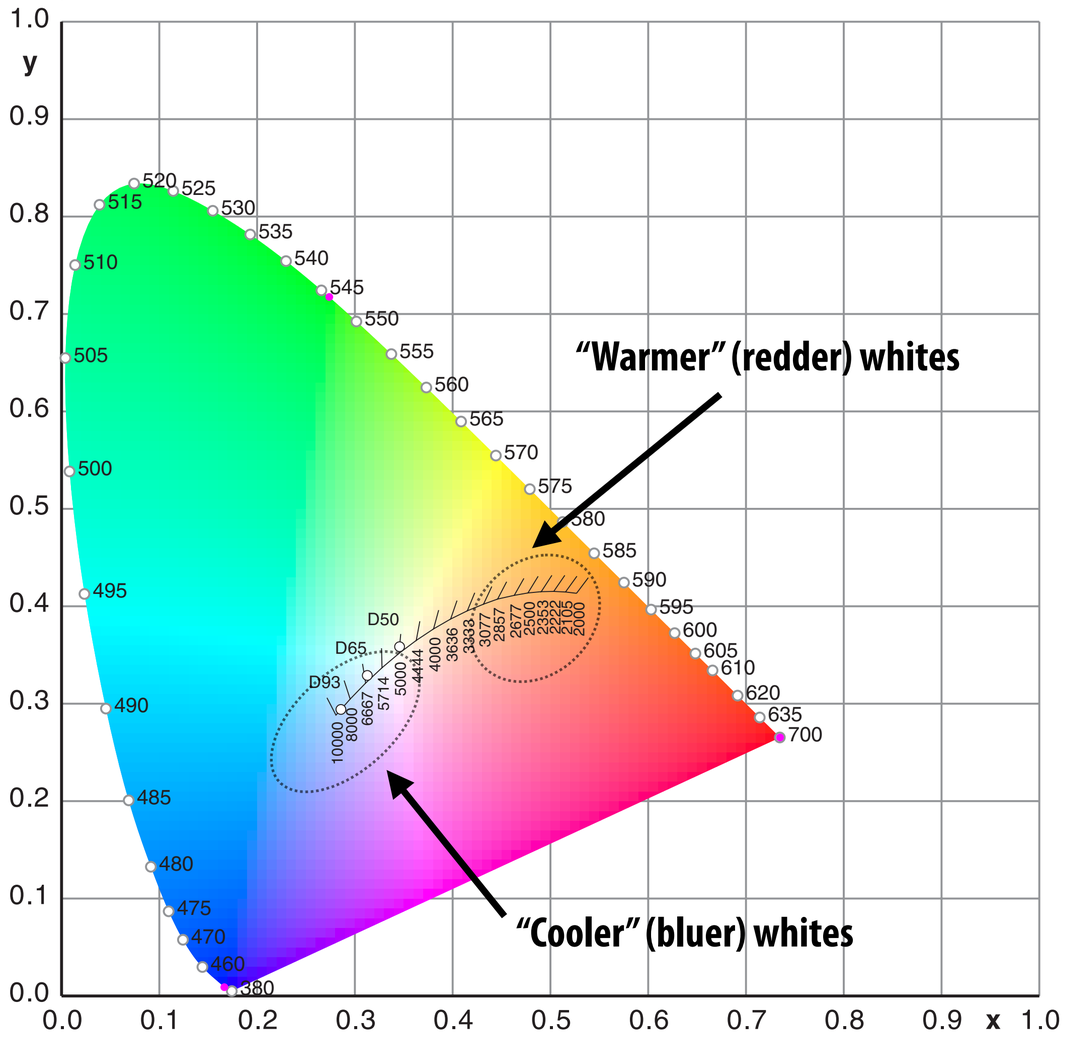
CIE RGB are the monochromatic primaries used for color matching tests described earlier



What is white?

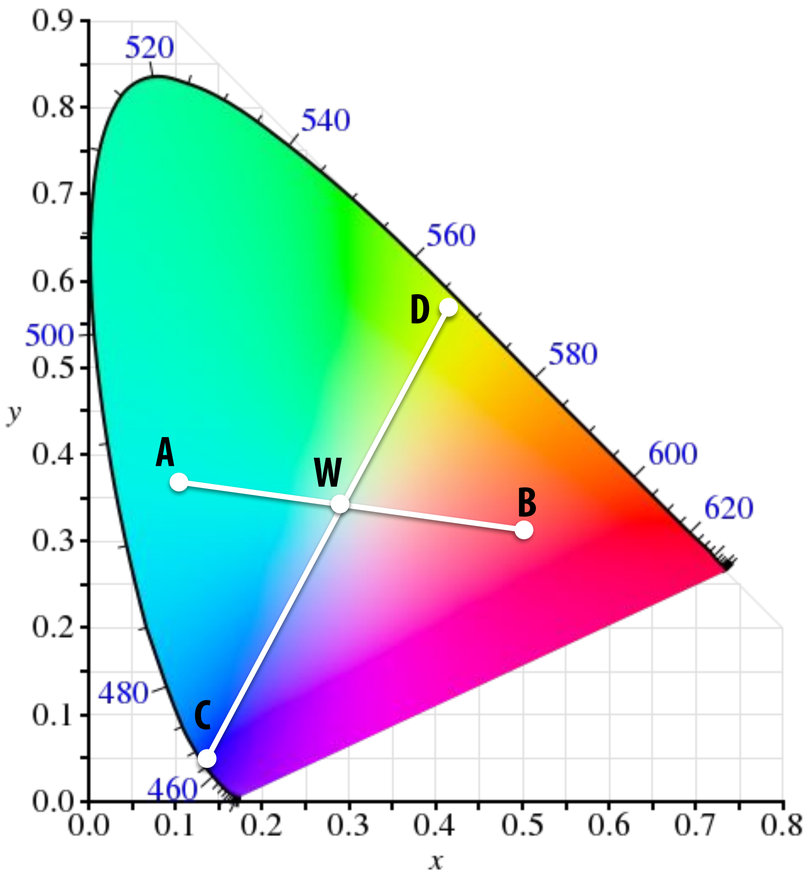
"White point" of a display is the X,Y,Z color space value of the point (1,1,1) in the color space defined by the display's primaries

"Warmth" of white light is often described by how chromaticity coordinates of (1,1,1) on display relate to that of spectrum emitted by black-body radiator of given temperature.



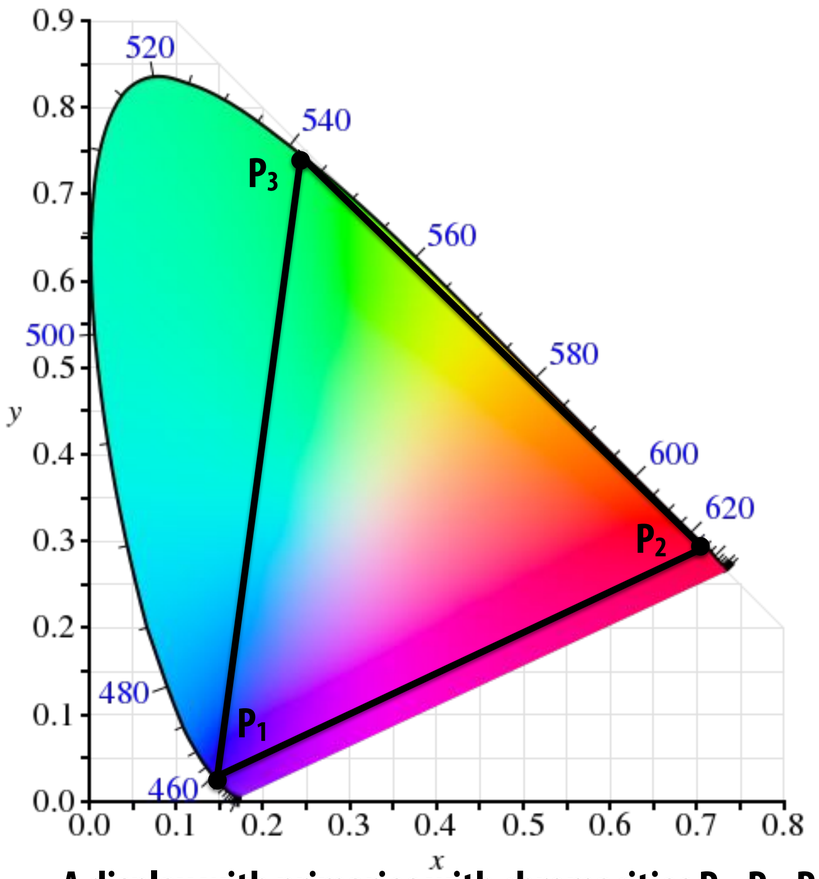
Uses of chromaticity diagram

Complementary colors are colors that can be mixed to form a designated white.



A and B and C and D are complementary with respect to reference white W

Demonstrate colors that fall out-of-gamut for a given choice of primaries

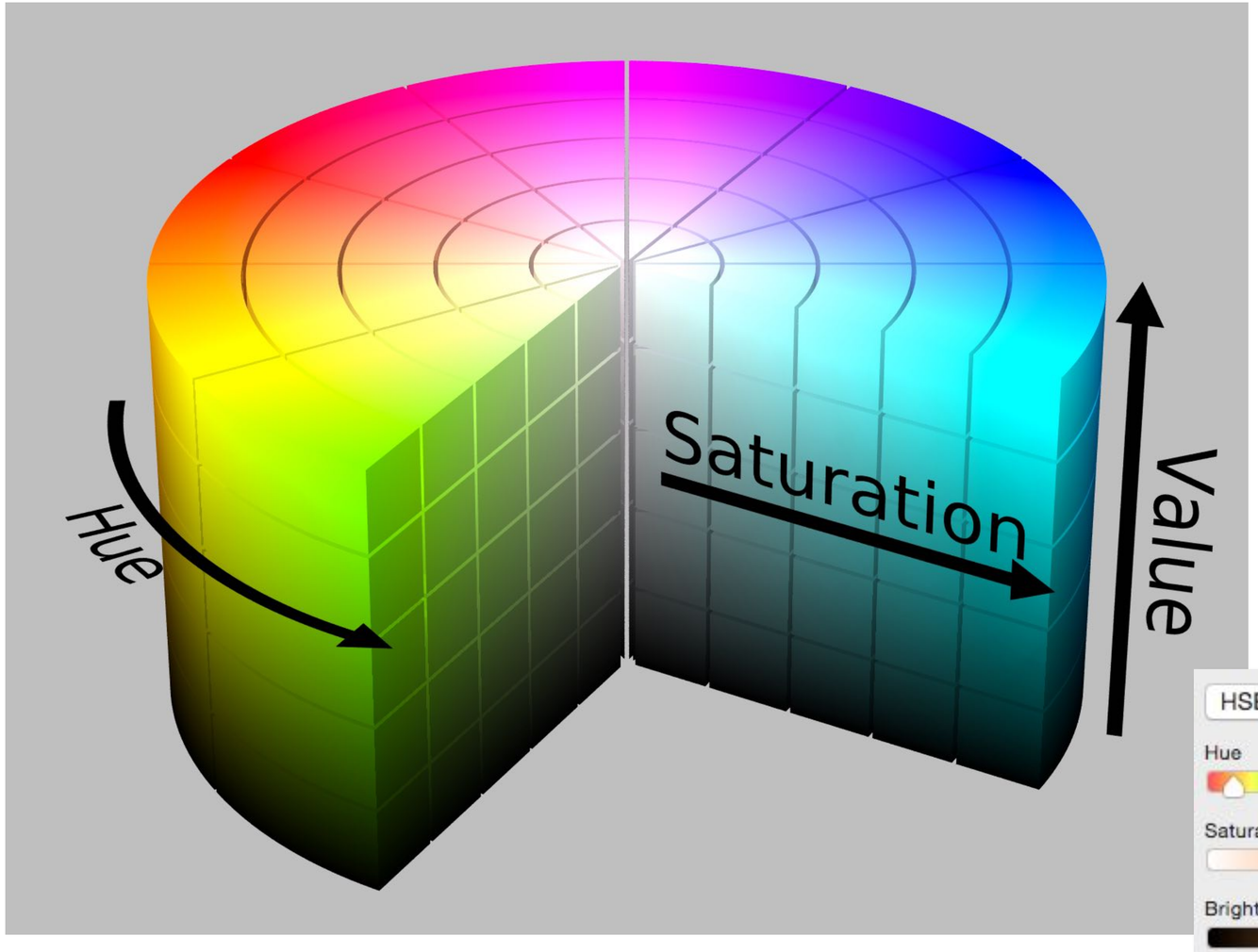


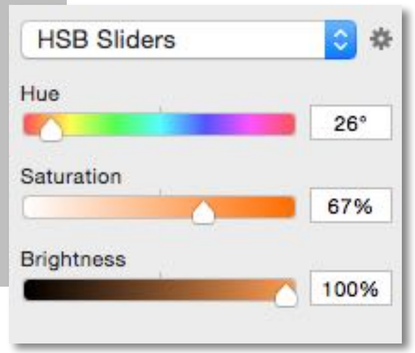
A display with primaries with chromacities P_1, P_2, P_3 can create colors that are combinations of these primaries (colors that fall within the triangle)

Perceptually Organized Color Spaces

HSV (hue-saturation-value)

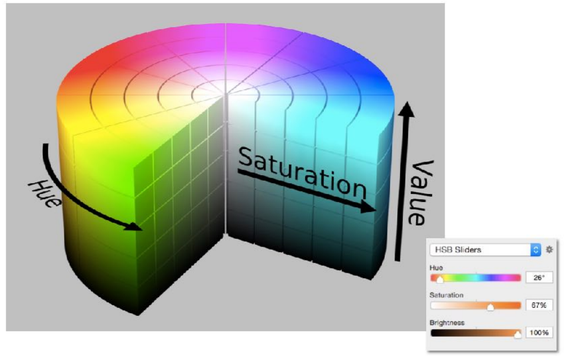
Axes of space correspond to natural notions of "characteristics" of color





Perceptual dimensions of color

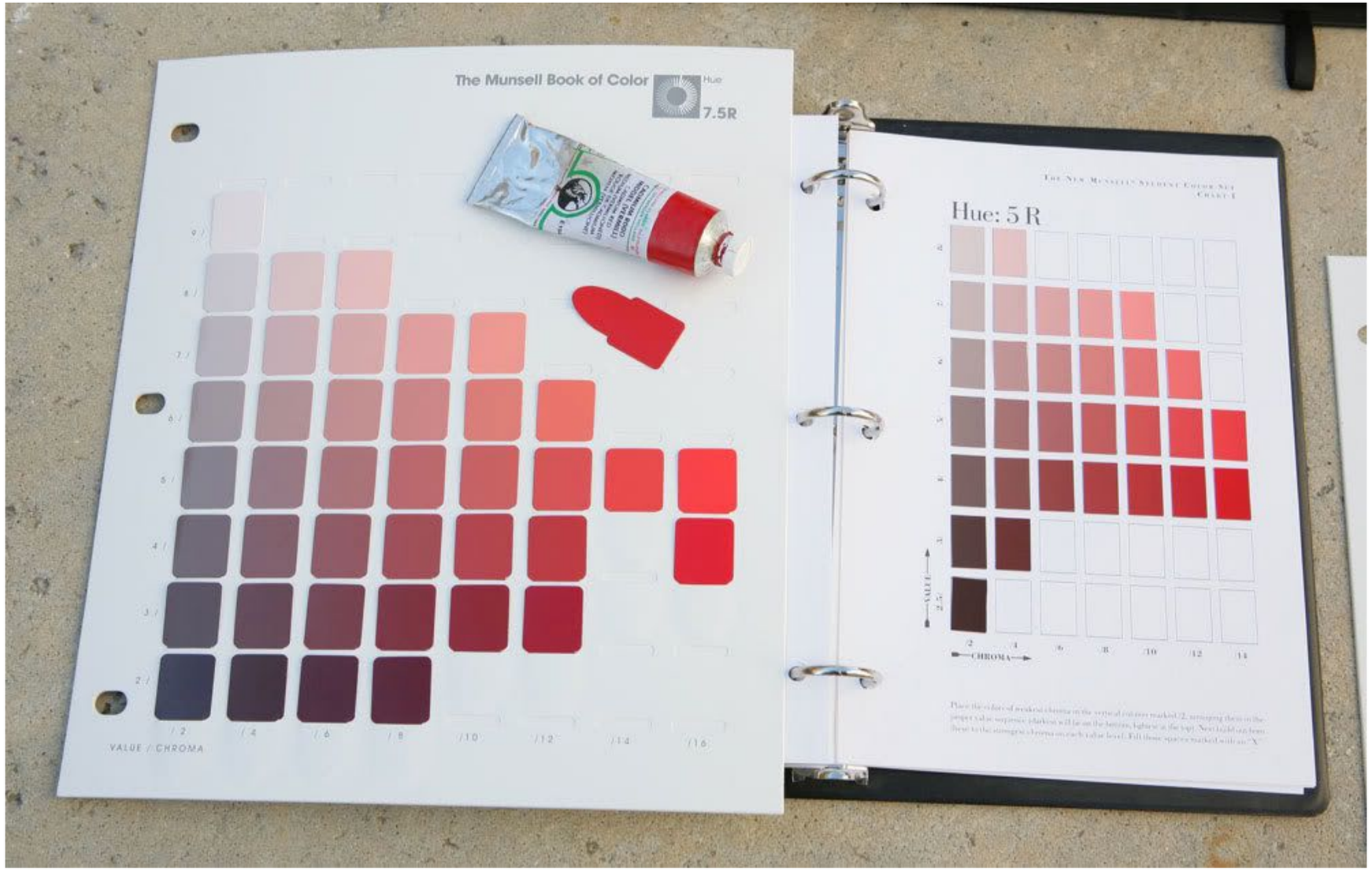
- Hue
  - the “kind” of color, regardless of attributes
  - colorimetric correlate: dominant wavelength
  - artist’s correlate: the chosen pigment color



- Saturation
  - the “colorfulness”
  - colorimetric correlate: purity
  - artist’s correlate: fraction of paint from the colored tube

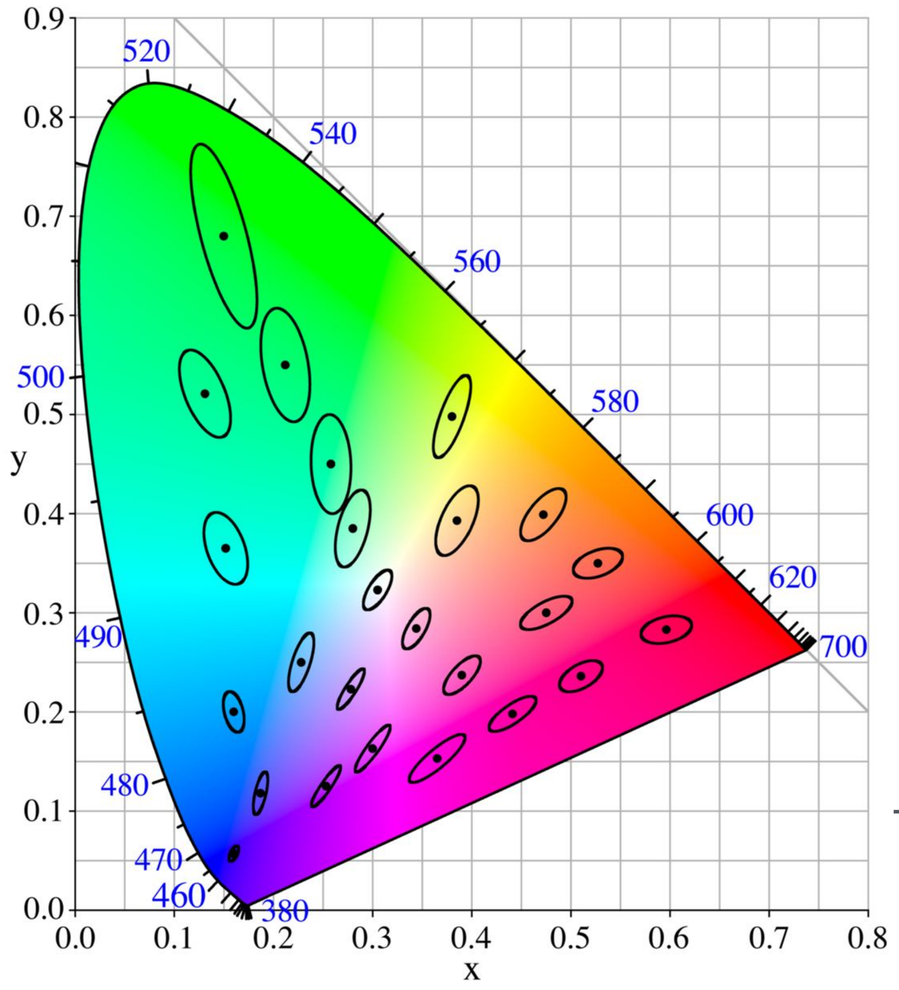
- Lightness (or value)
  - the overall amount of light
  - colorimetric correlate: luminance
  - artist’s correlate: tints are lighter, shades are darker

Munsell book of color



Swatch identified by three numbers: hue, value (lightness), and chroma (color purity)

Perceptual non-uniformity

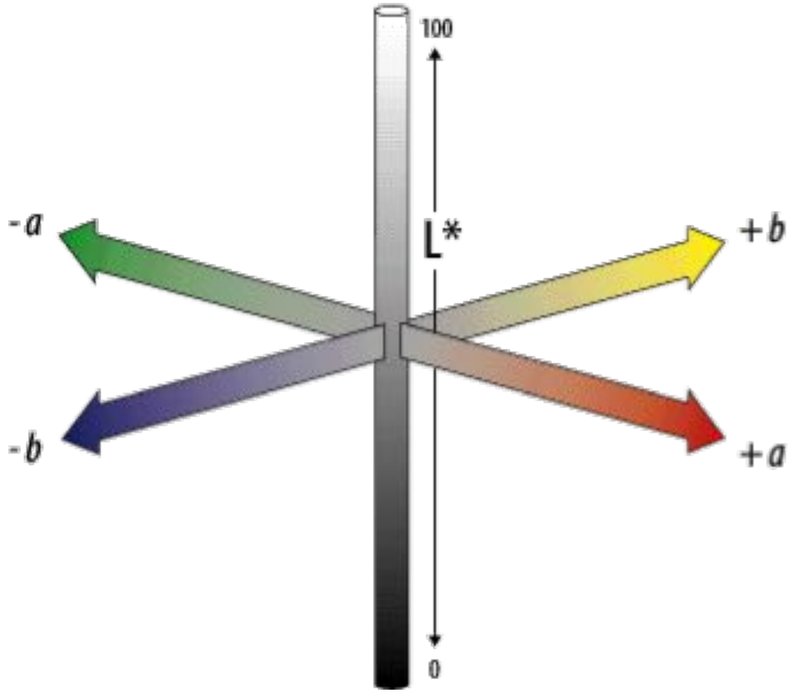


Wikipedia

- In the xy chromaticity diagram at left, MacAdam ellipses show regions of perceptually equivalent color (ellipses enlarged 10x)
- Must non-linearly warp the diagram to achieve uniform perceptual distances

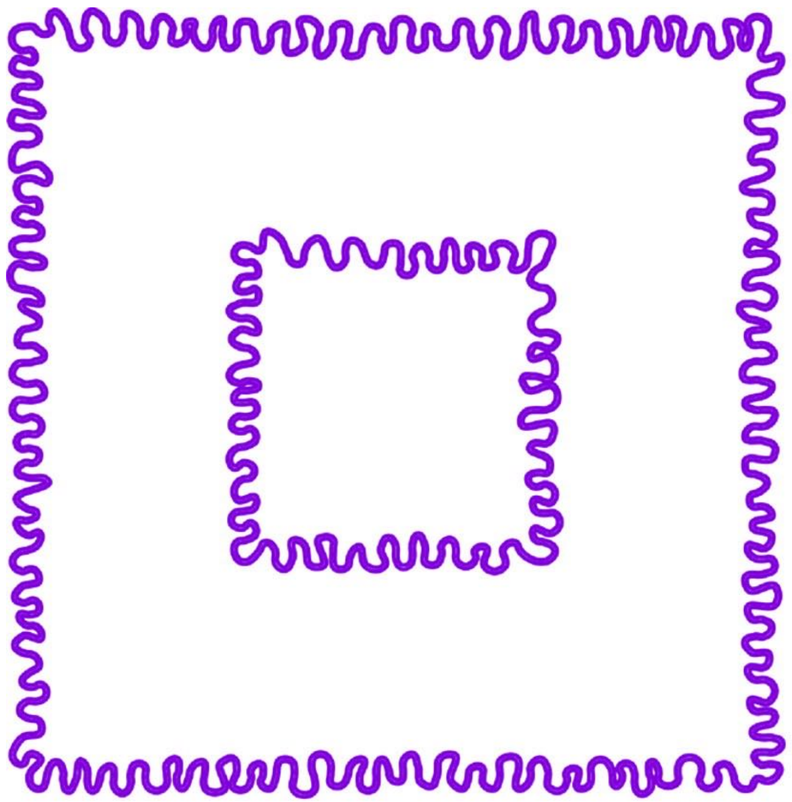
CIELAB Space (L*a*b*)

- A commonly used color space that strives for perceptual uniformity
  - L* is lightness
  - a* and b* are color-opponent pairs
    - a* is red-green, and b* is blue-yellow
  - A gamma transform is used for warping because perceived brightness is proportional to scene intensity$^{\gamma}$, where $\gamma \approx 1/3$



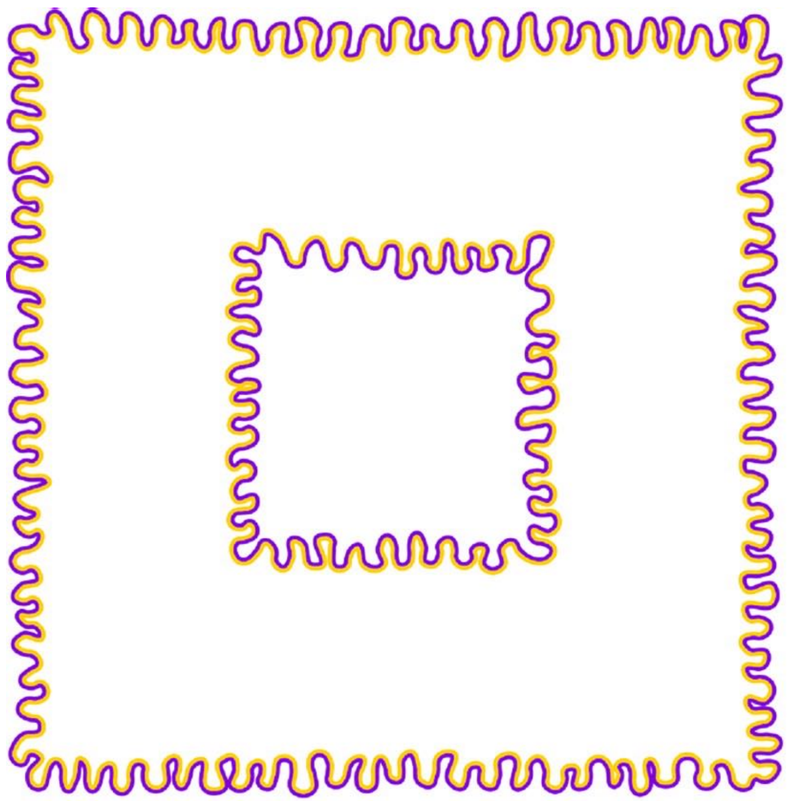
How we perceive color can be surprising

Watercolor illusion



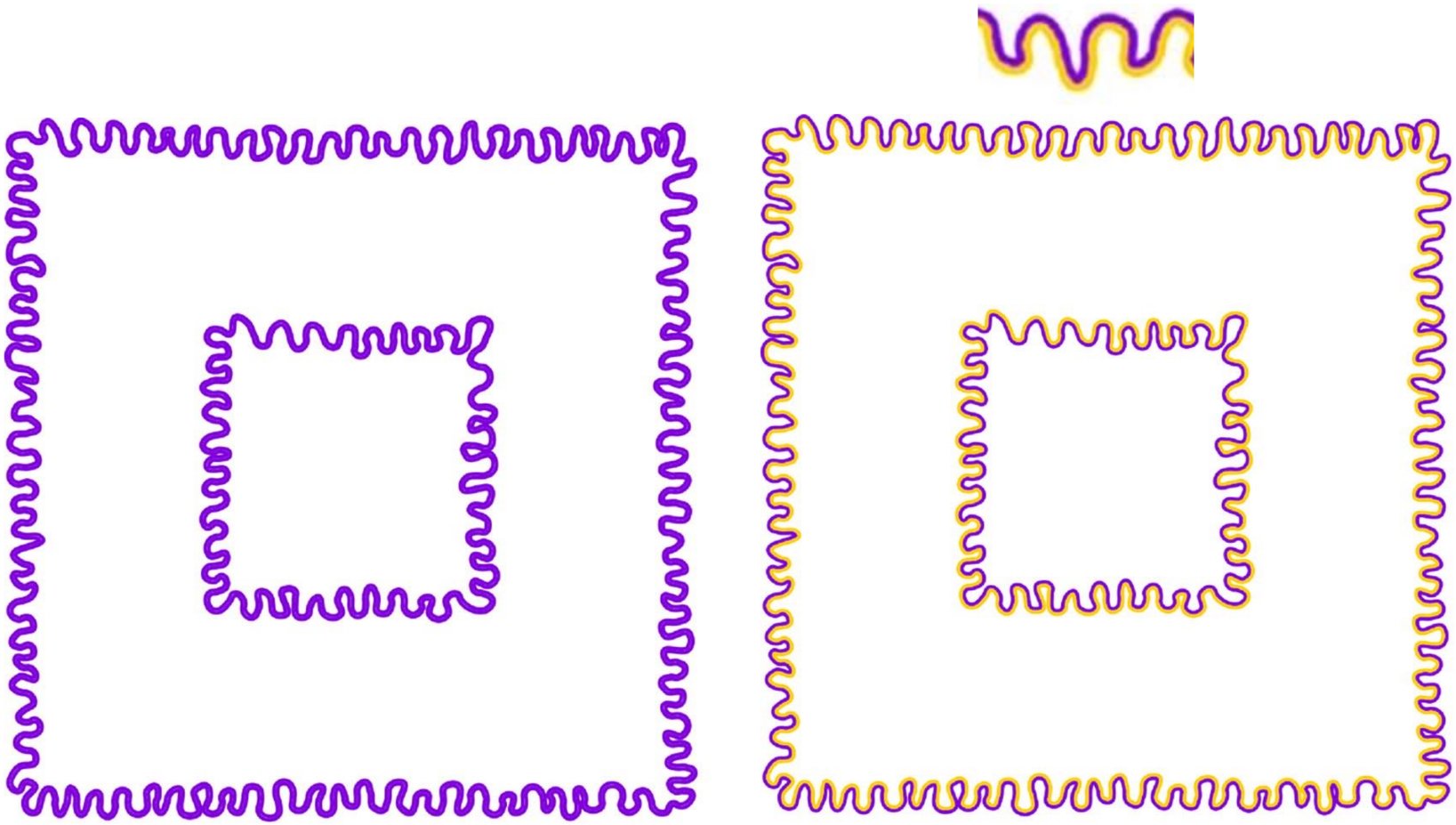
Pinna & Tanca, *JOV*, 2008

Watercolor illusion



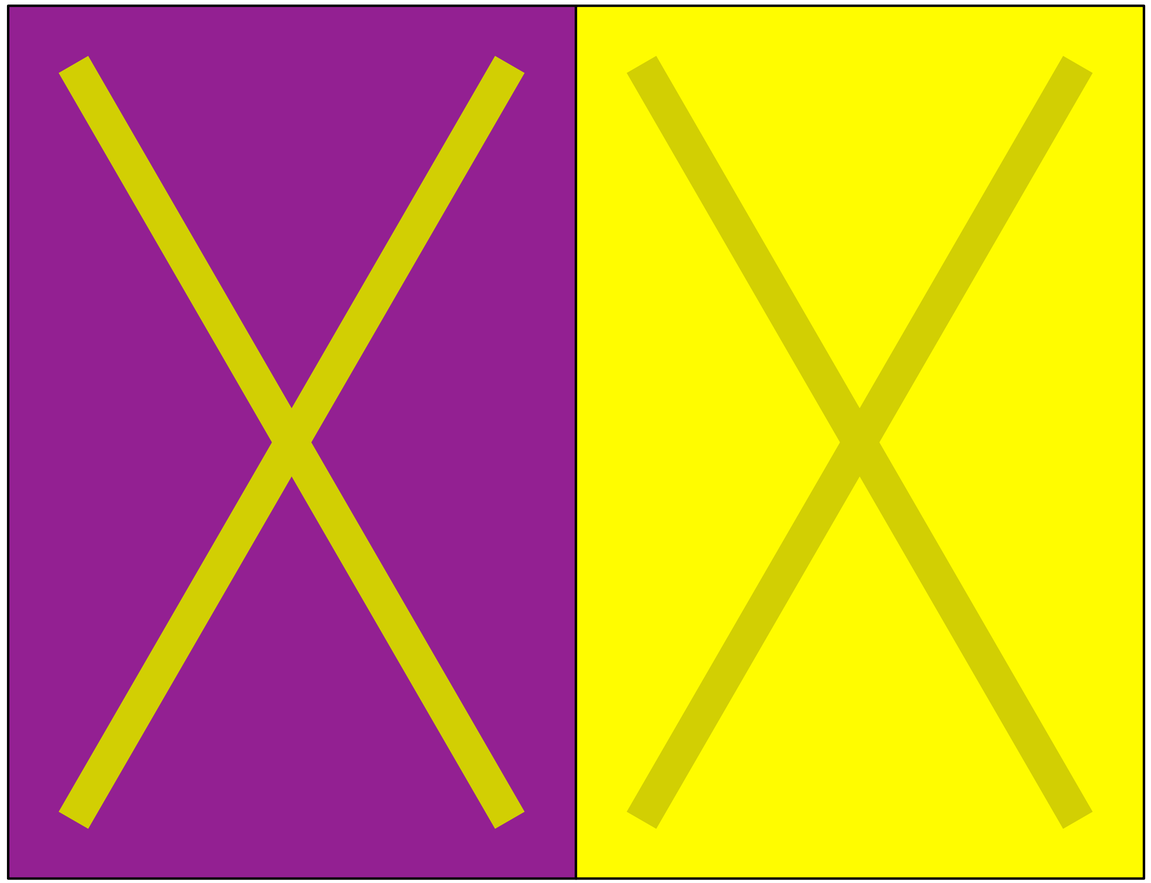
Pinna & Tanca, *JOV*, 2008

Watercolor illusion

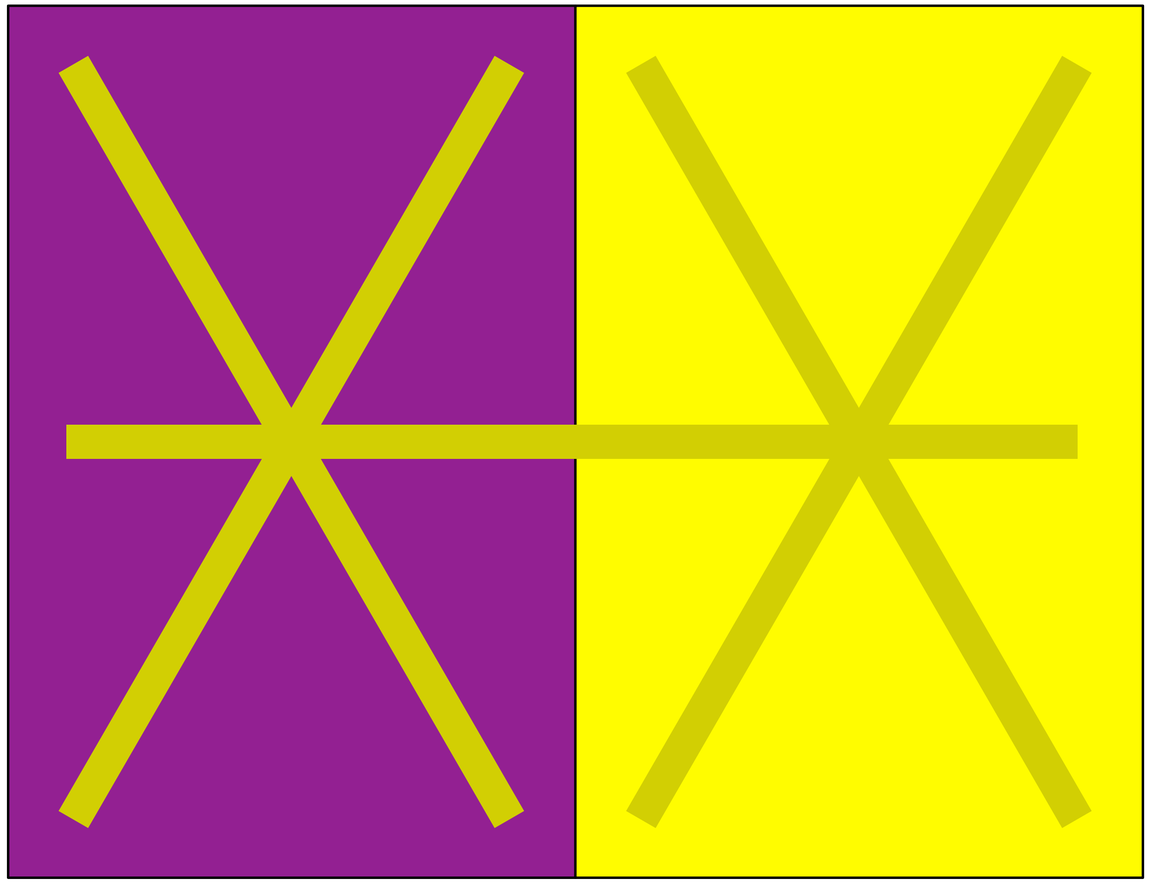


Pinna & Tanca, *JOV*, 2008

Which "X" is darker?



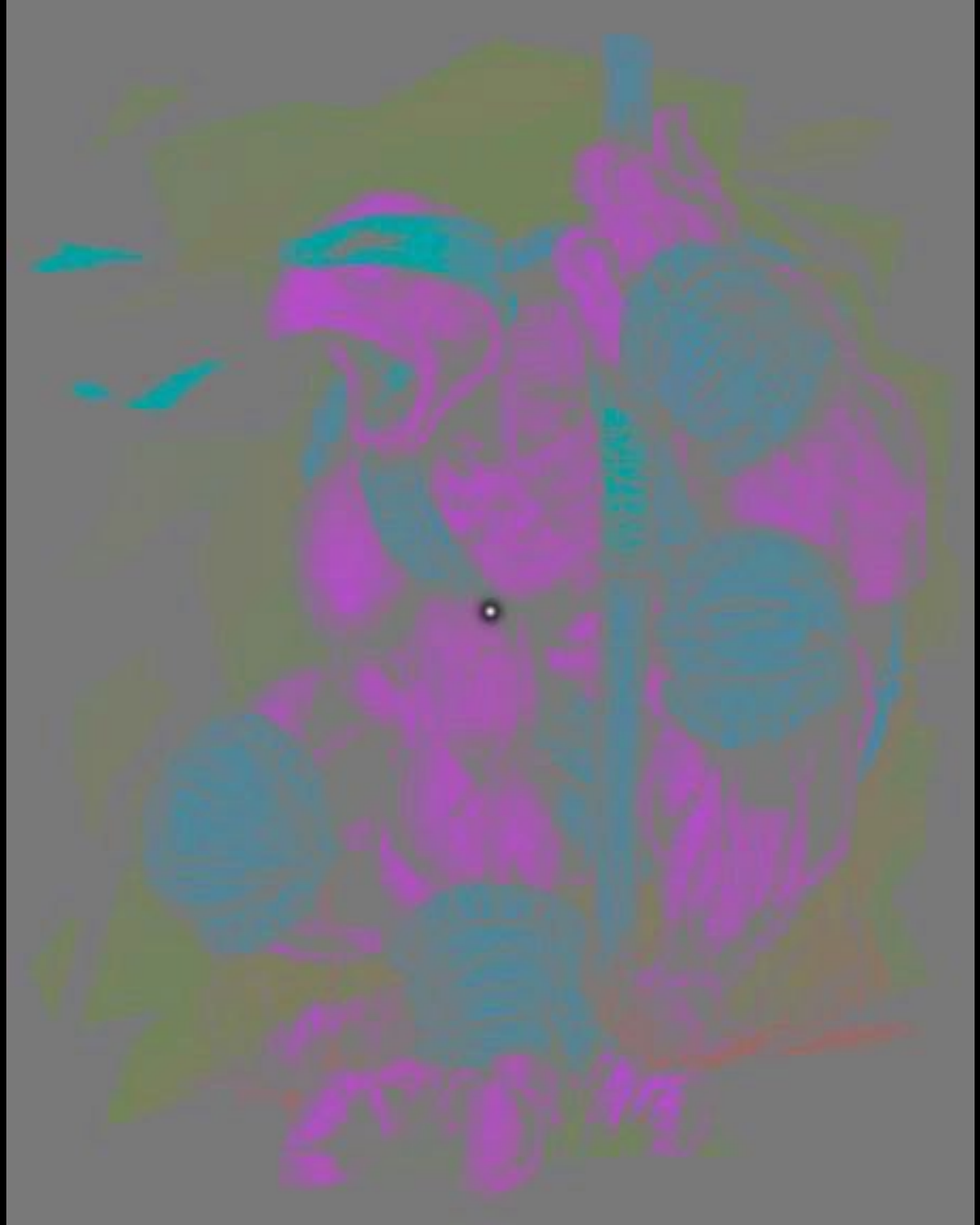
Which "X" is darker?



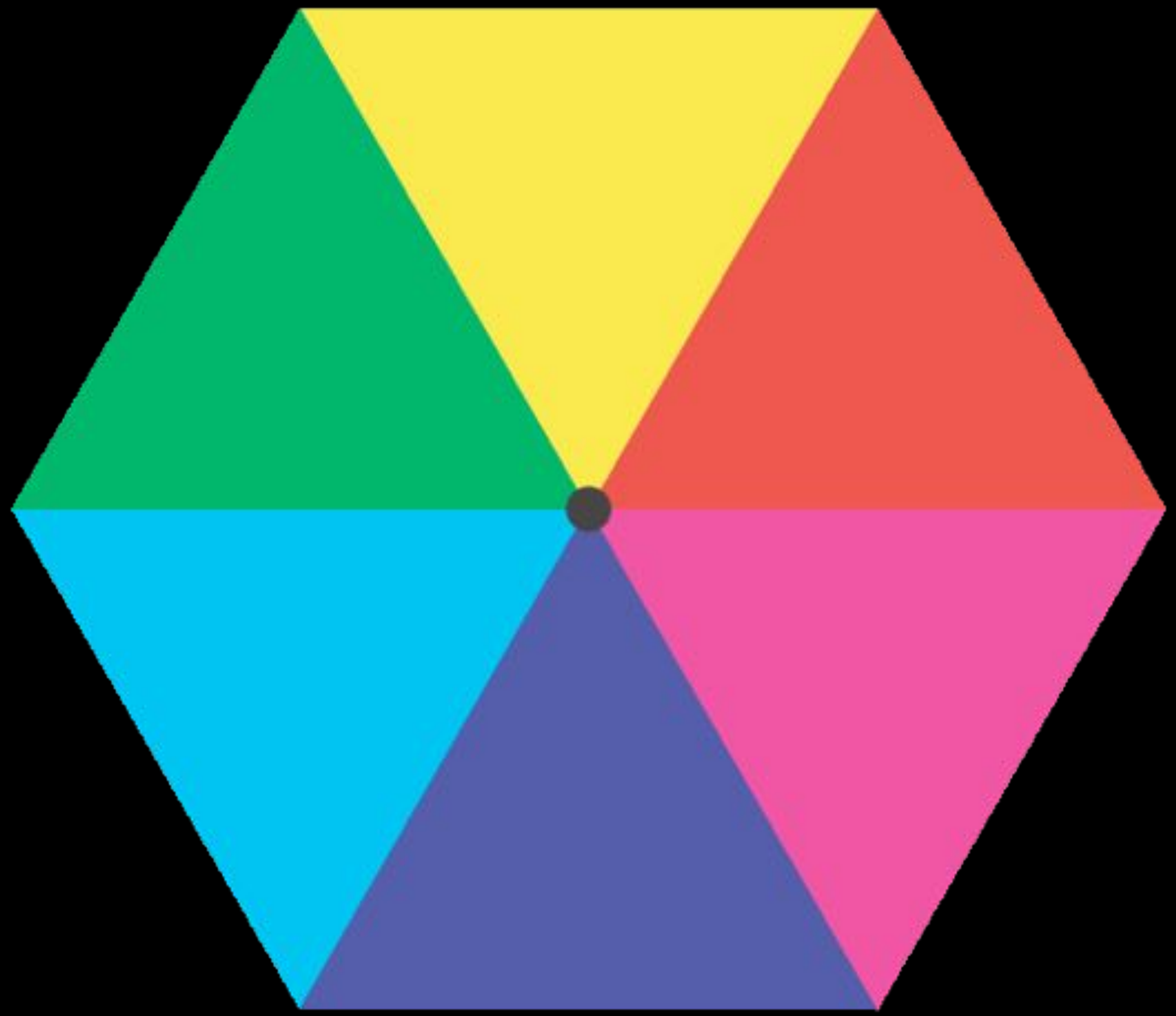
keep staring at the black dot.

johnsadowski.com

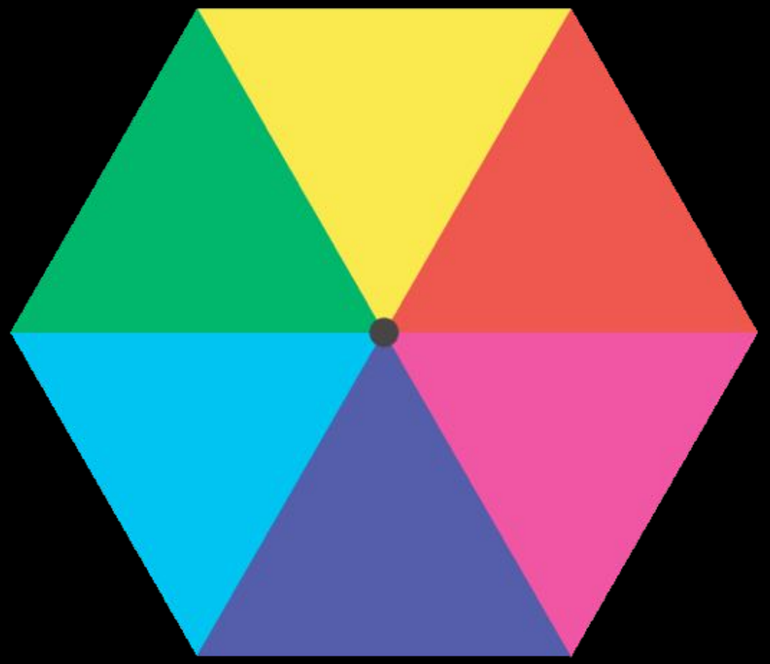
Adapt



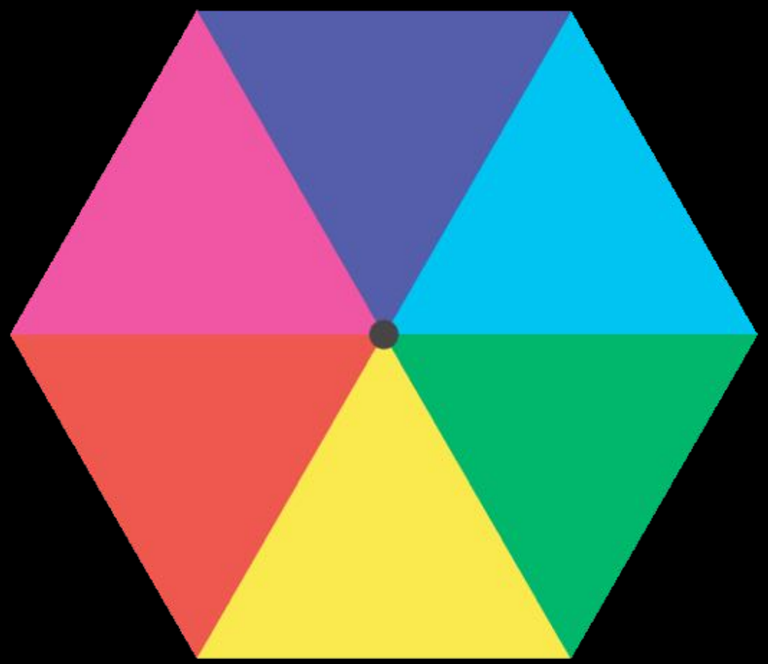
Adapt



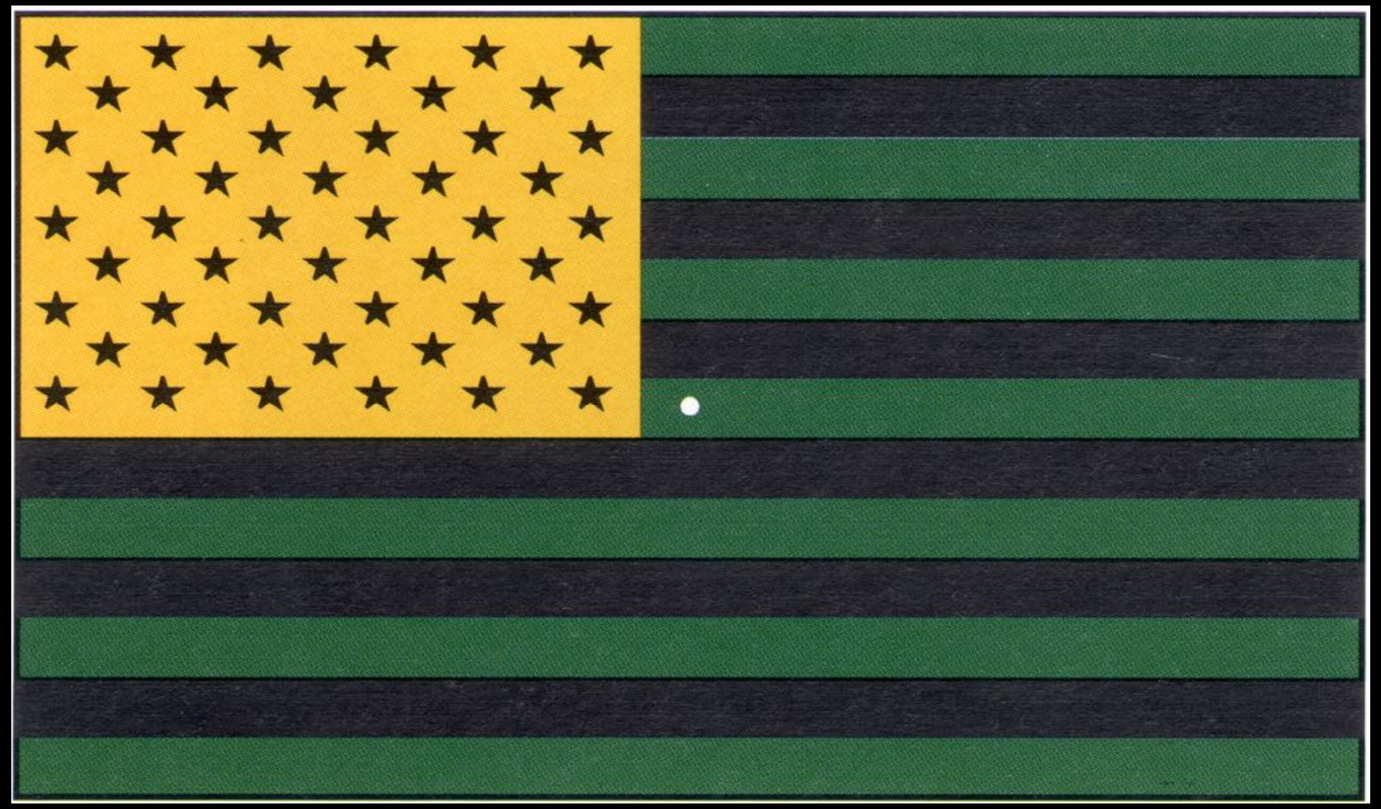
[Slide left blank.. Students should see afterimage.]



Image

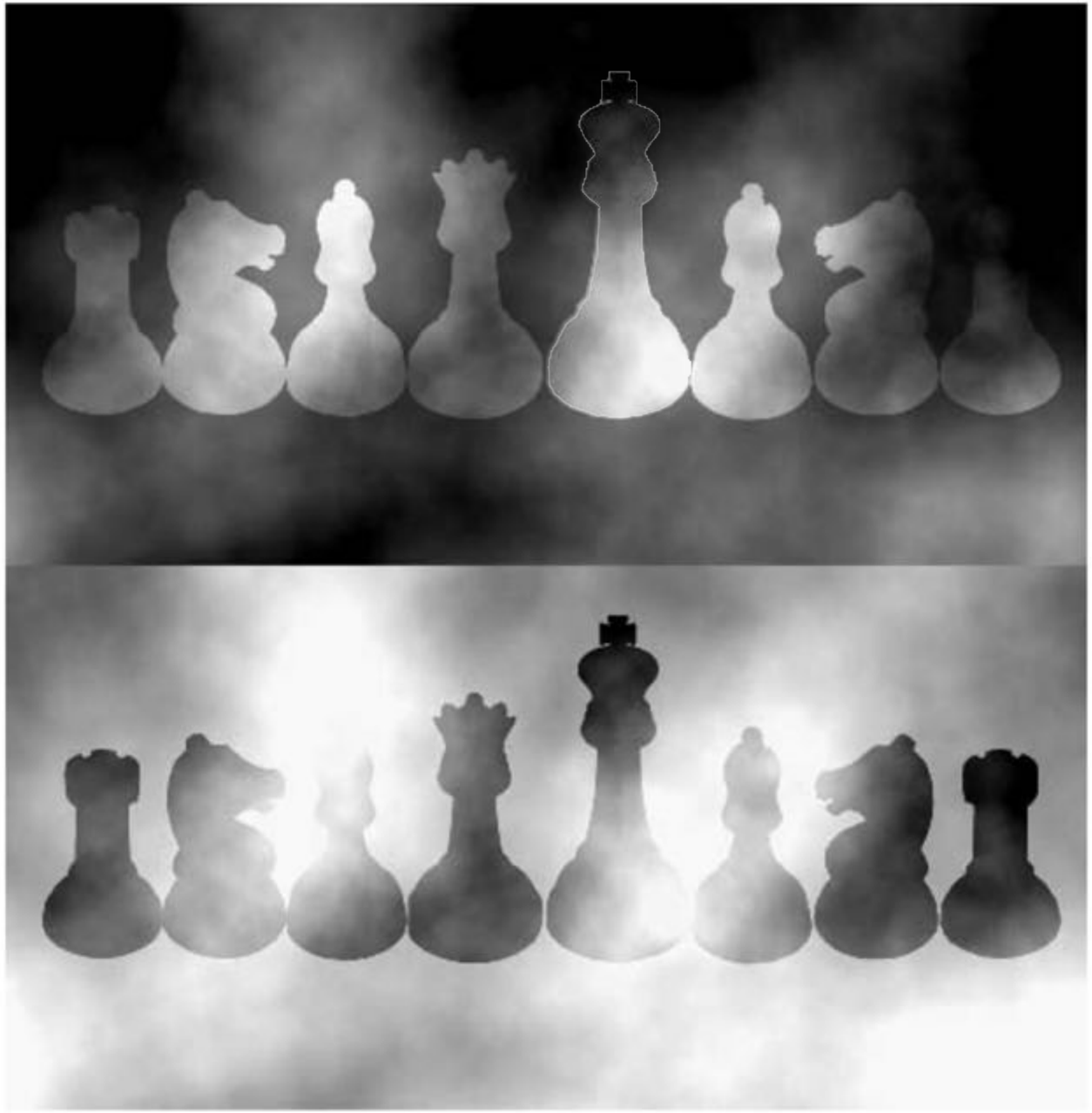


Afterimage

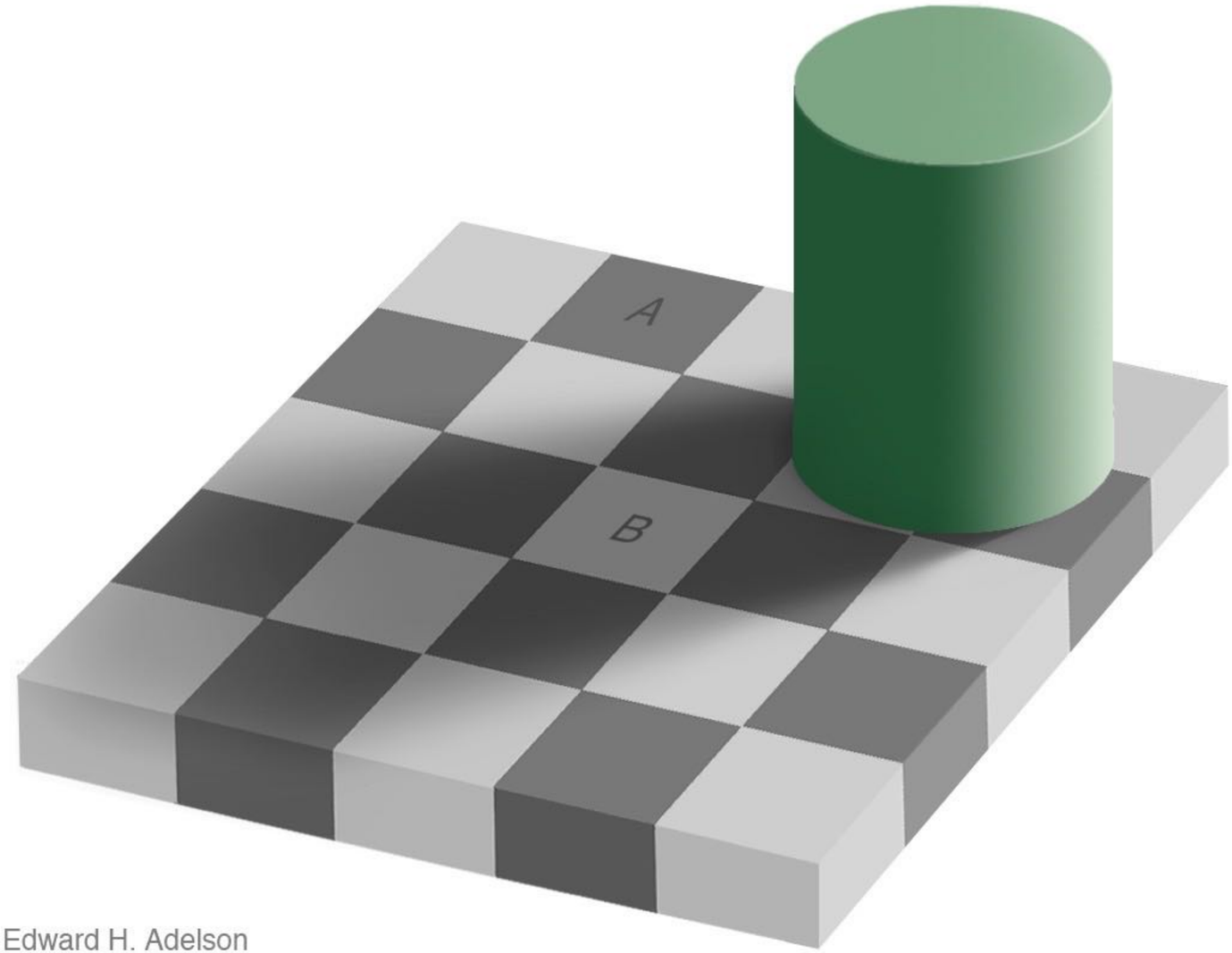


[Slide left blank.. Students should see afterimage.]

Even simple judgments – such as lightness - depend on brain processing (Anderson and Winawer, Nature, 2005)

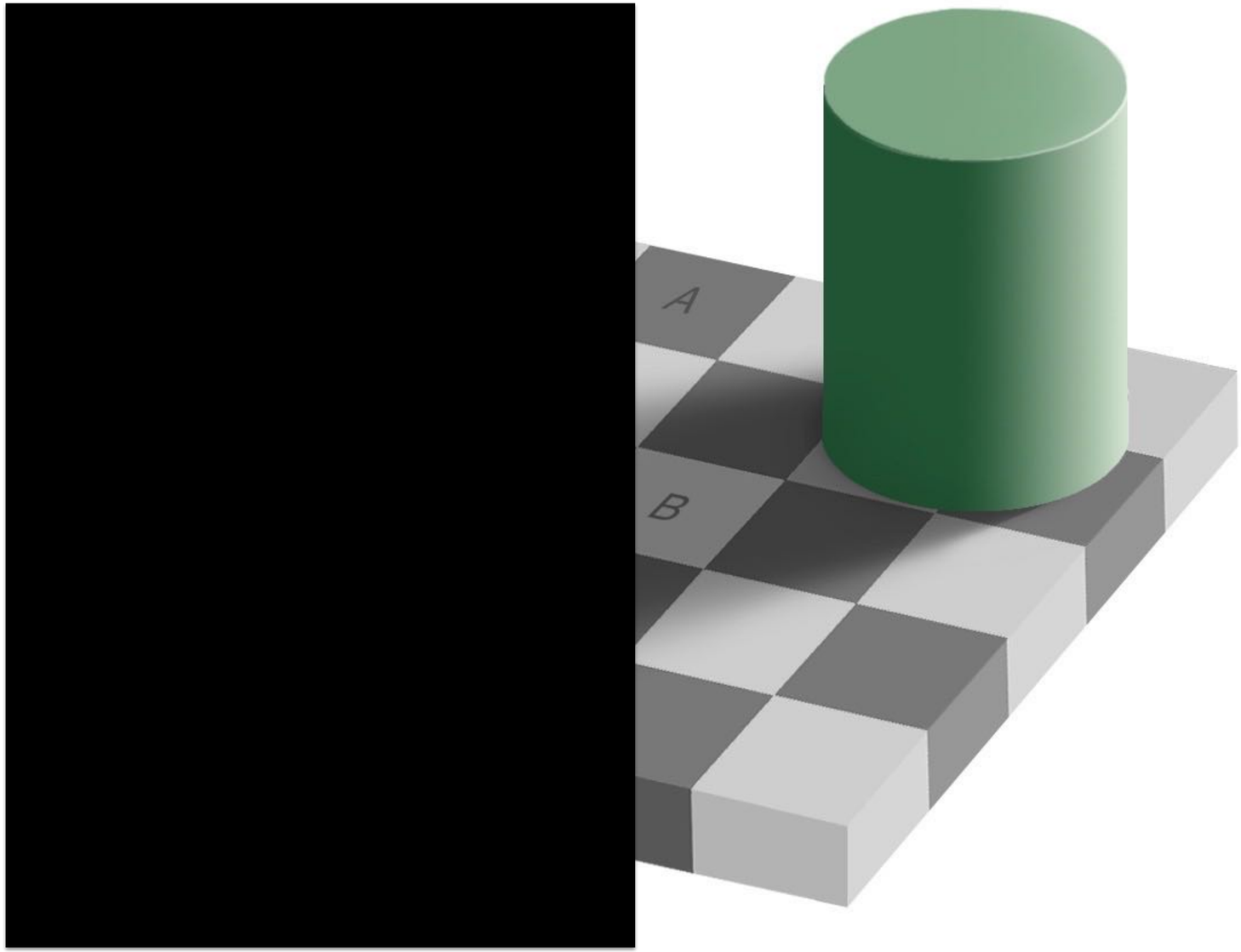


Everything is relative



Edward H. Adelson

Everything is relative



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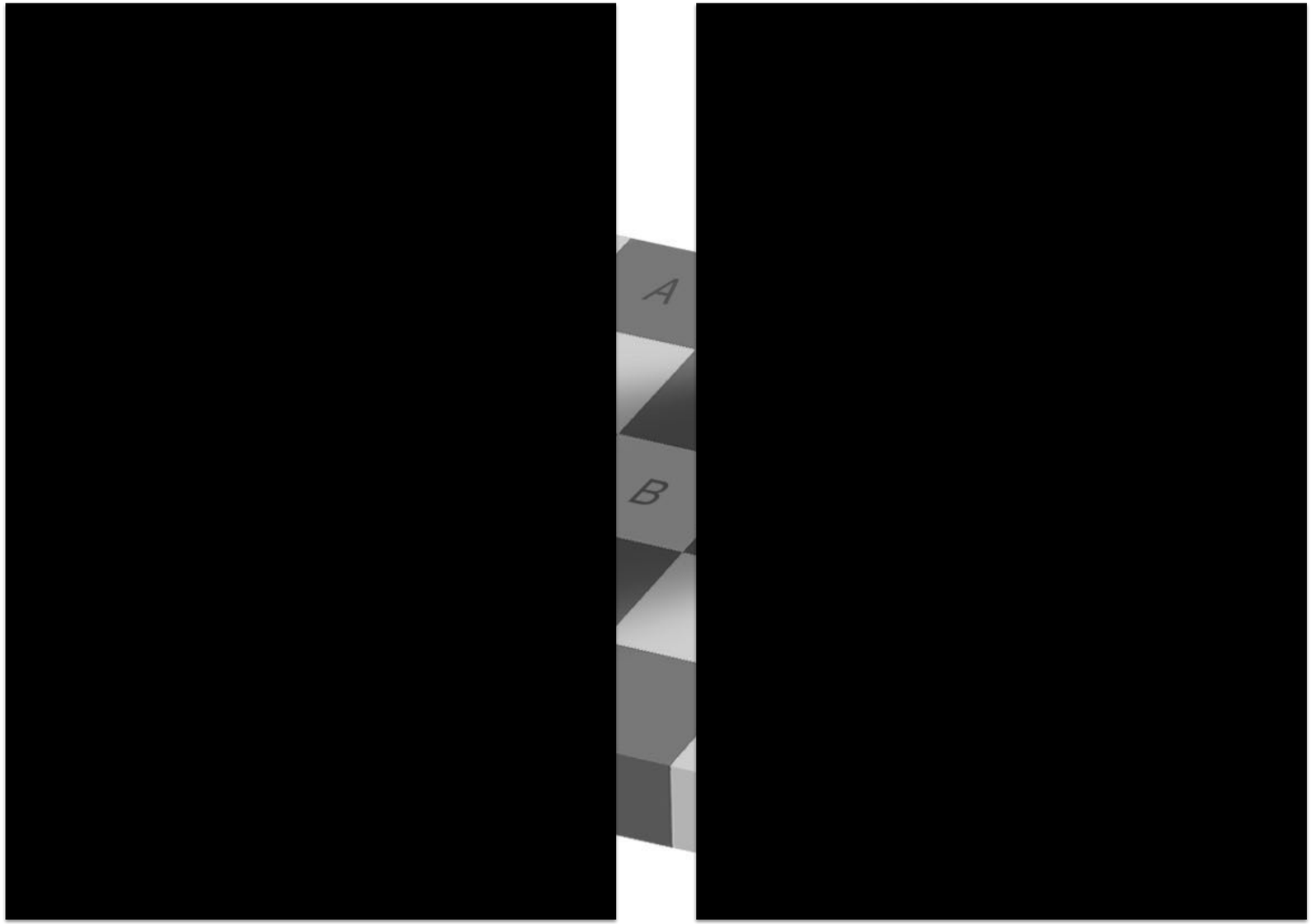

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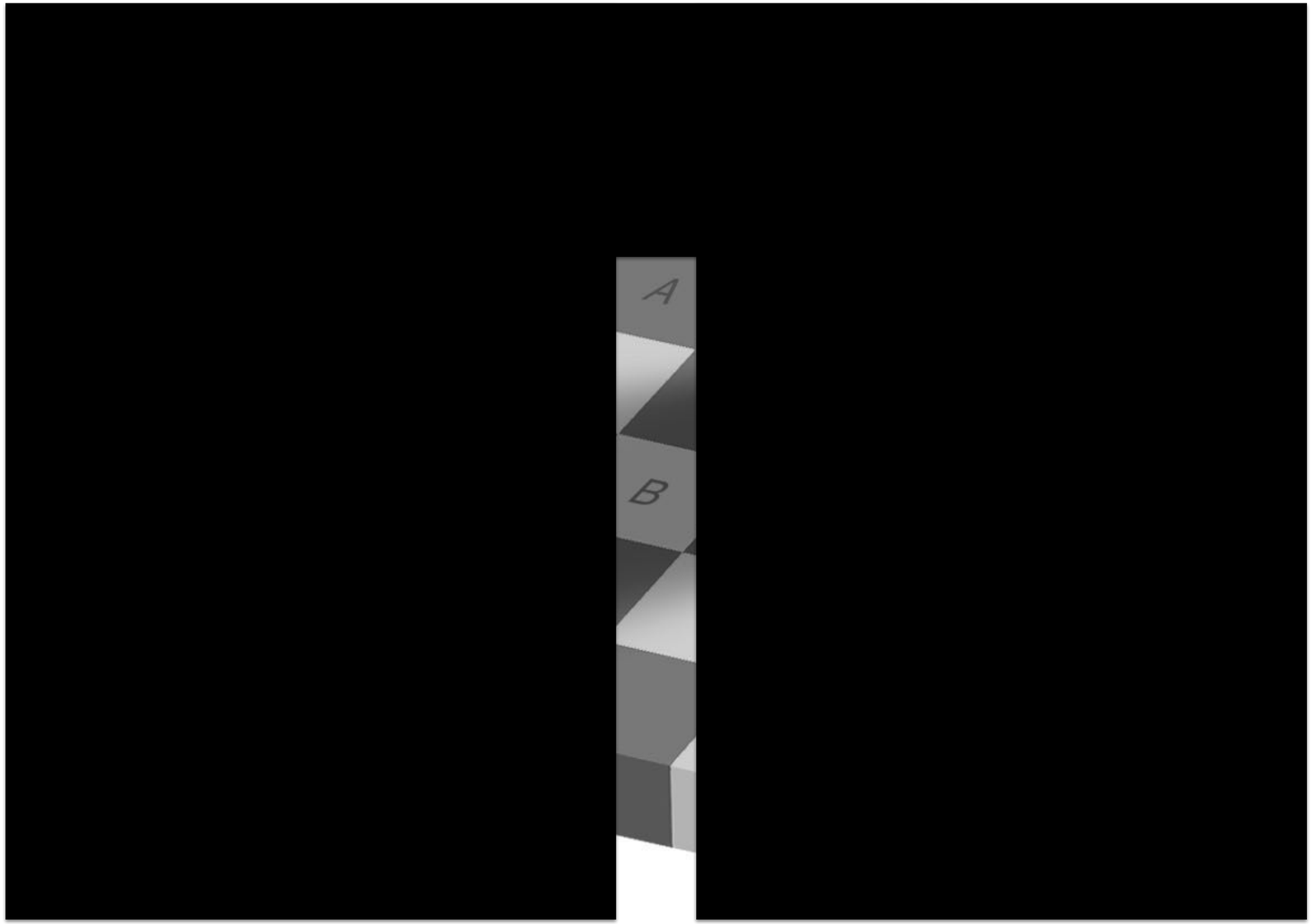

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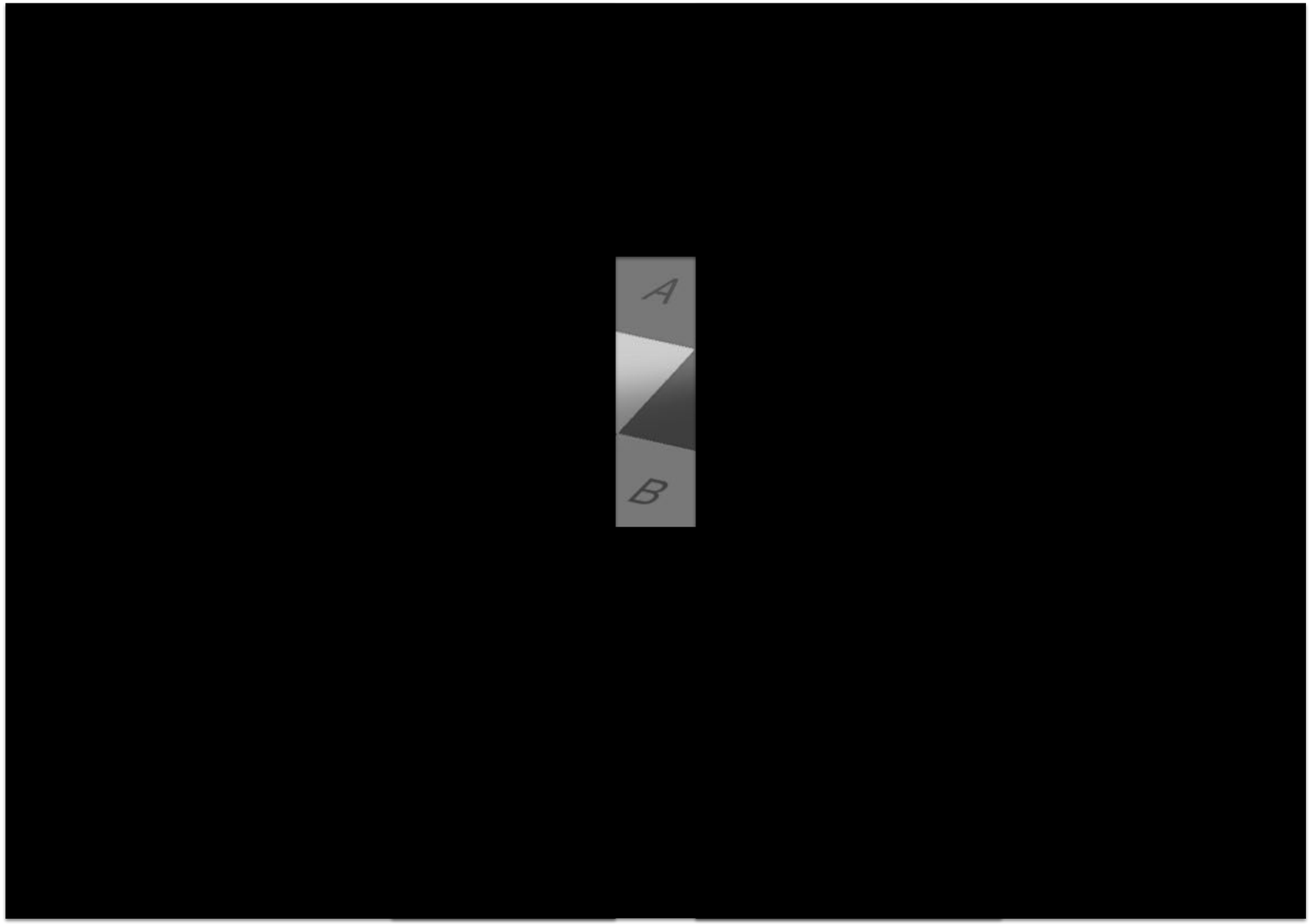

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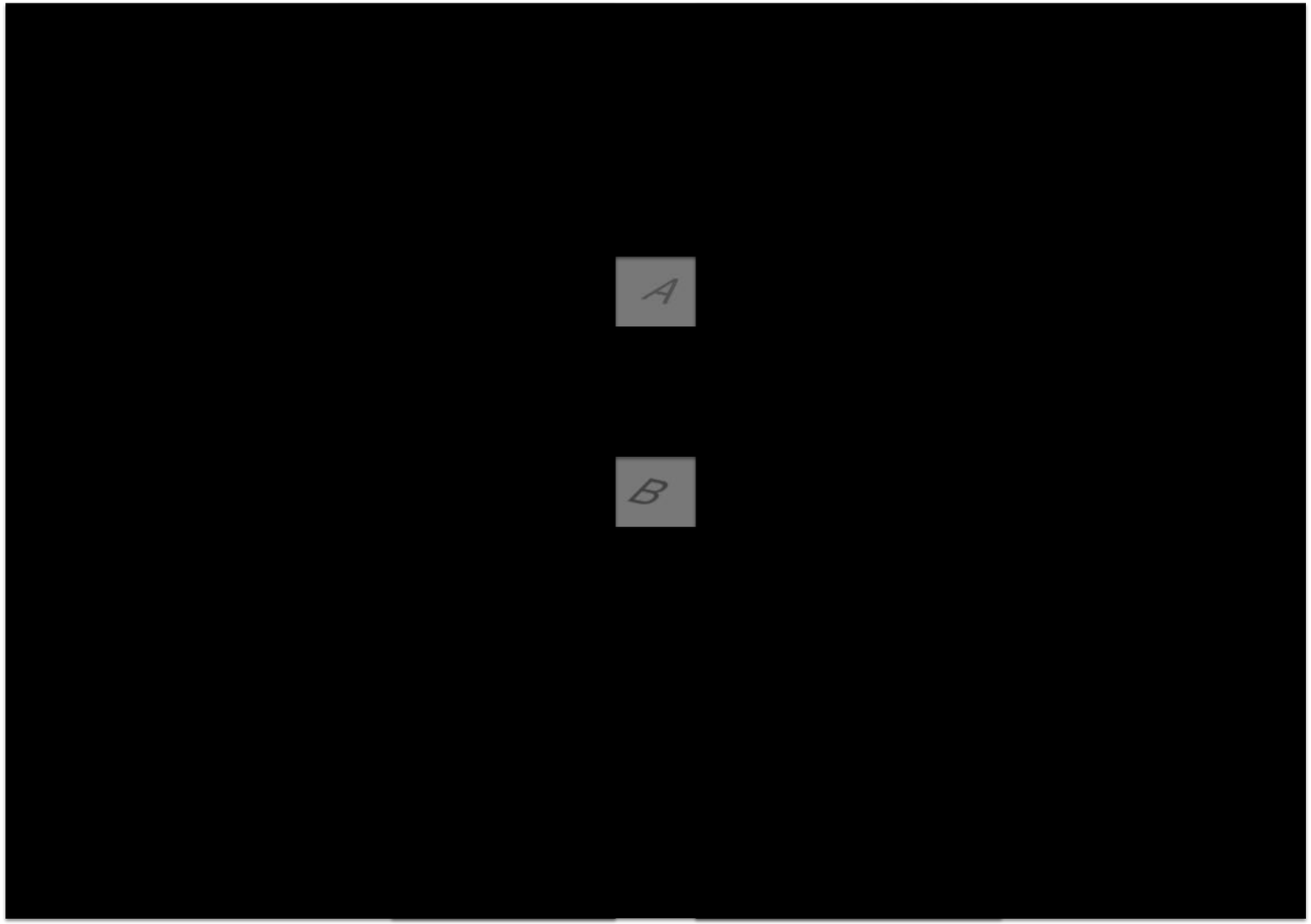

Things to remember

- Physics of Light
  - Spectral power distribution (SPD)
  - Superposition (linearity)
- Tristimulus theory of color
  - Spectral response of human cone cells (S, M, L)
  - Metamers - different SPDs with the same perceived color
  - Color reproduction mathematics
  - Color matching experiment, per-wavelength matching functions
- Color spaces
  - CIE RGB, XYZ, xy chromaticity, LAB, HSV
  - Gamut

Acknowledgements

- Thanks and credit for slides to Ren Ng, Steve Marschner, Brian Wandell, Marc Levoy, Katherine Breeden, Austin Roorda, Keenan Crane, James O'Brien