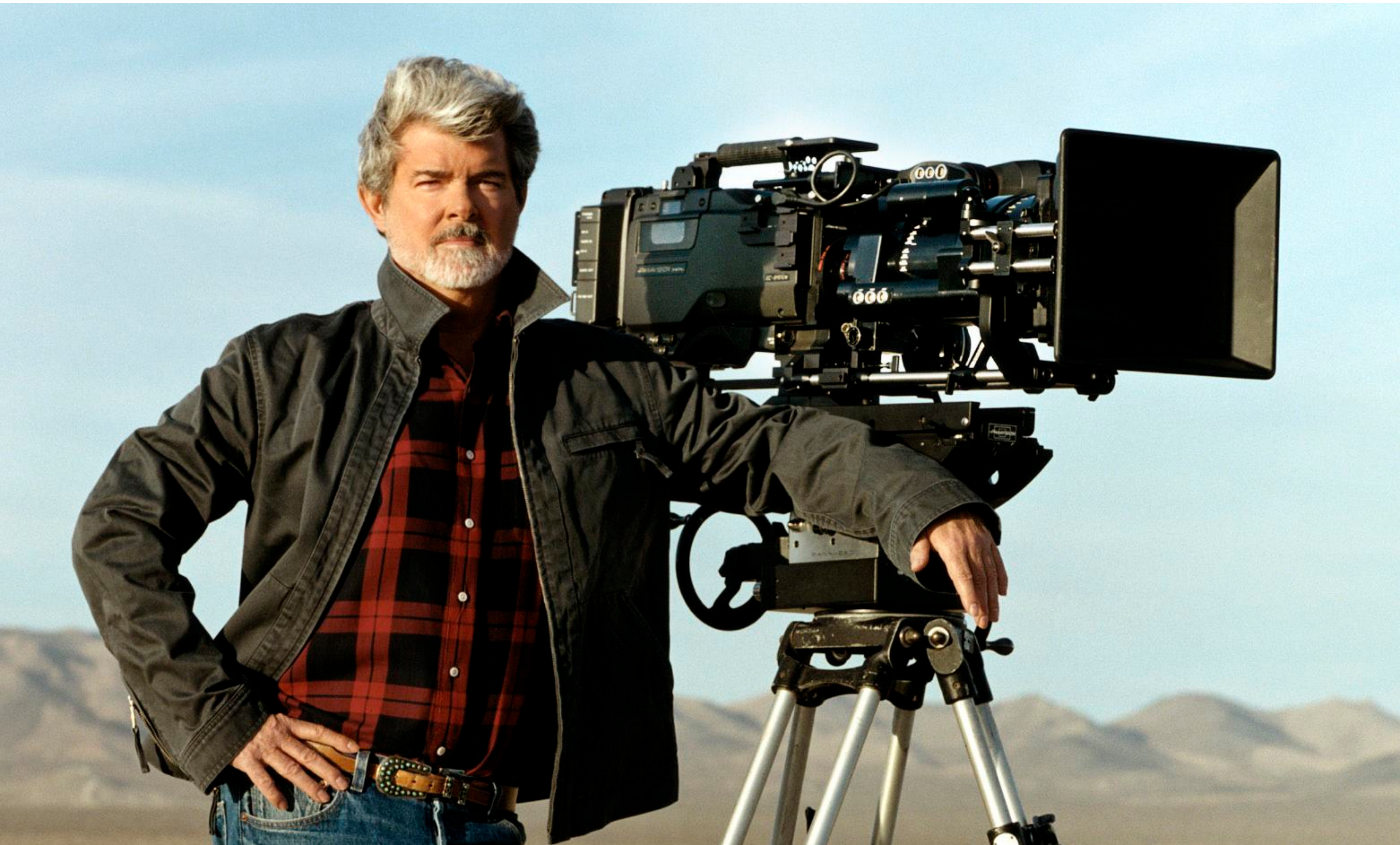


# Cameras and Lenses



**Image credit: Canon**





**"Tangerine" (2015)  
Shot with iPhone 5**

# Today

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## Camera basics

- **Lenses**
- **Exposure**
- **Depth of Field**
- **Light field cameras**

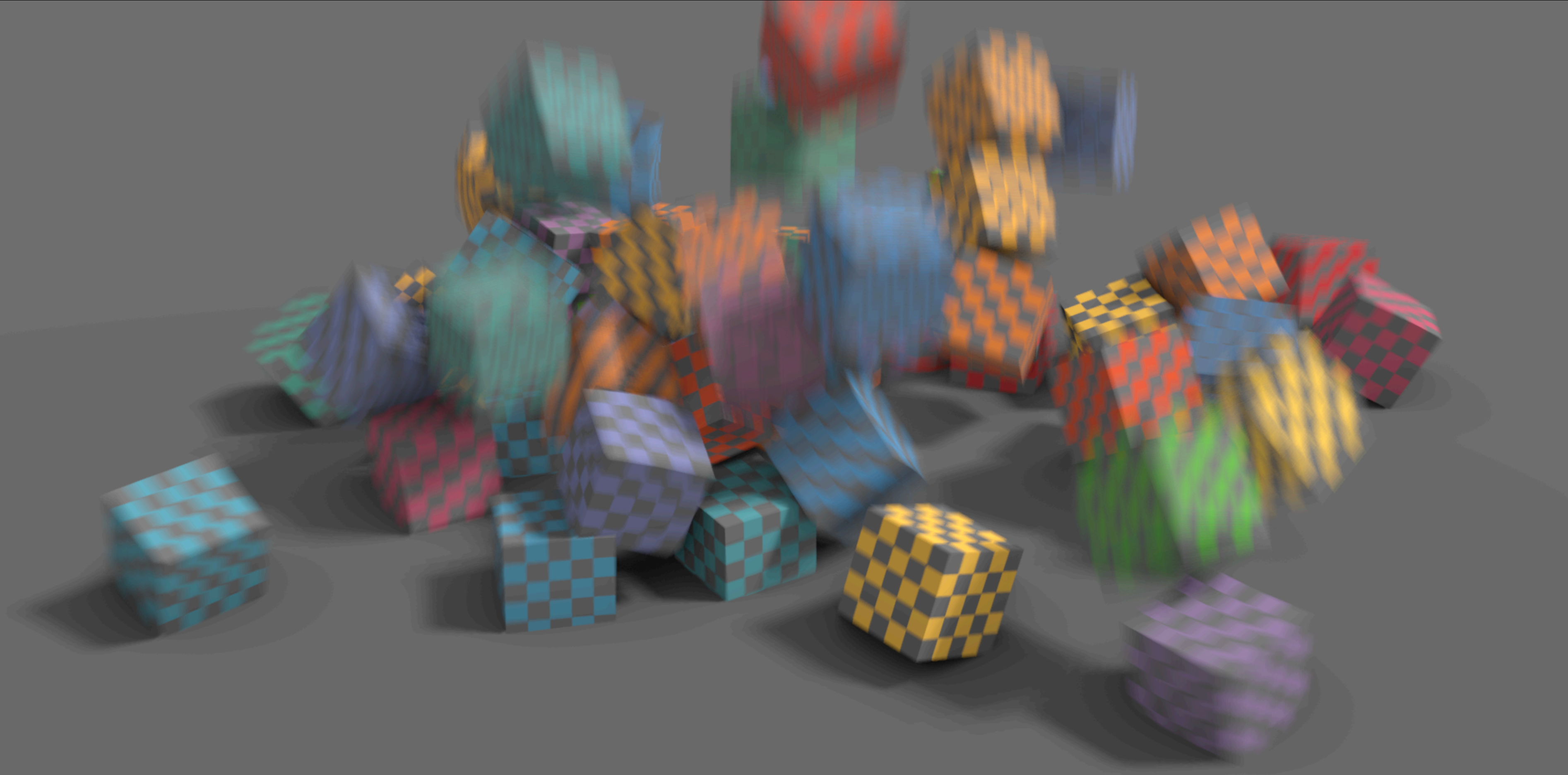
**Simulating these effects in a ray tracer**

# Rendering with lens defocus blur



**Credit: Pixar**

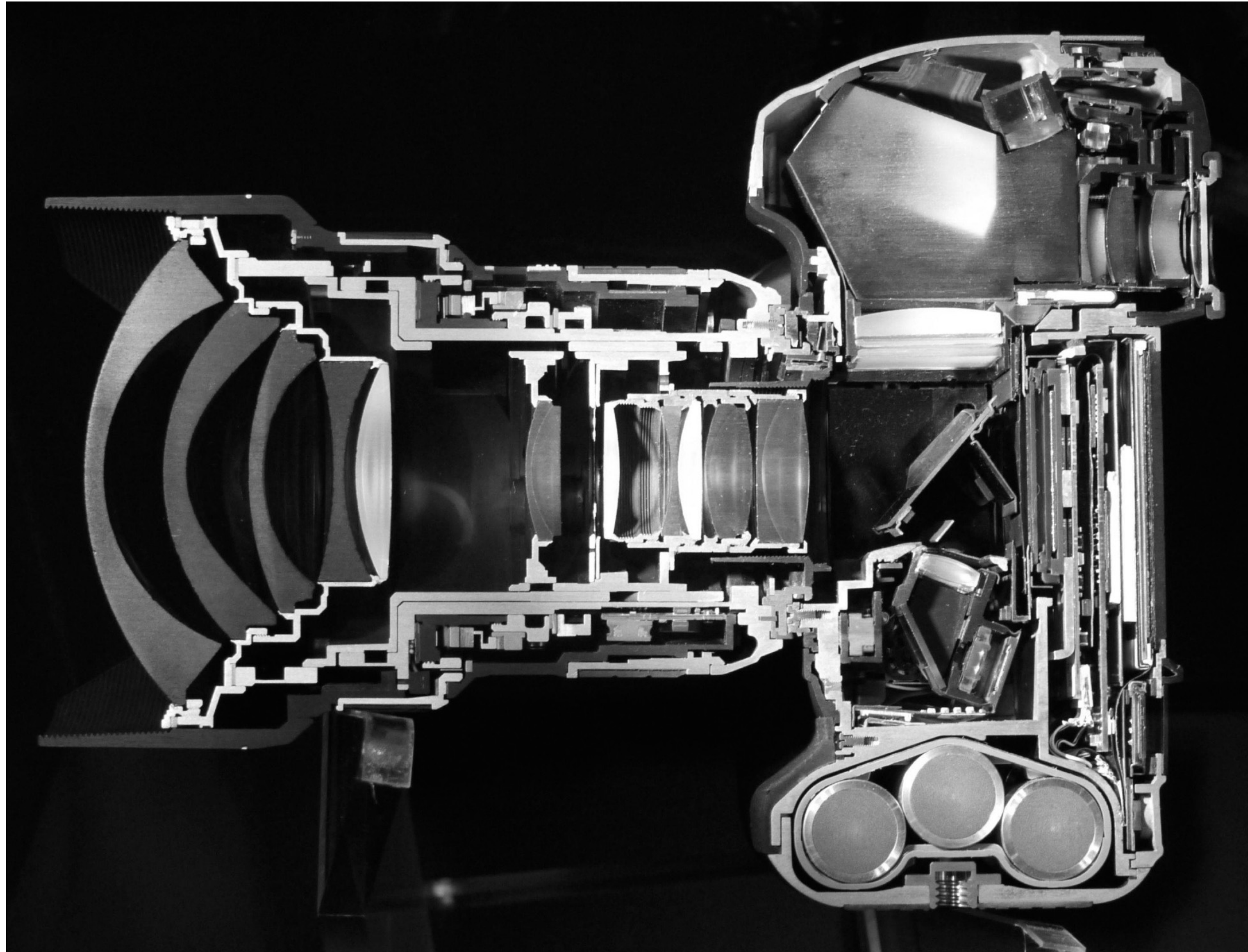
# Rendering with motion blur



Credit: Blender Docs

# What's Happening Inside the Camera?

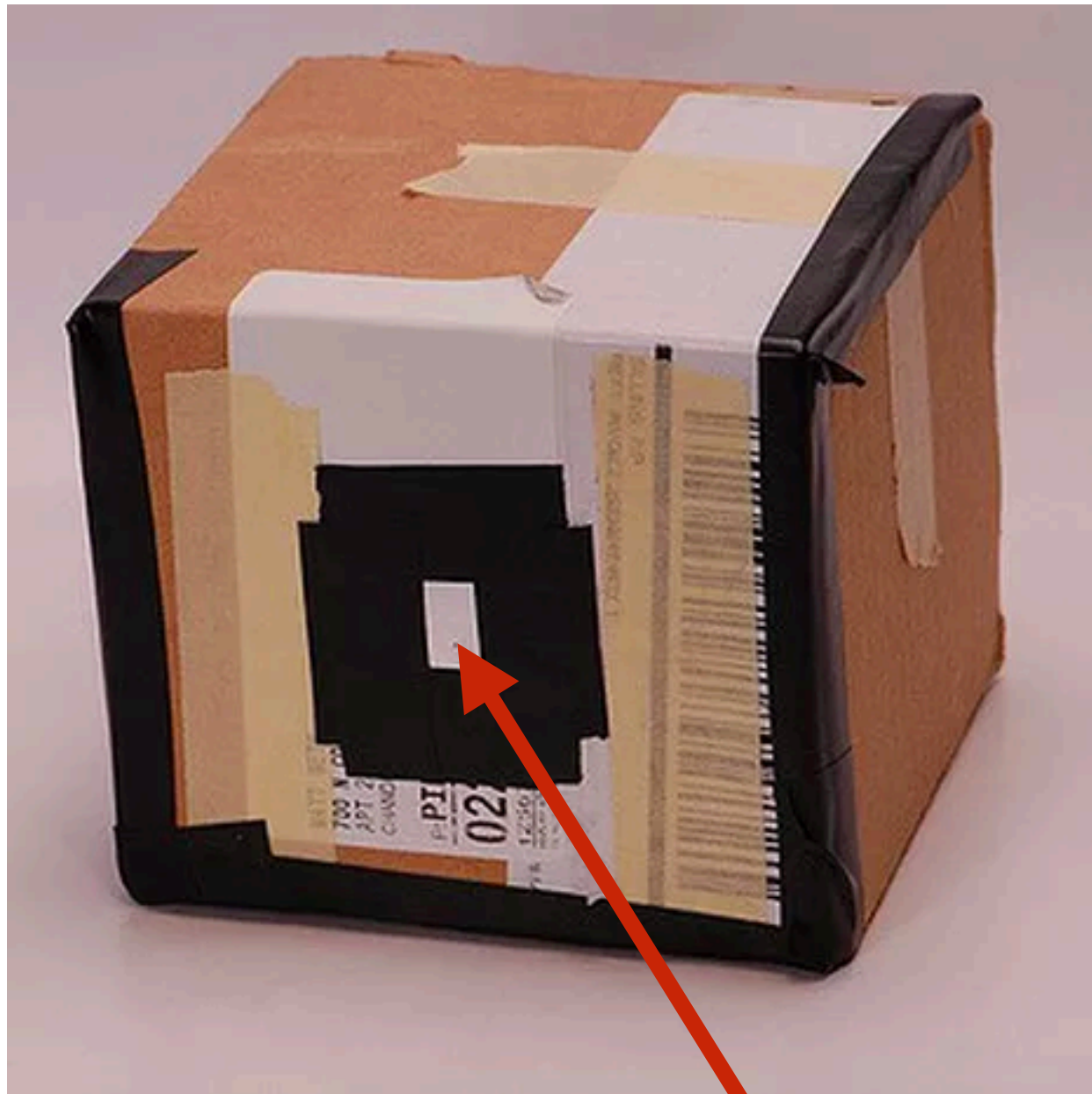
---



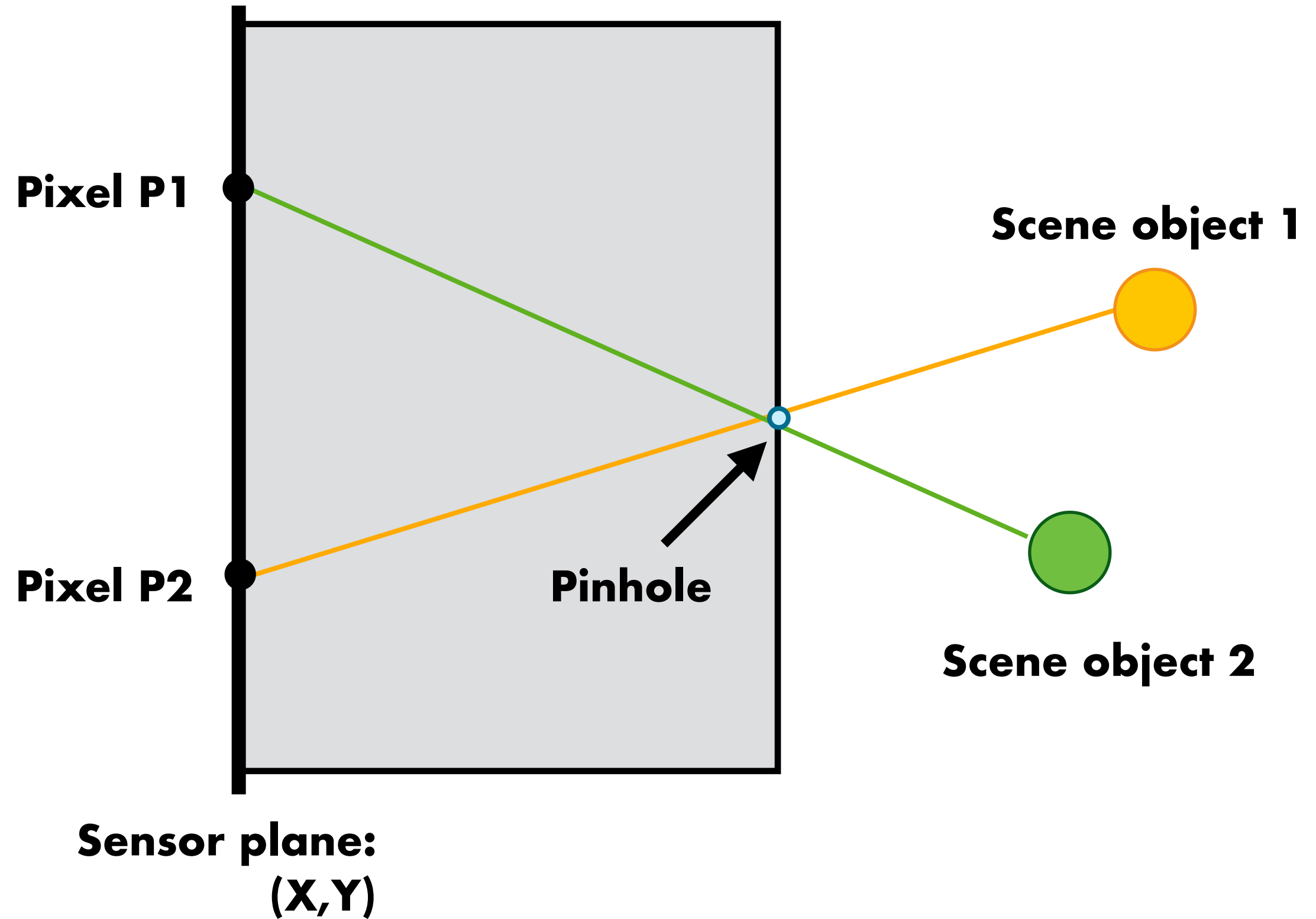
Cross-section of Nikon D3, 14-24mm F2.8 lens



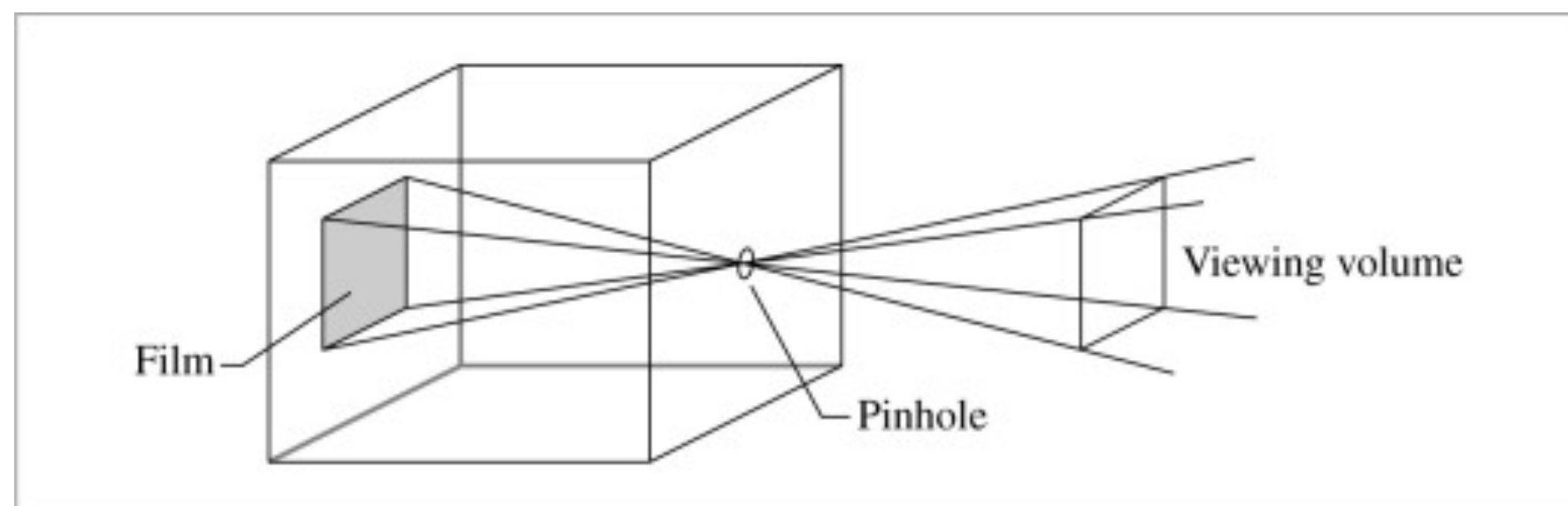
# A much simpler camera



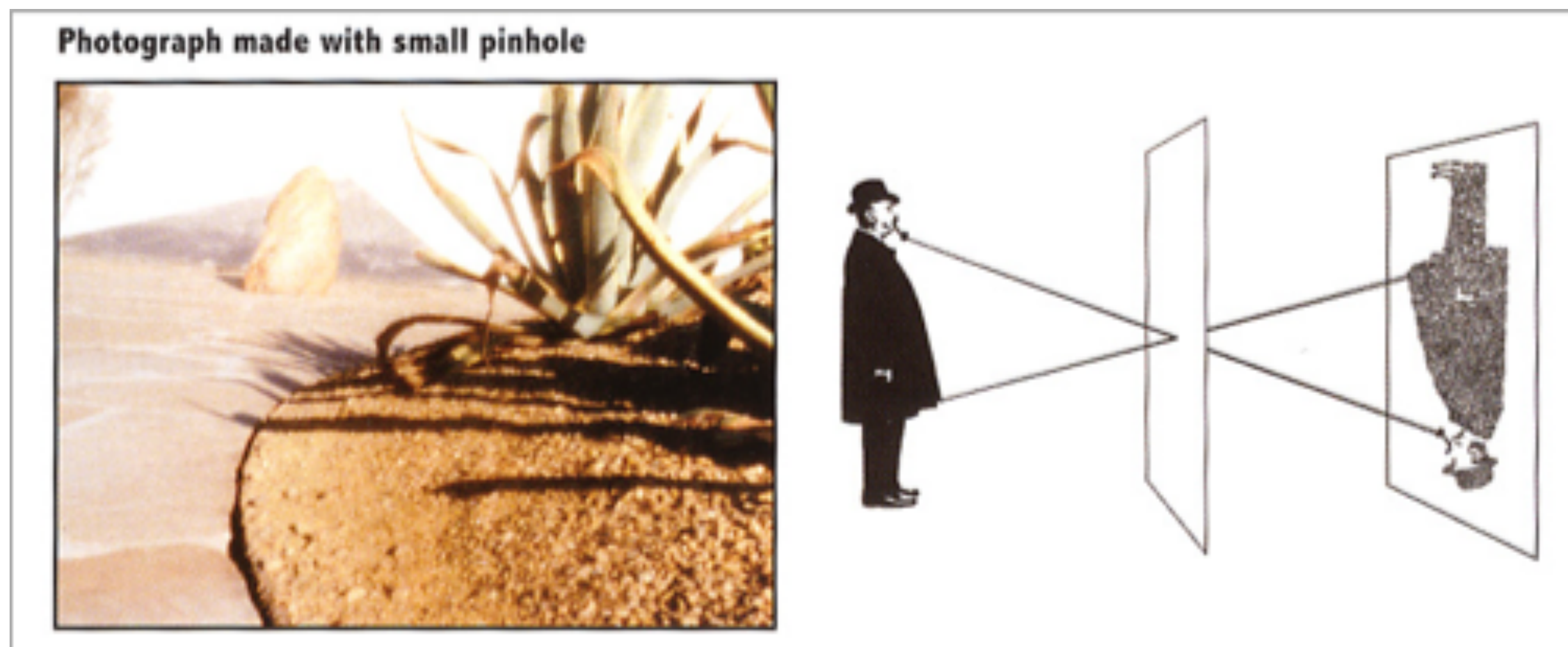
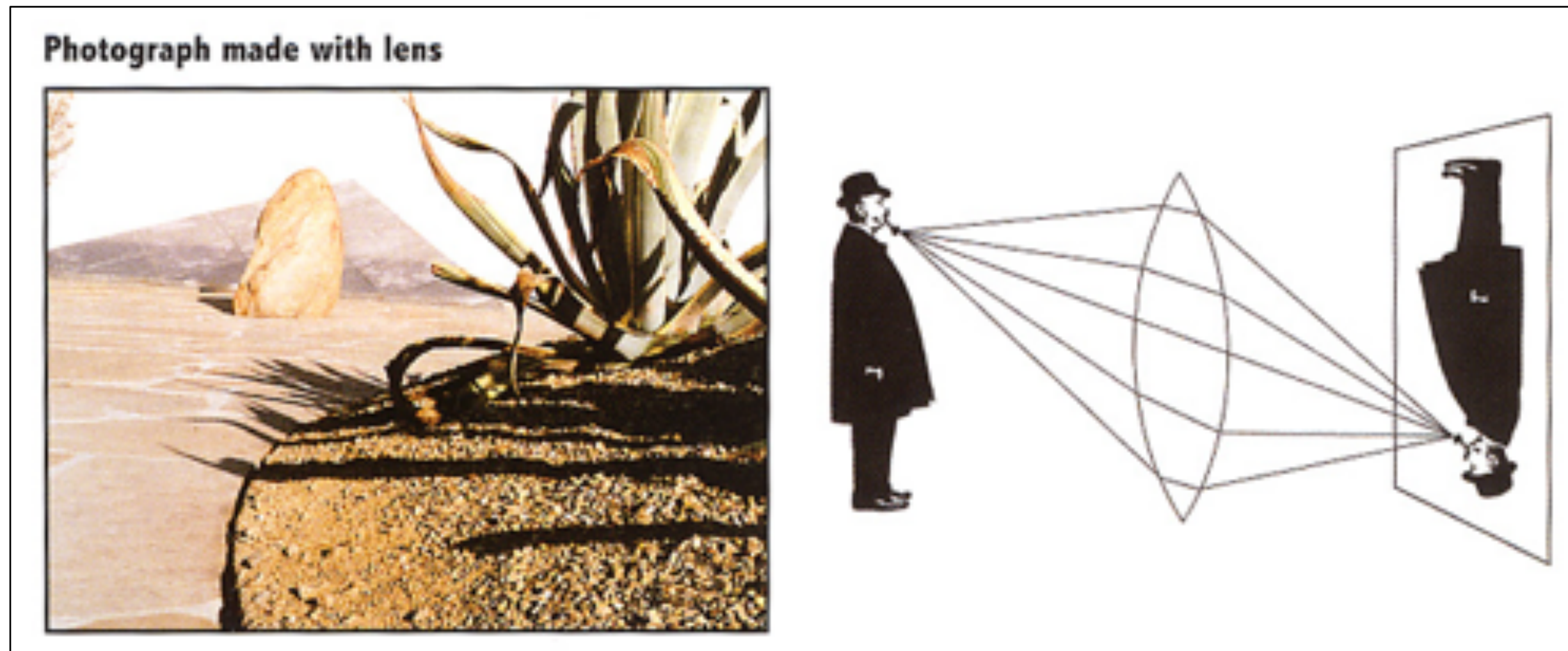
**Pinhole**



**Diagram in 3D...**



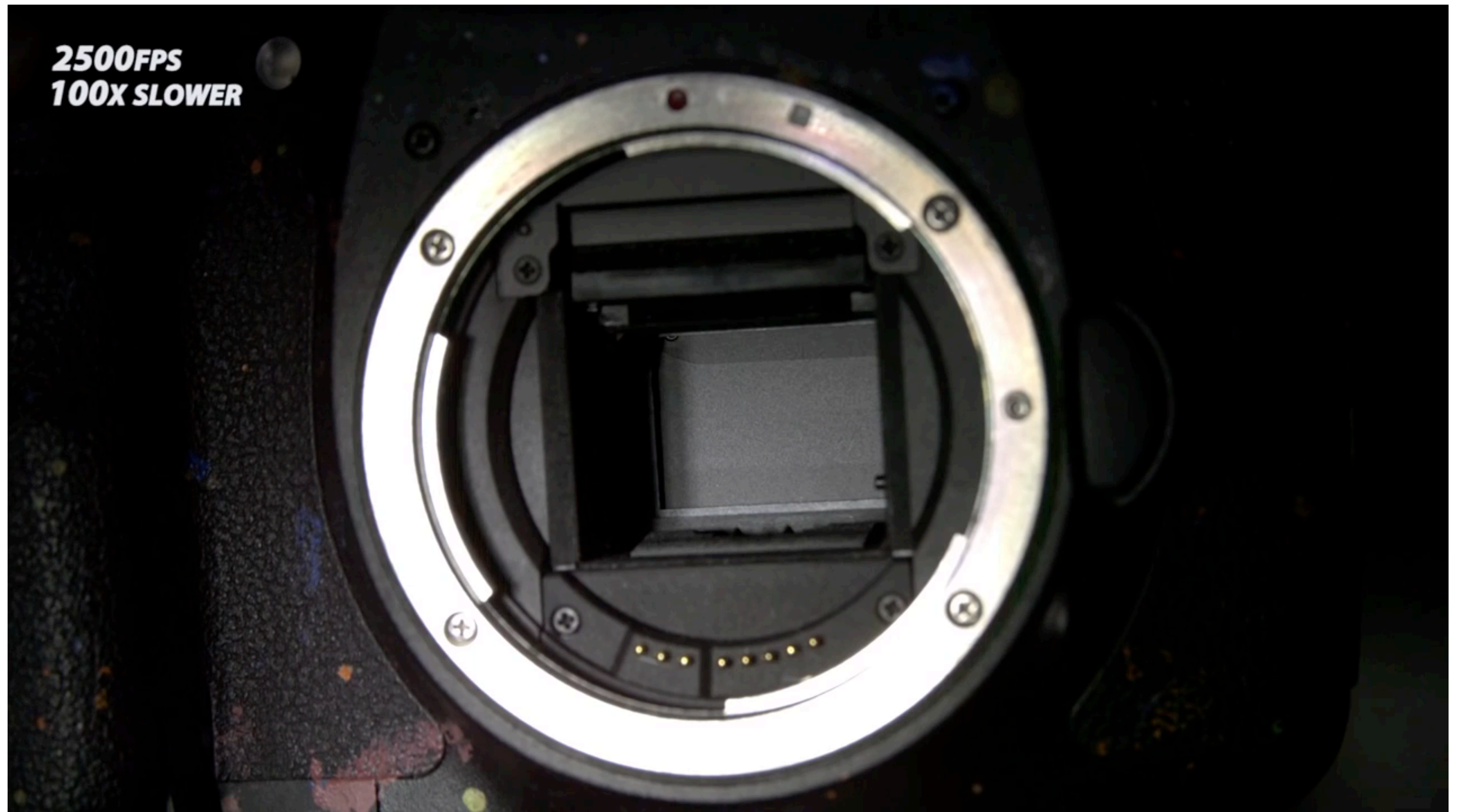
# Pinholes & Lenses Form Image on Sensor



London and Upton

# Shutter Exposes Sensor For Precise Duration

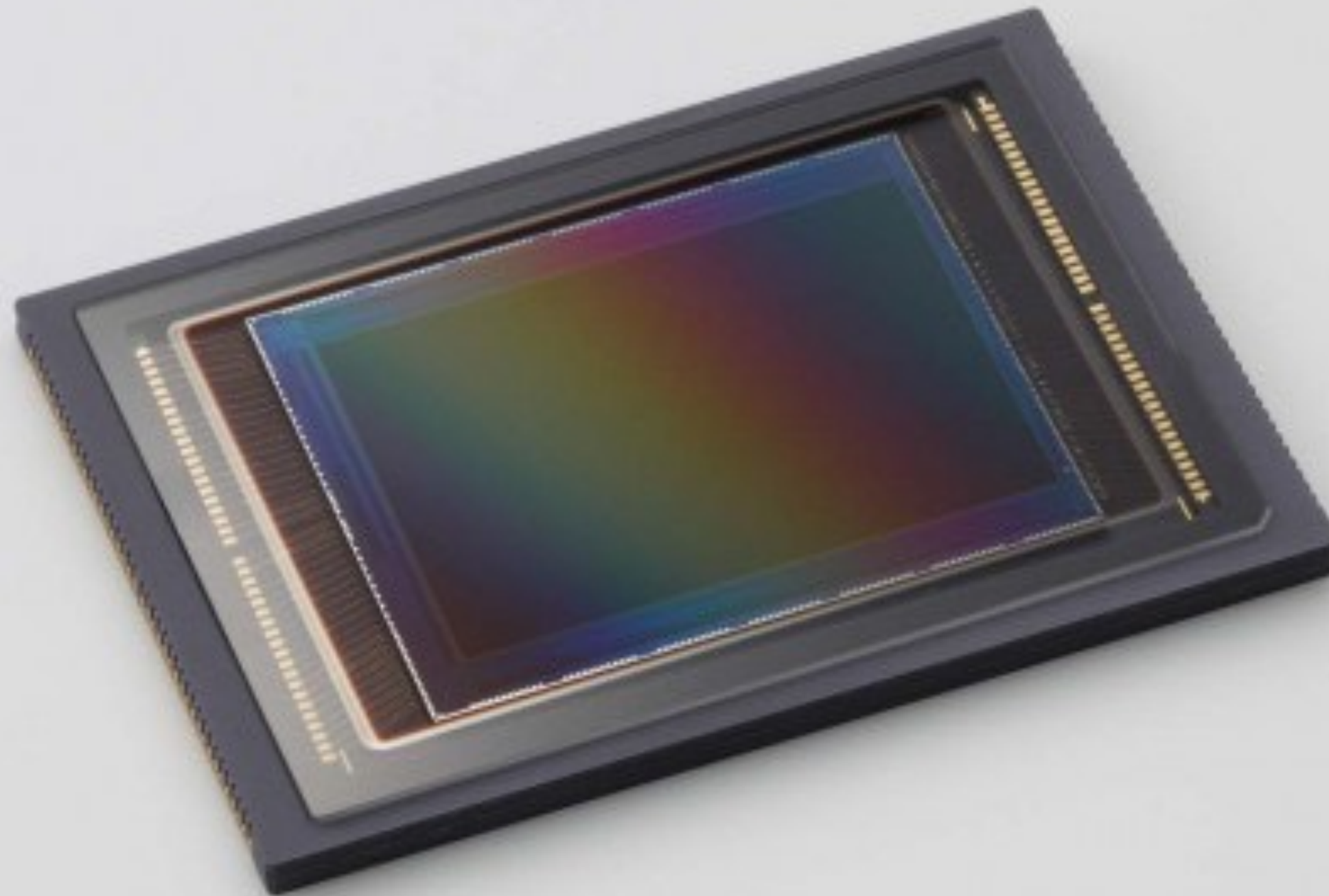
---



The Slow Mo Guys, <https://youtu.be/CmjeCchGRQo>

# Sensor Accumulates Irradiance During Exposure

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**Recall: irradiance = power per unit area**  
**Sensor pixels measure integral of irradiance over time**

# Lenses

# Modern Lens Designs Are Complex

---

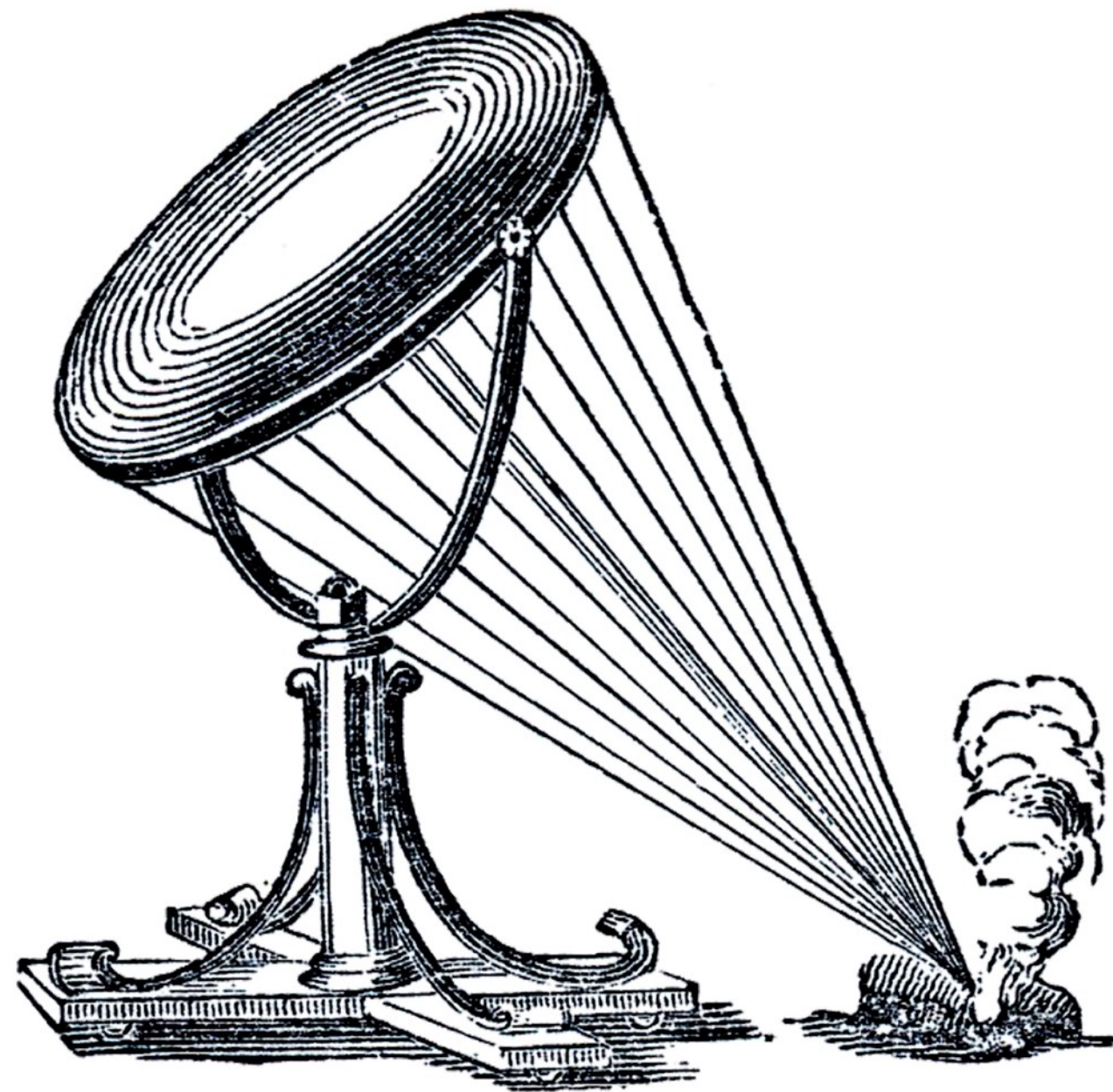


[Apple]

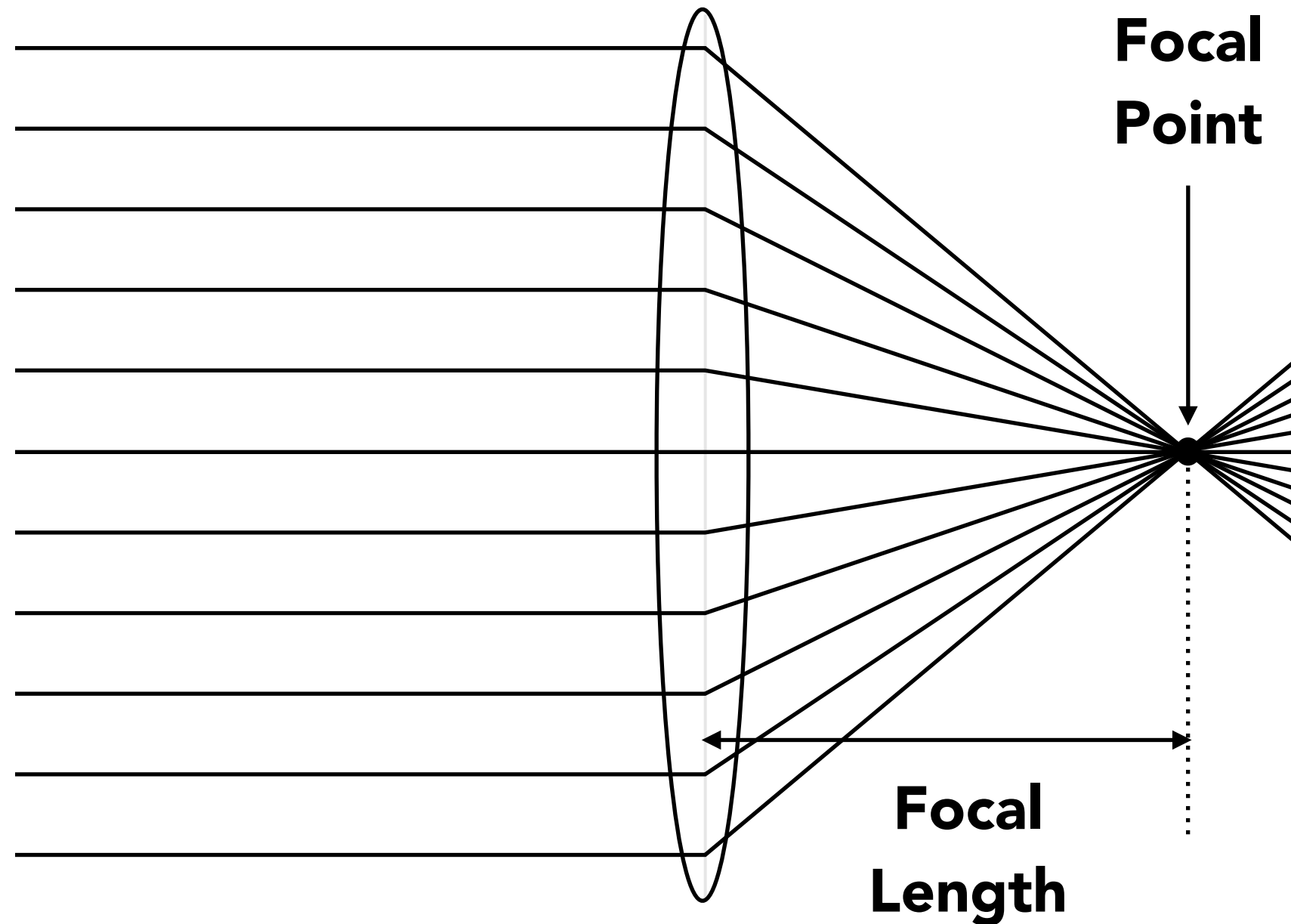
# **First: Thin Lens Approximation**

# Ideal Thin Lens – Focal Point

---



Credit: Karen Watson

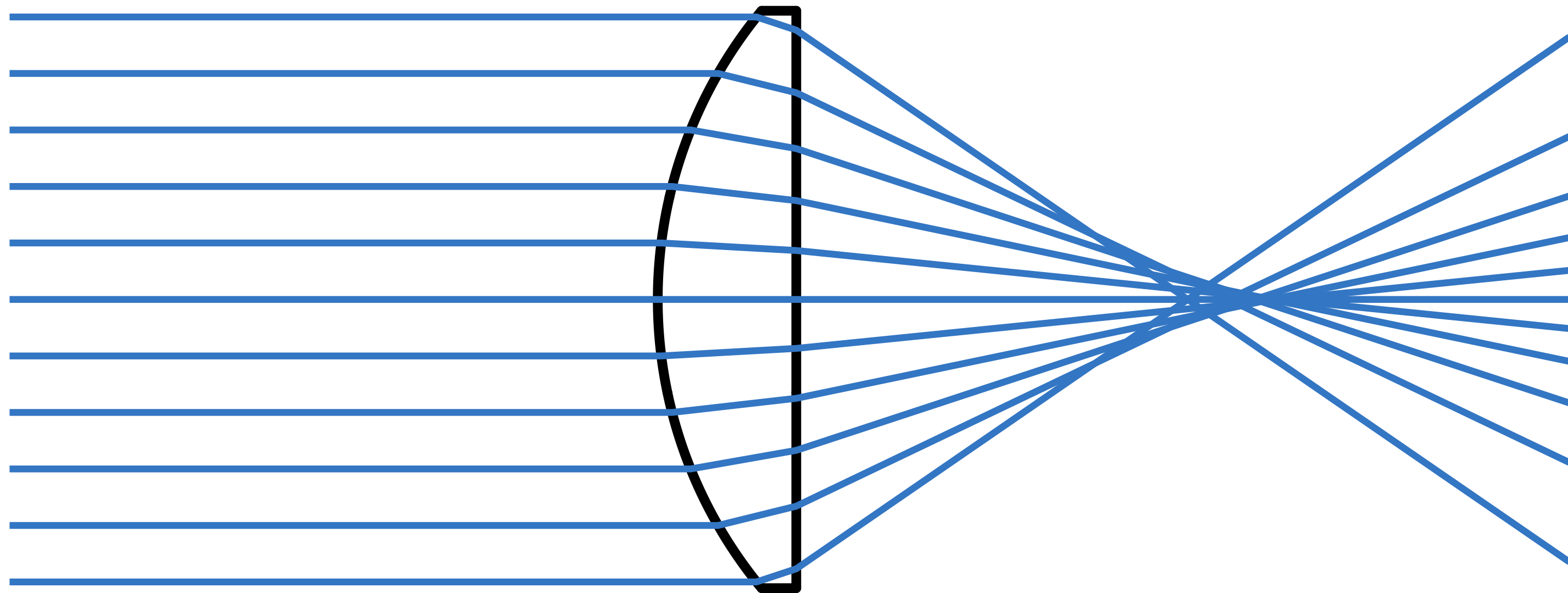


**Assume all parallel rays entering a lens pass through its focal point.**



# **Keep in mind: Real Lens Elements Are Not Ideal – Aberrations**

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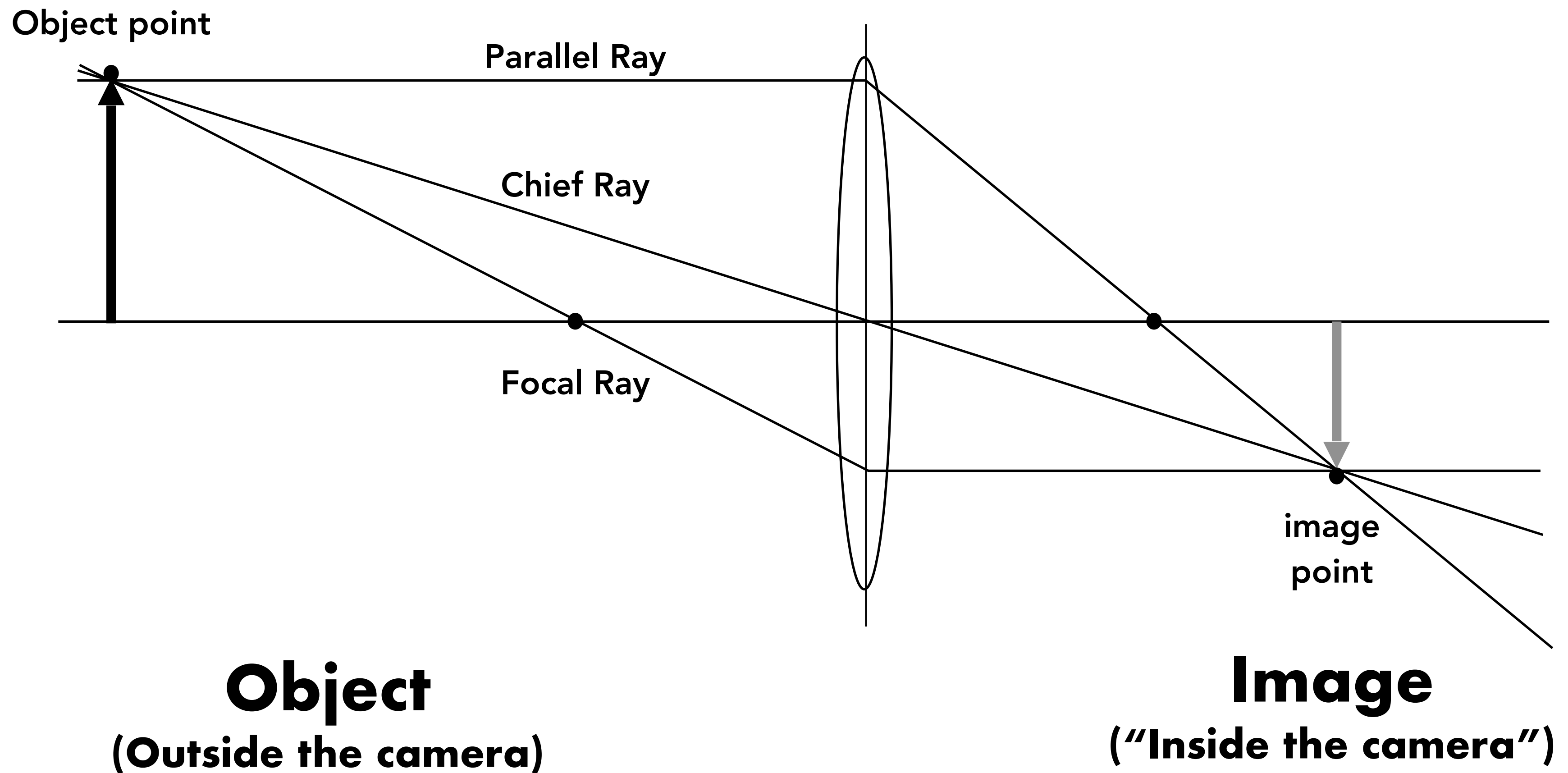


**Real plano-convex lens (spherical surface shape).  
Lens does not converge rays to a point anywhere.**

# **Gauss' Ray Diagrams**

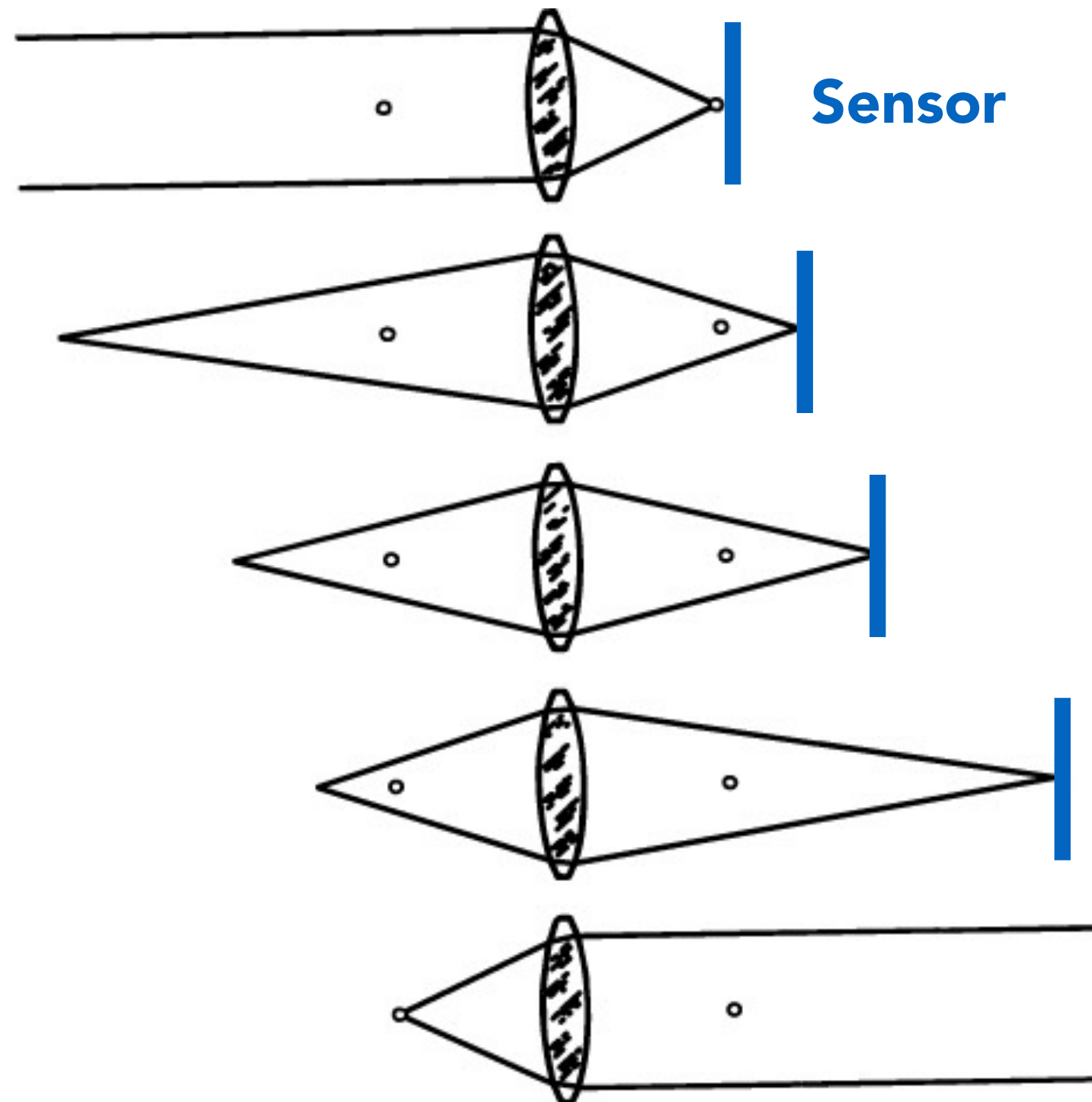
# Gauss' Ray Tracing Construction

---



# Lenses focus light!

---



**Rays from a point in object space intersect at a point in image space**

**These are conjugate points**

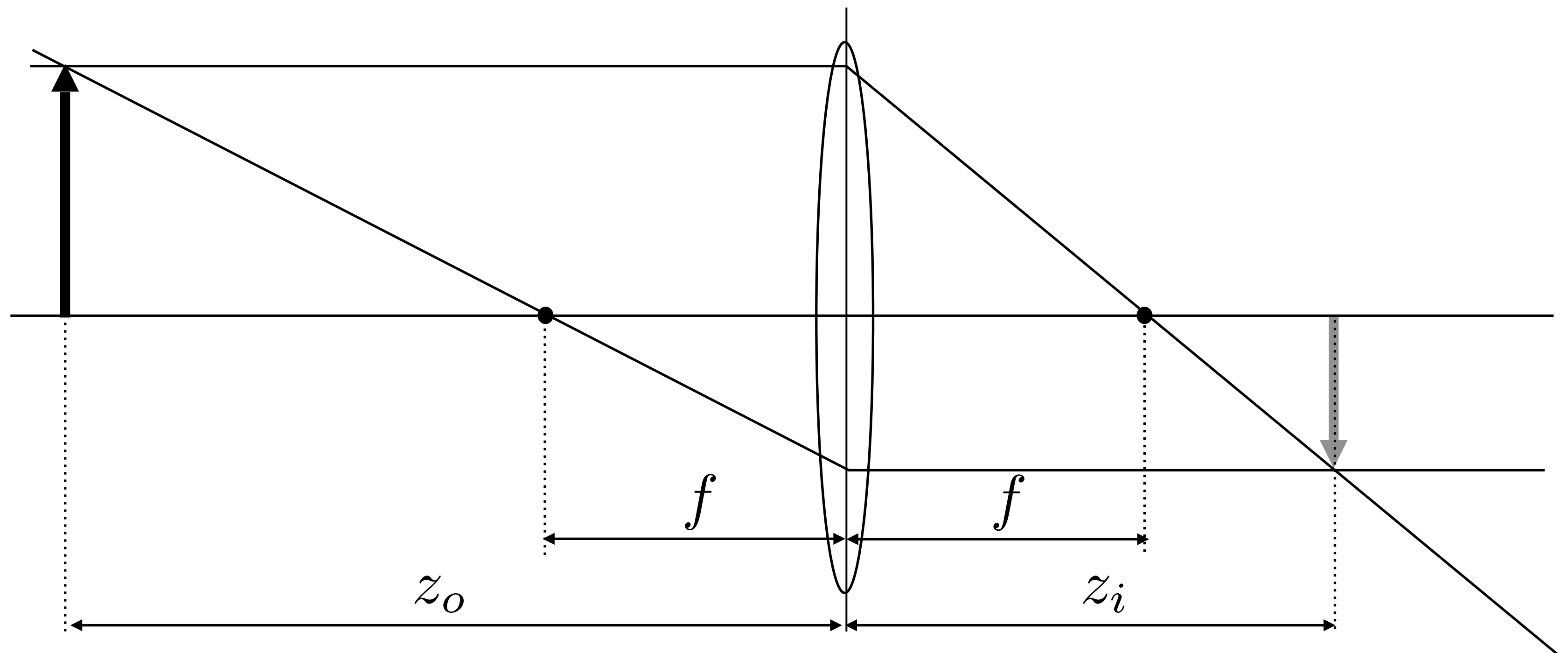
**Points at infinity converge at the focal point or focus**

**Points on different object planes focus on different image planes**

**The position of the point of focus can be changed by changing the distance between the lens and the sensor**

# Gauss' Ray Tracing Construction

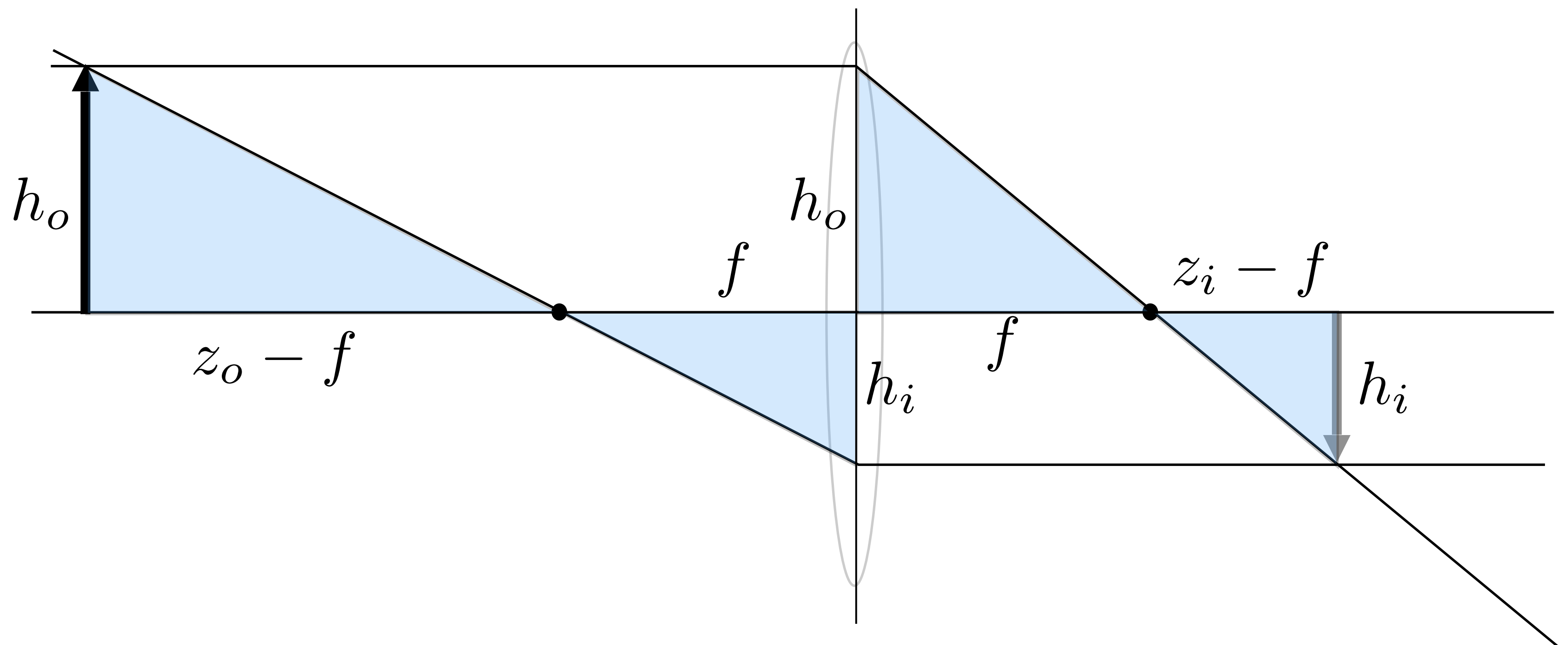
---



What is the relationship between conjugate depths  $z_o, z_i$ ?

# Gauss' Ray Tracing Construction

---



$$\frac{h_o}{z_o - f} = \frac{h_i}{f}$$

$$\frac{h_o}{f} = \frac{h_i}{z_i - f}$$

# Gauss' Ray Tracing Construction

---

$$\frac{h_o}{z_o - f} = \frac{h_i}{f} \qquad \frac{h_o}{f} = \frac{h_i}{z_i - f}$$
$$\frac{h_o}{h_i} = \frac{z_o - f}{f} \qquad \frac{h_o}{h_i} = \frac{f}{z_i - f}$$

$$\frac{z_o - f}{f} = \frac{f}{z_i - f}$$

**Object / image heights  
factor out - applies to all rays**

$$(z_o - f)(z_i - f) = f^2$$

**Newtonian Thin Lens Equation**

$$z_o z_i - (z_o + z_i)f + f^2 = f^2$$

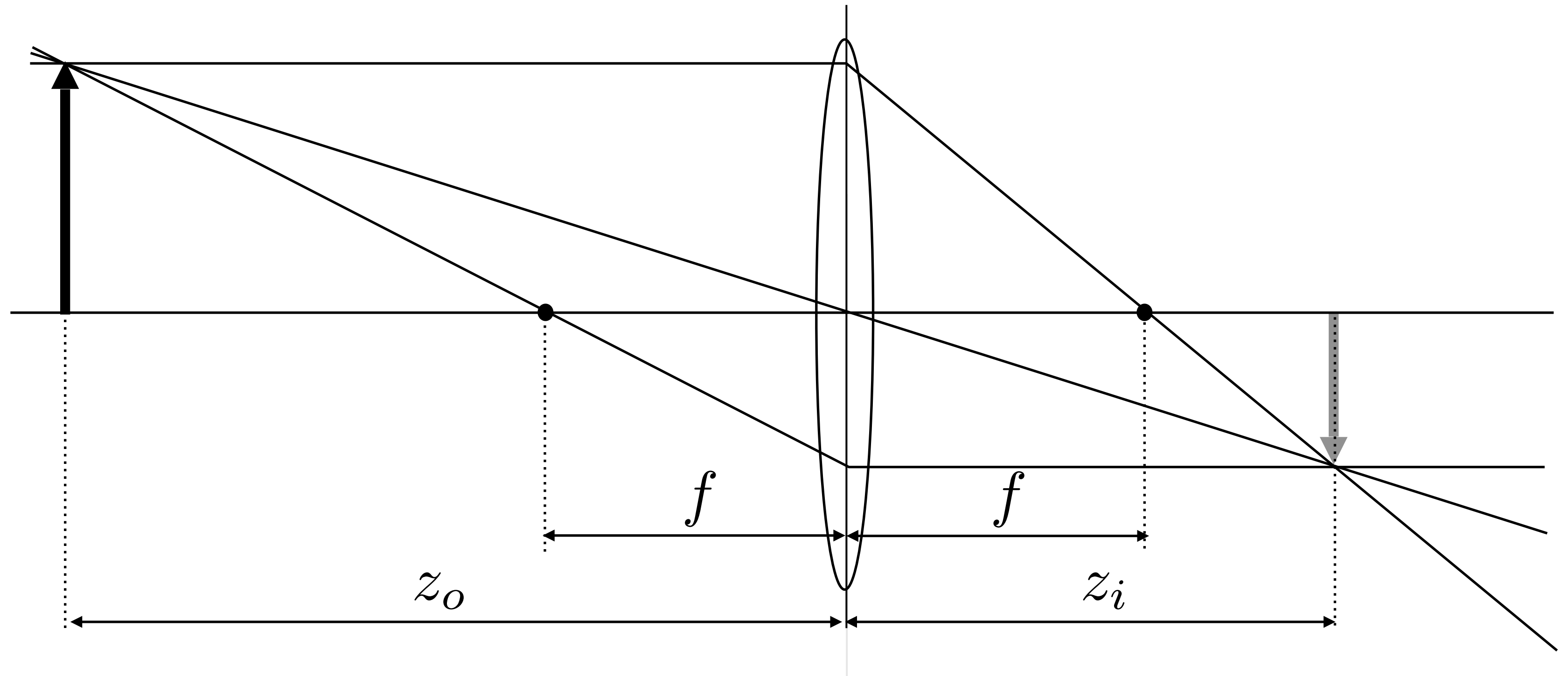
$$z_o z_i = (z_o + z_i)f$$

$$\frac{1}{f} = \frac{1}{z_i} + \frac{1}{z_o}$$

**Gaussian Thin Lens Equation**

# The Thin Lens Equation

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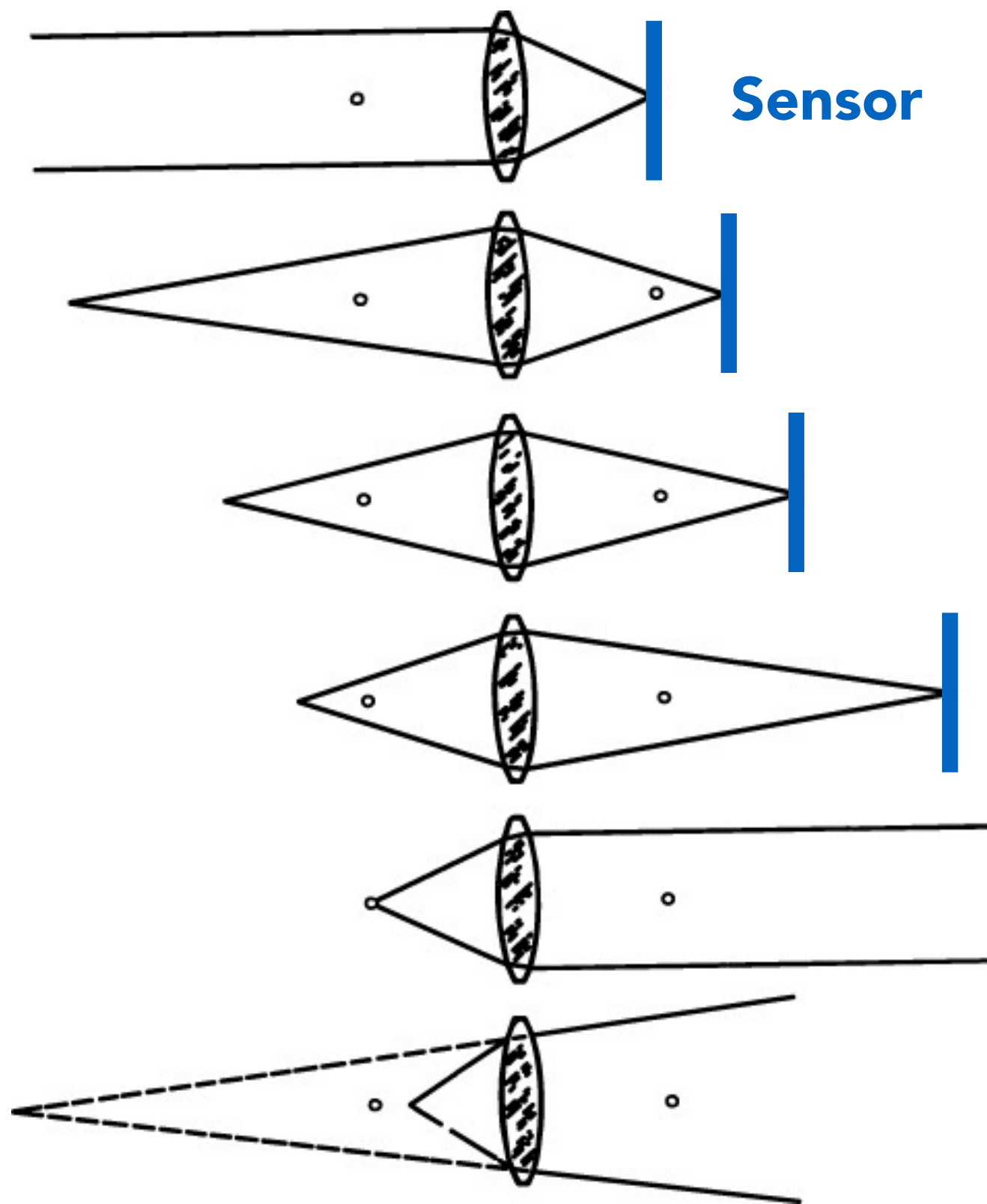


$$\frac{1}{f} = \frac{1}{z_i} + \frac{1}{z_o}$$



# Changing the Focus Distance

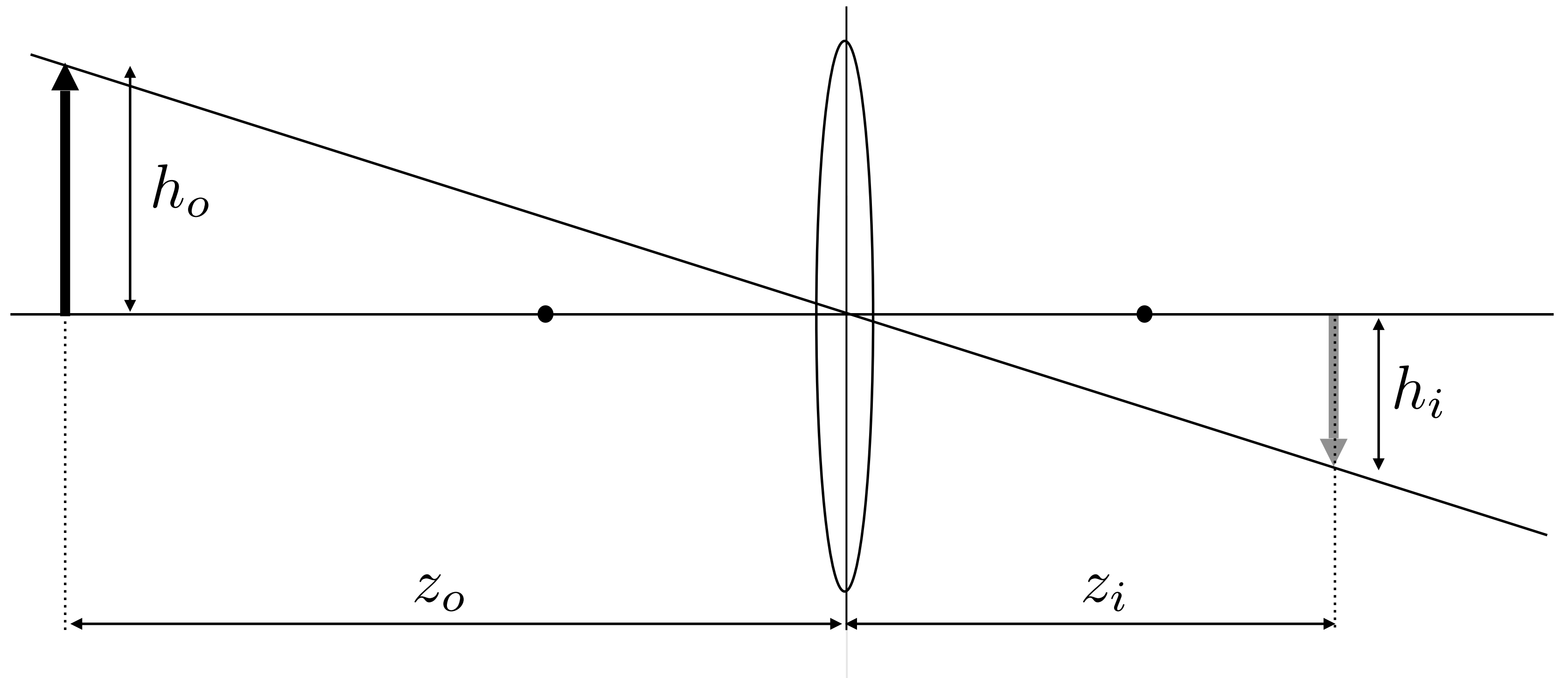
$$\frac{1}{f} = \frac{1}{z_i} + \frac{1}{z_o}$$



- $z_i$  and  $z_o$  are called conjugate points
- To focus on objects at different distances, move the sensor relative to the lens
- For  $z_i < z_o$  the object is larger than the image
- At  $z_i = z_o$  we have 1:1 macro imaging
- For  $z_i > z_o$  the image is larger than the object (magnified)
- Can't focus on objects closer than the lens' focal length

# Magnification

---



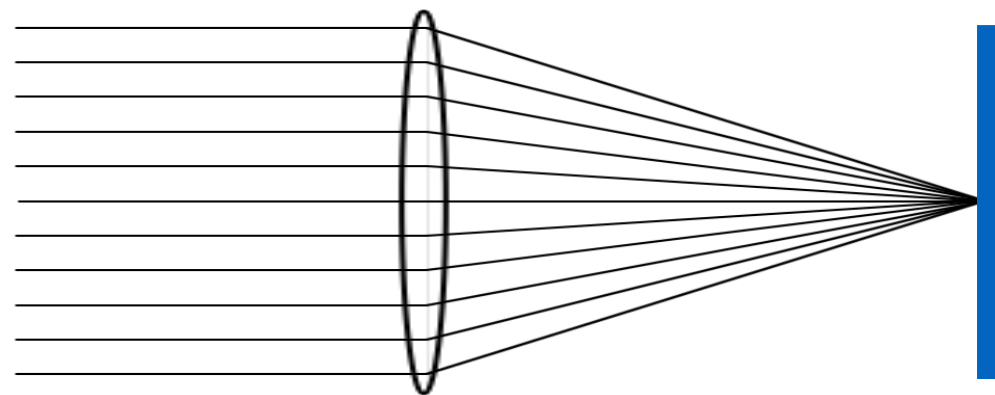
$$m = \frac{h_i}{h_o} = \frac{z_i}{z_o}$$

# Magnification Example – Focus at Infinity

$$\frac{1}{f} = \frac{1}{z_i} + \frac{1}{z_o} \quad m = \frac{z_i}{z_o}$$

If focused on a distant mountain

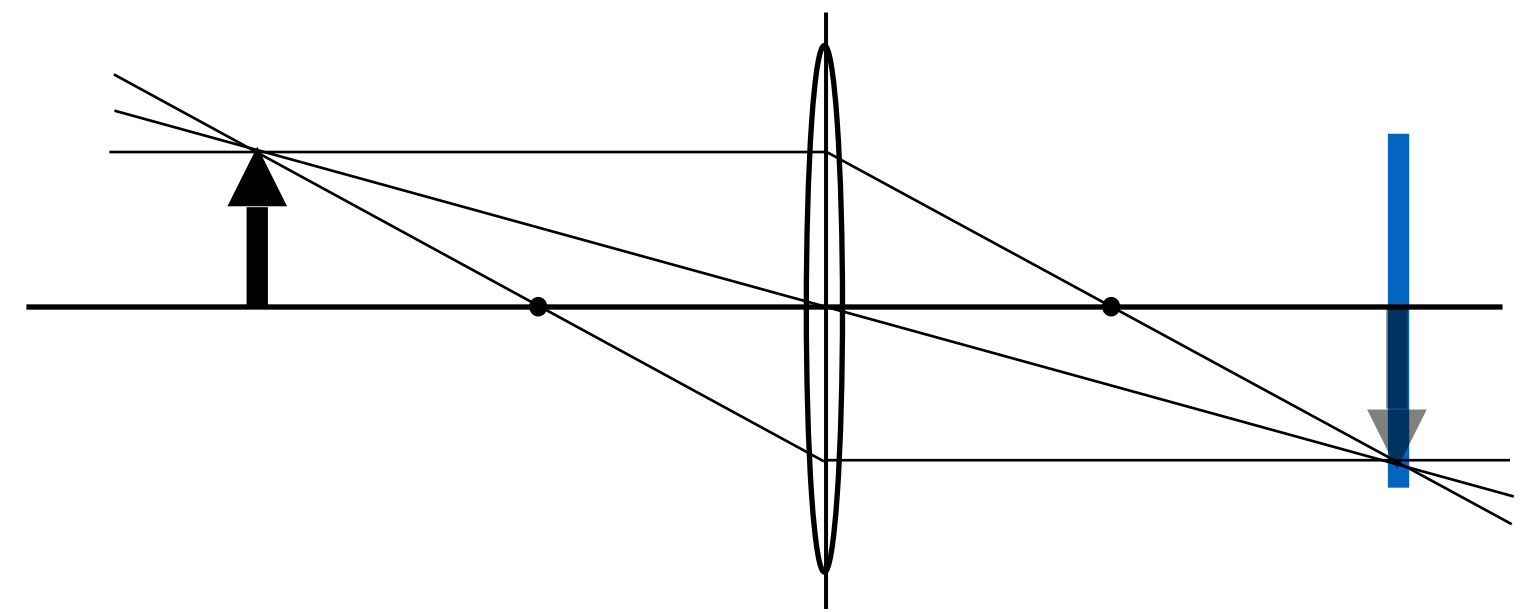
- $z_o \approx \infty$ , so  $z_i = f$
- sensor at focal point
- magnification  $\approx 0$



# Magnification Example – Focus at 1:1 Macro



$$\frac{1}{f} = \frac{1}{z_i} + \frac{1}{z_o} \quad m = \frac{z_i}{z_o}$$



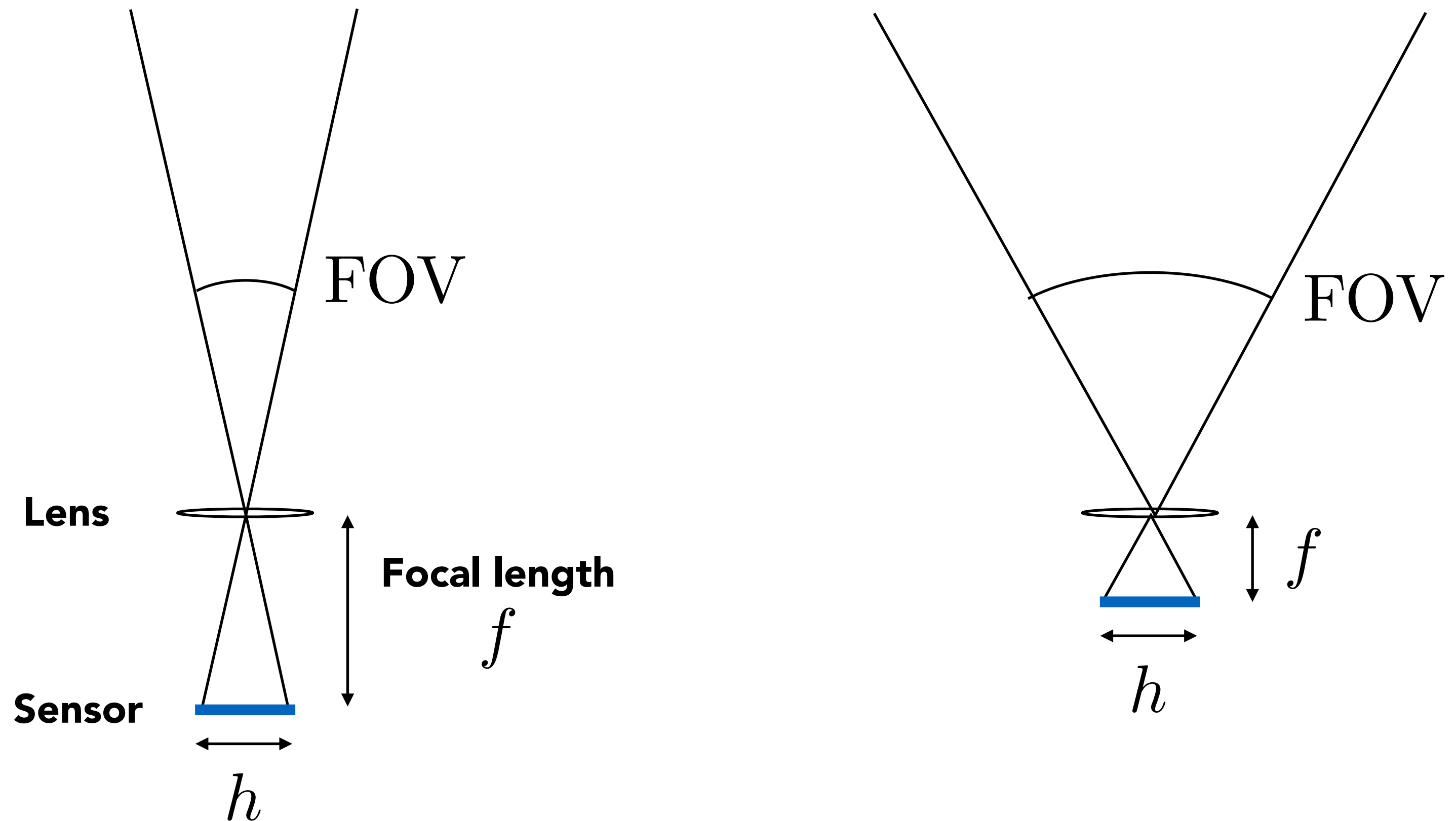
What configuration do we need to achieve a magnification of 1 (i.e. image and object the same size, a.k.a. 1:1 macro)?

- Need  $z_i = z_o$ , so  $z_i = z_o = 2f$  — sensor at twice focal length
- In 1:1 imaging, if the sensor is 36 mm wide, an object 36 mm wide will fill the frame

# **Relationship between focal length and field of view**

# Effect of Focal Length on FOV

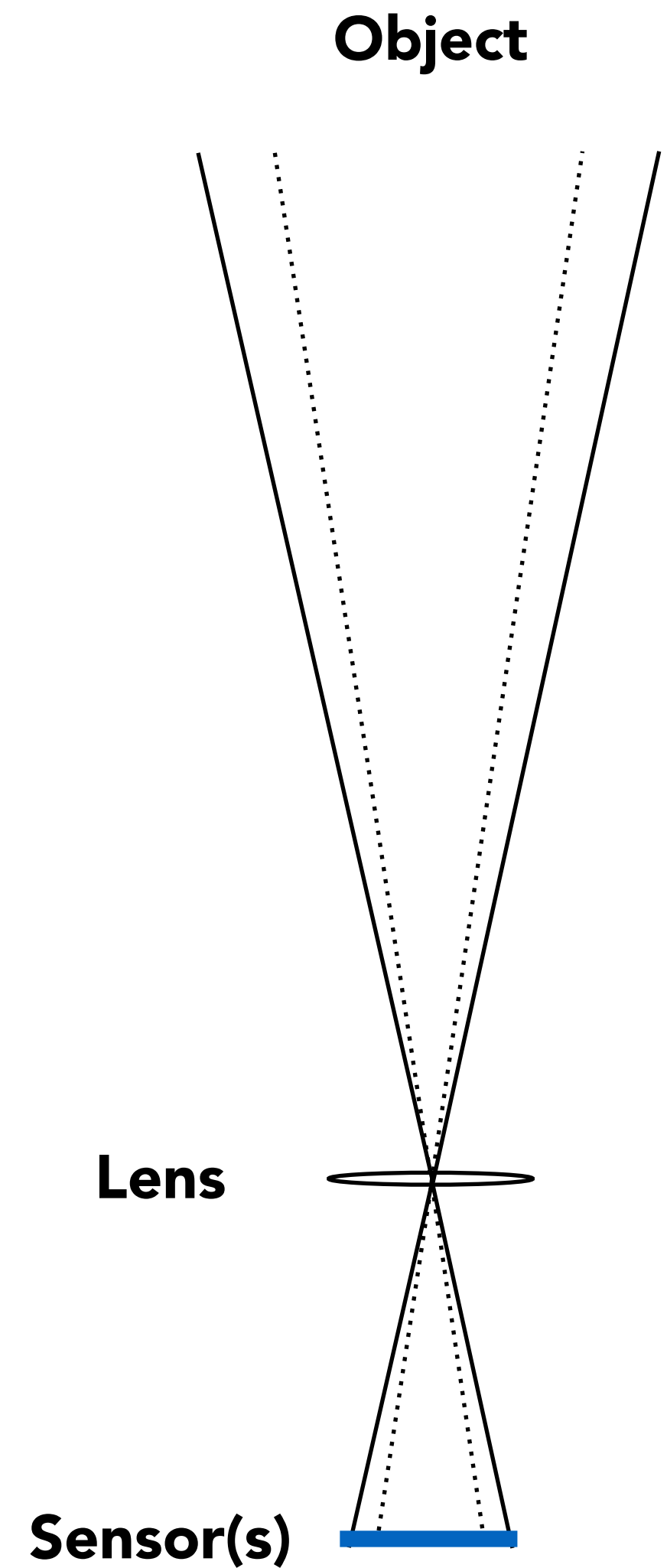
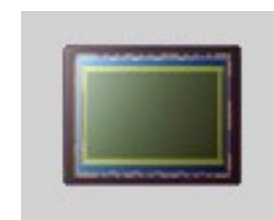
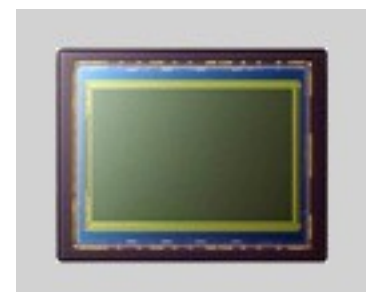
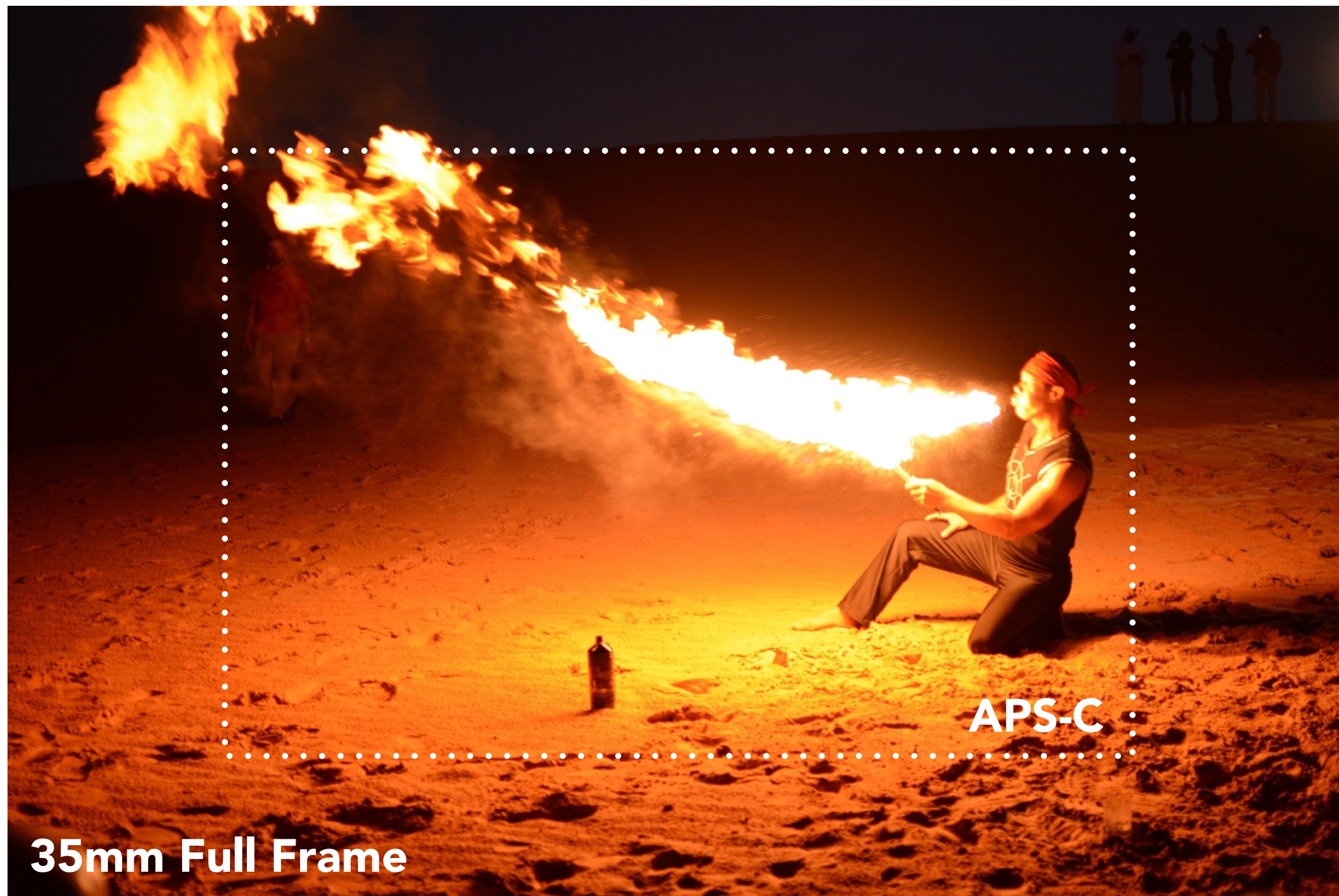
---



**For a fixed sensor size, decreasing the focal length increases the field of view.**

$$\text{FOV} = 2 \arctan \left( \frac{h}{2f} \right)$$

# Effect of Sensor Size on FOV



# Sensor Sizes

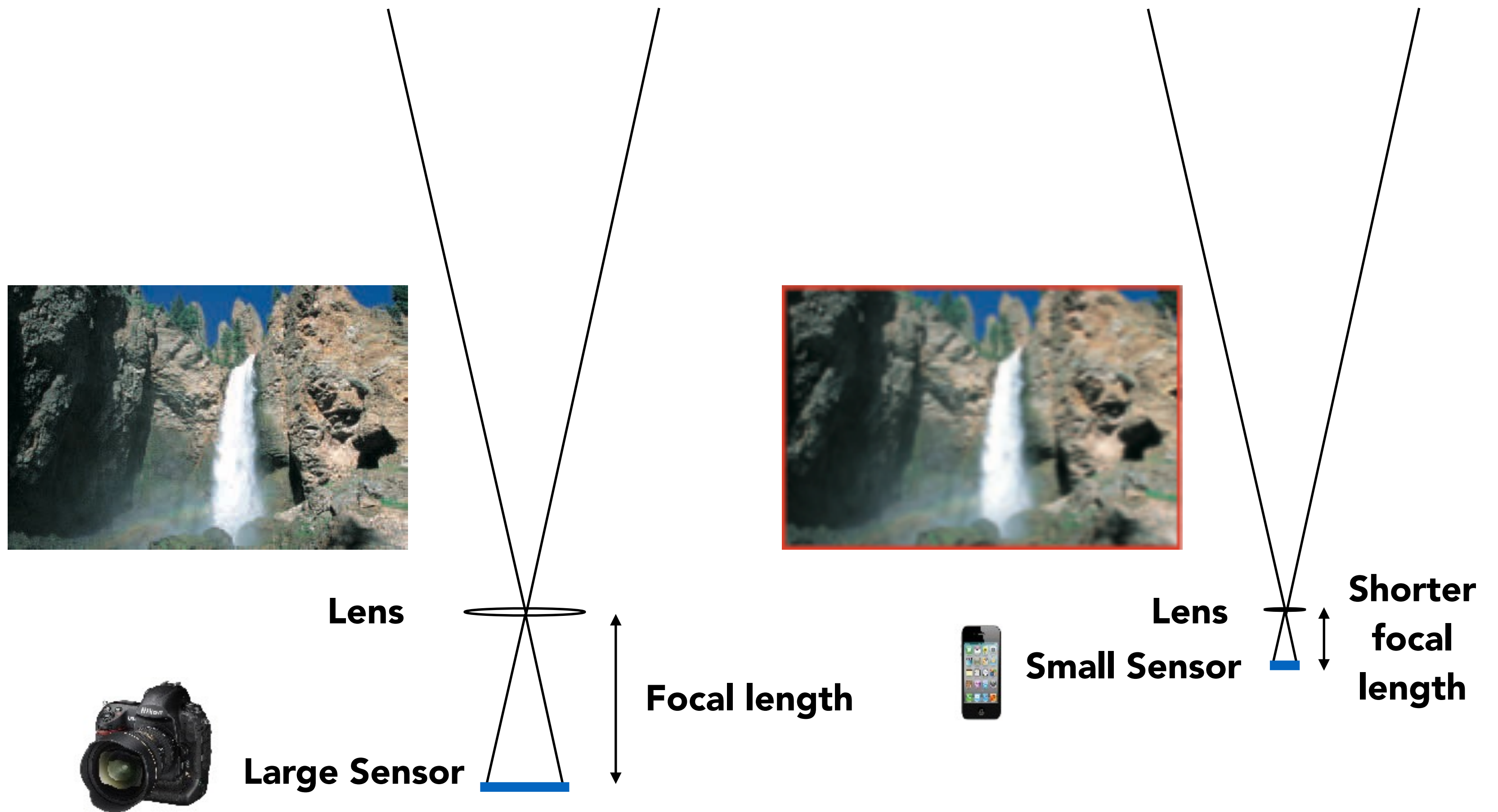
Sensor Name	Medium Format	Full Frame	APS-H	APS-C	4/3	1"	1/1.63"	1/2.3"	1/3.2"
Sensor Size	53.7 x 40.2mm	36 x 23.9mm	27.9x18.6mm	23.6x15.8mm	17.3x13mm	13.2x8.8mm	8.38x5.59mm	6.16x4.62mm	4.54x3.42mm
Sensor Area	21.59 cm <sup>2</sup>	8.6 cm <sup>2</sup>	5.19 cm <sup>2</sup>	3.73 cm <sup>2</sup>	2.25 cm <sup>2</sup>	1.16 cm <sup>2</sup>	0.47 cm <sup>2</sup>	0.28 cm <sup>2</sup>	0.15 cm <sup>2</sup>
Crop Factor	0.64	1.0	1.29	1.52	2.0	2.7	4.3	5.62	7.61
Image									
Example									



Credit: [lensvid.com](http://lensvid.com)

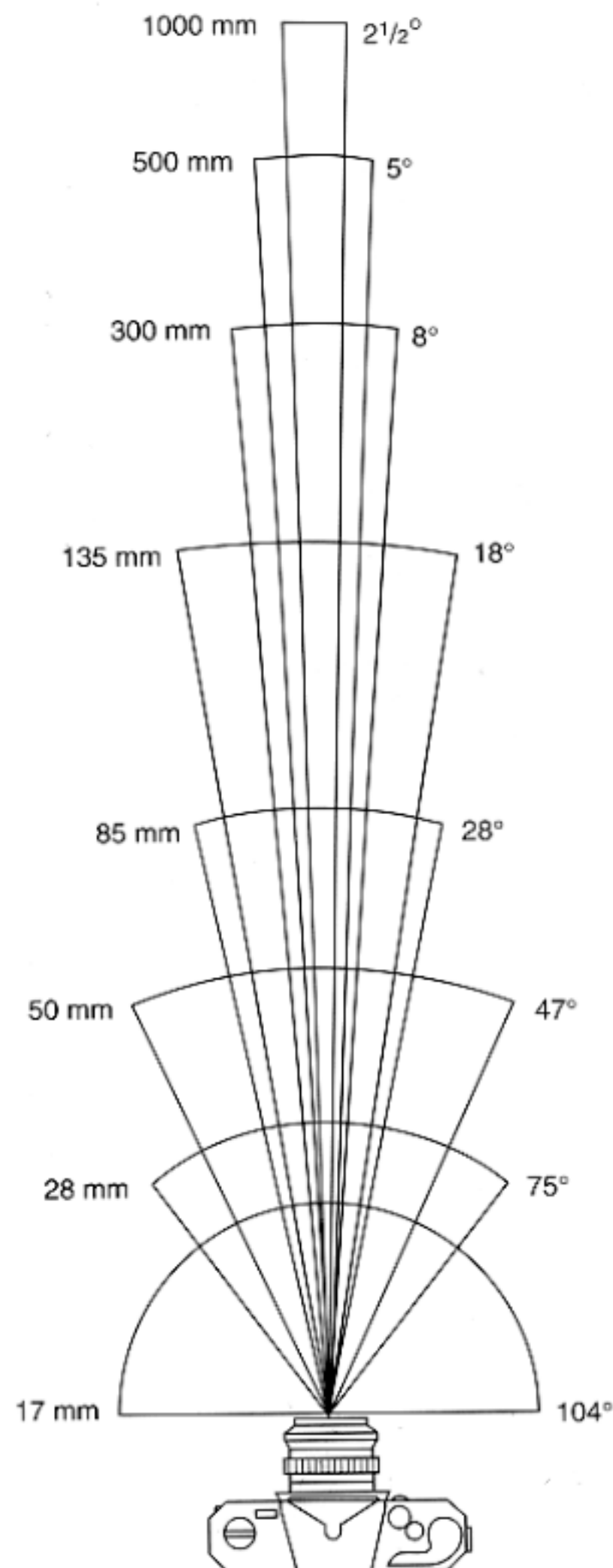


# Maintain FOV on Smaller Sensor?



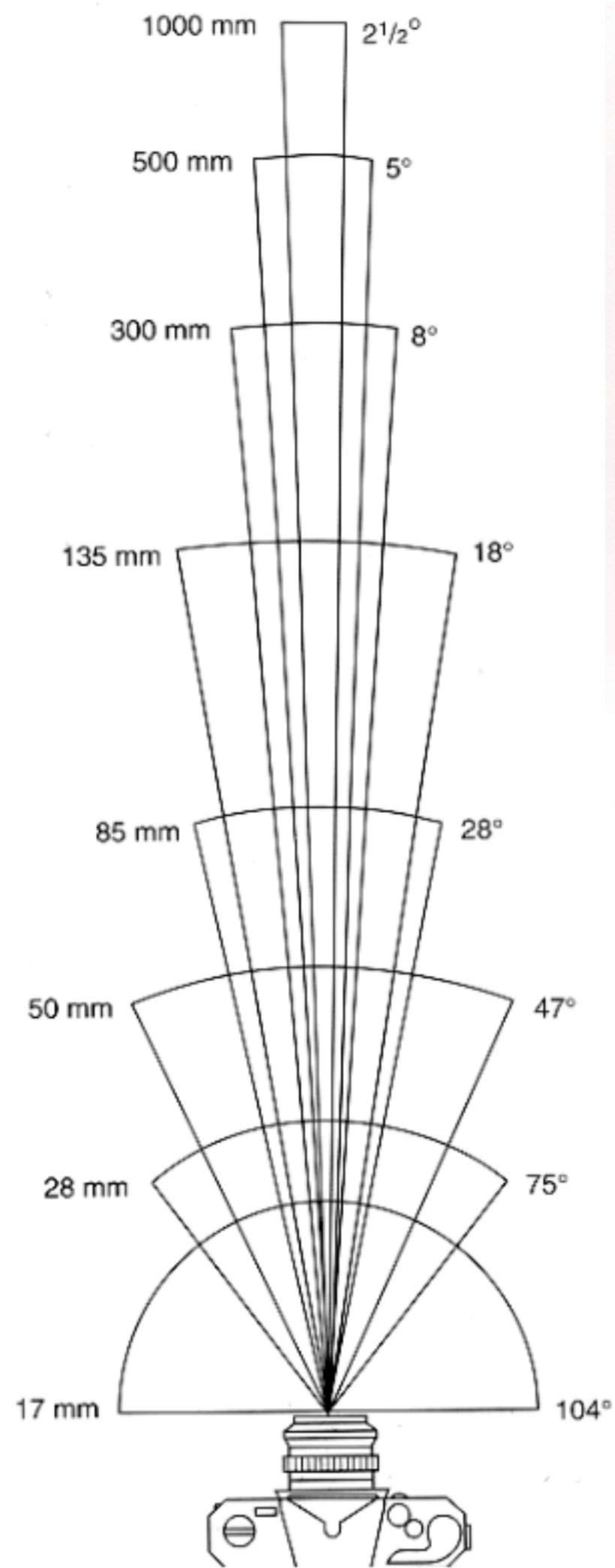
To maintain FOV, decrease focal length of lens  
in proportion to width/height of sensor

# Focal Length v. Field of View



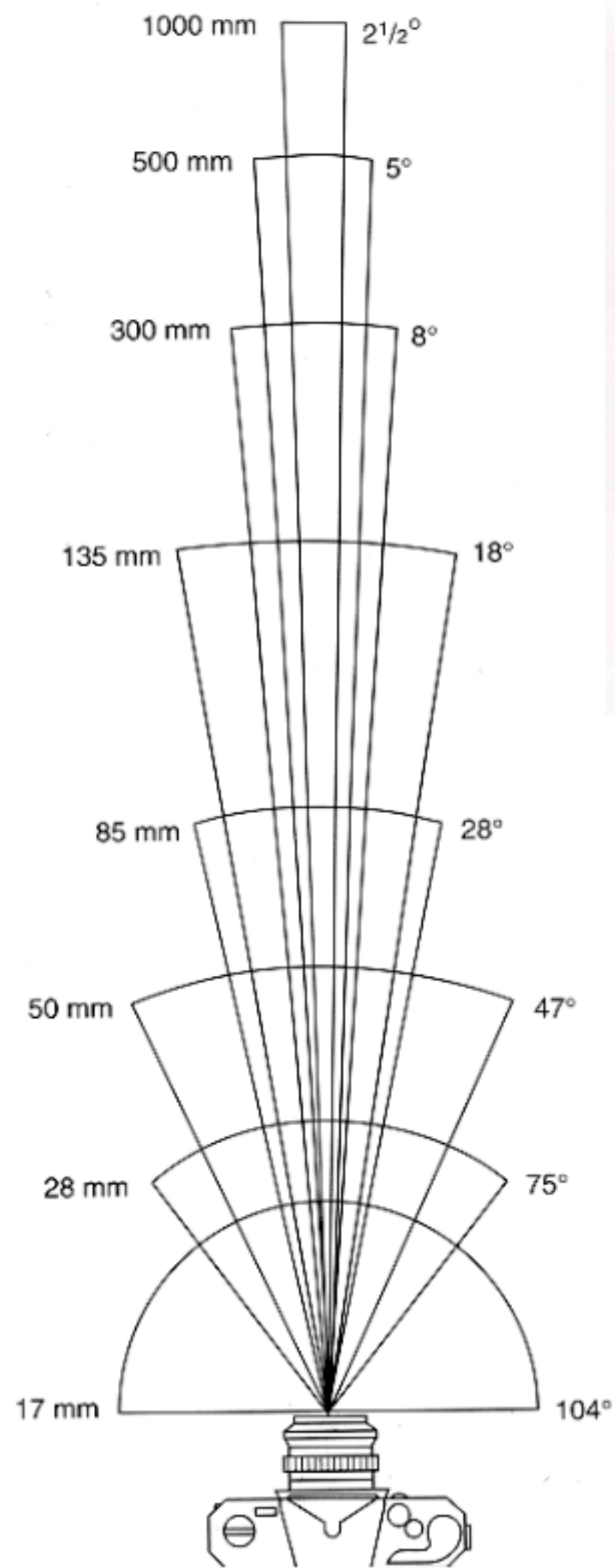
- For historical reasons, it is common to refer to angular field of view by focal length of a lens used on a 35mm-format film (36 x 24mm)
- Examples of focal lengths on 35mm format:
  - 17mm is wide angle 104°
  - 50mm is a "normal" lens 47°
  - 200mm is telephoto lens 12°
- Careful! When we say current cell phones have approximately 28mm "equivalent" focal length, this uses the above convention. The physical focal length is often 5-6 times shorter, because the sensor is correspondingly smaller

# Focal Length v. Field of View



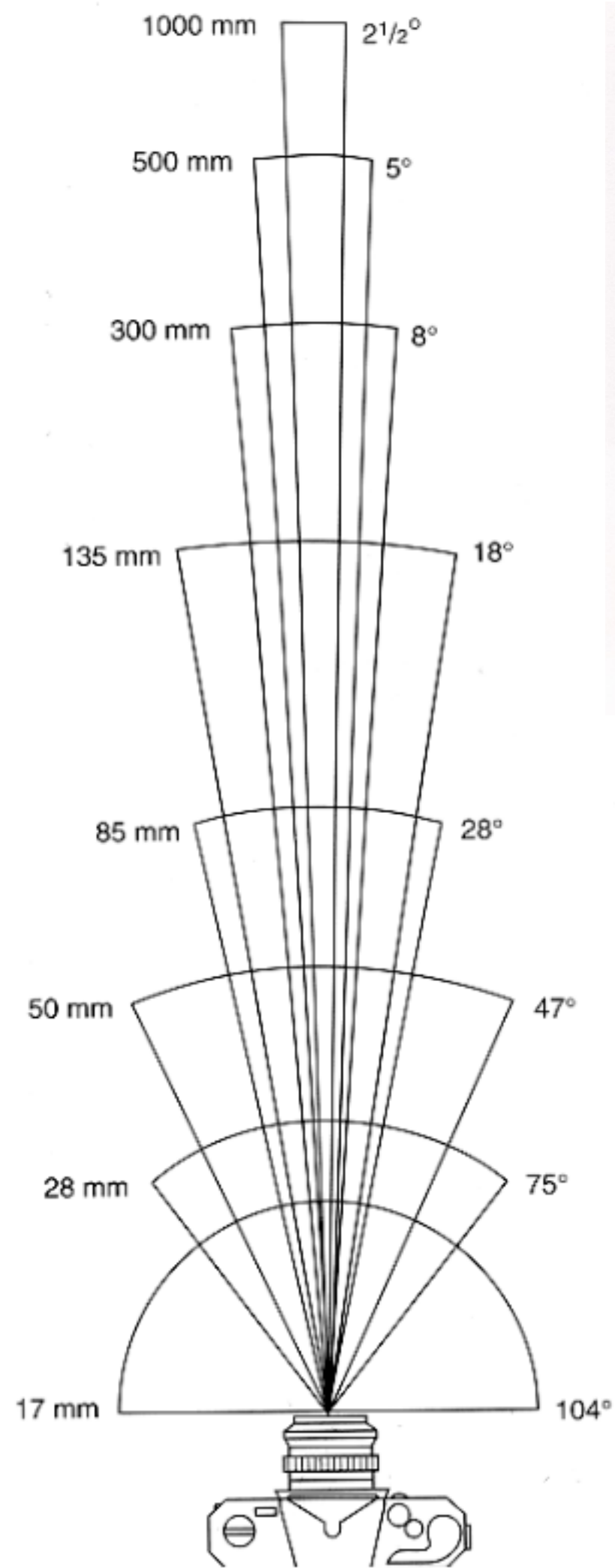
From London and Upton, and Canon EF Lens Work III

# Focal Length v. Field of View



From London and Upton, and Canon EF Lens Work III

# Focal Length v. Field of View



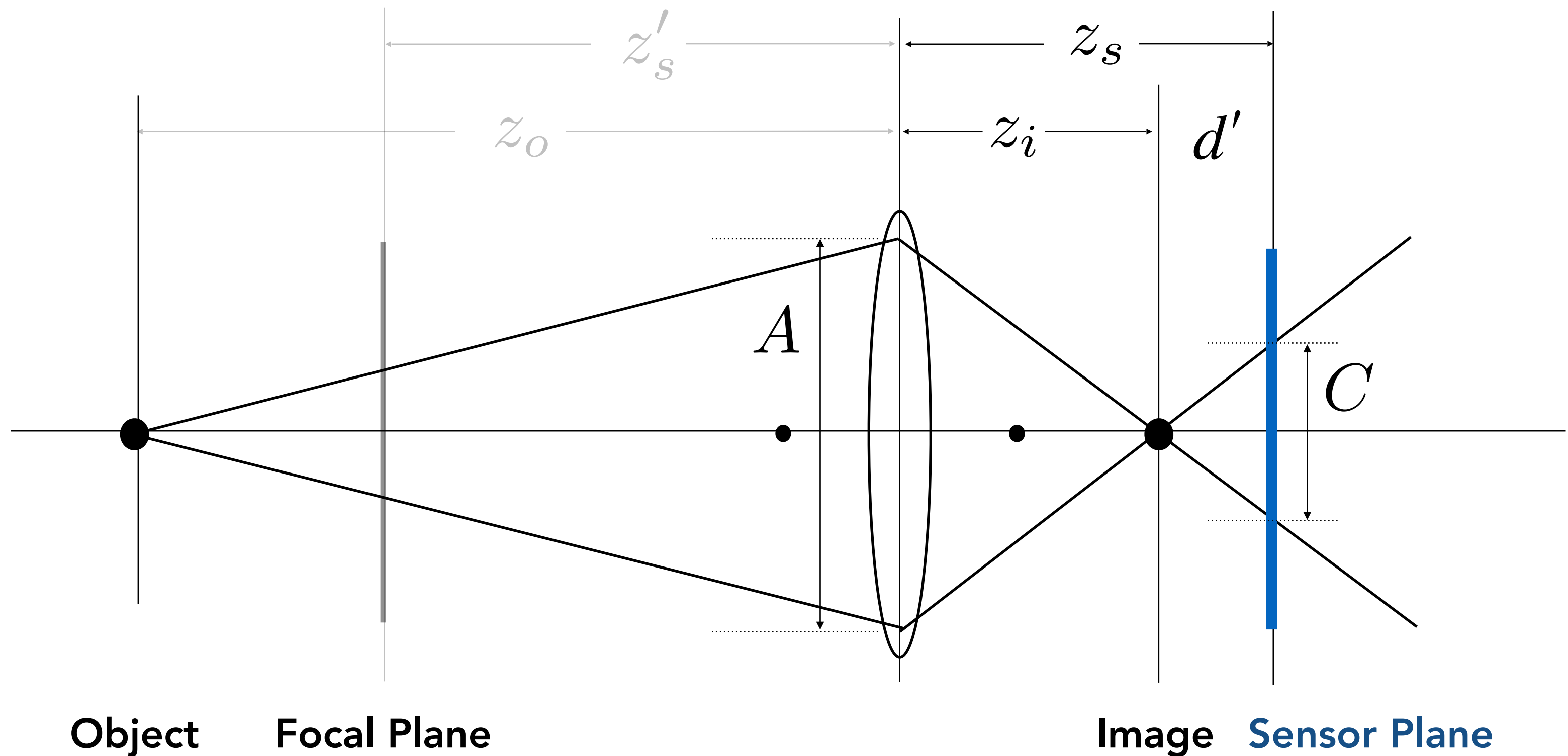
From London and Upton, and Canon EF Lens Work III

# Defocus Blur

# Defocus blur



# Computing Circle of Confusion Diameter (C)



**Circle of confusion is proportional to the size of the aperture**

$$\frac{C}{A} = \frac{d'}{z_i} = \frac{|z_s - z_i|}{z_i}$$

$$C = A \frac{|z_s - z_i|}{z_i}$$

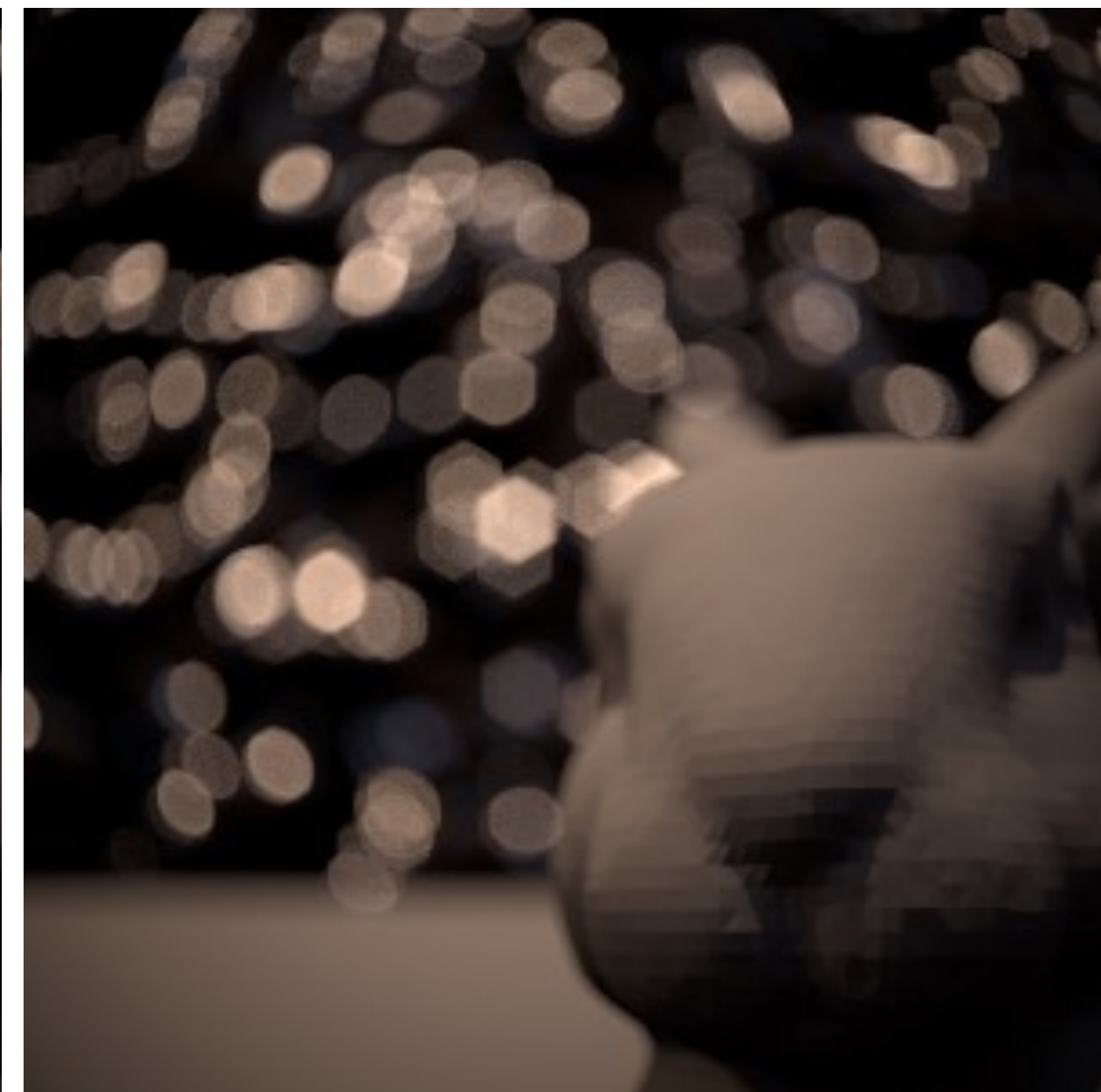
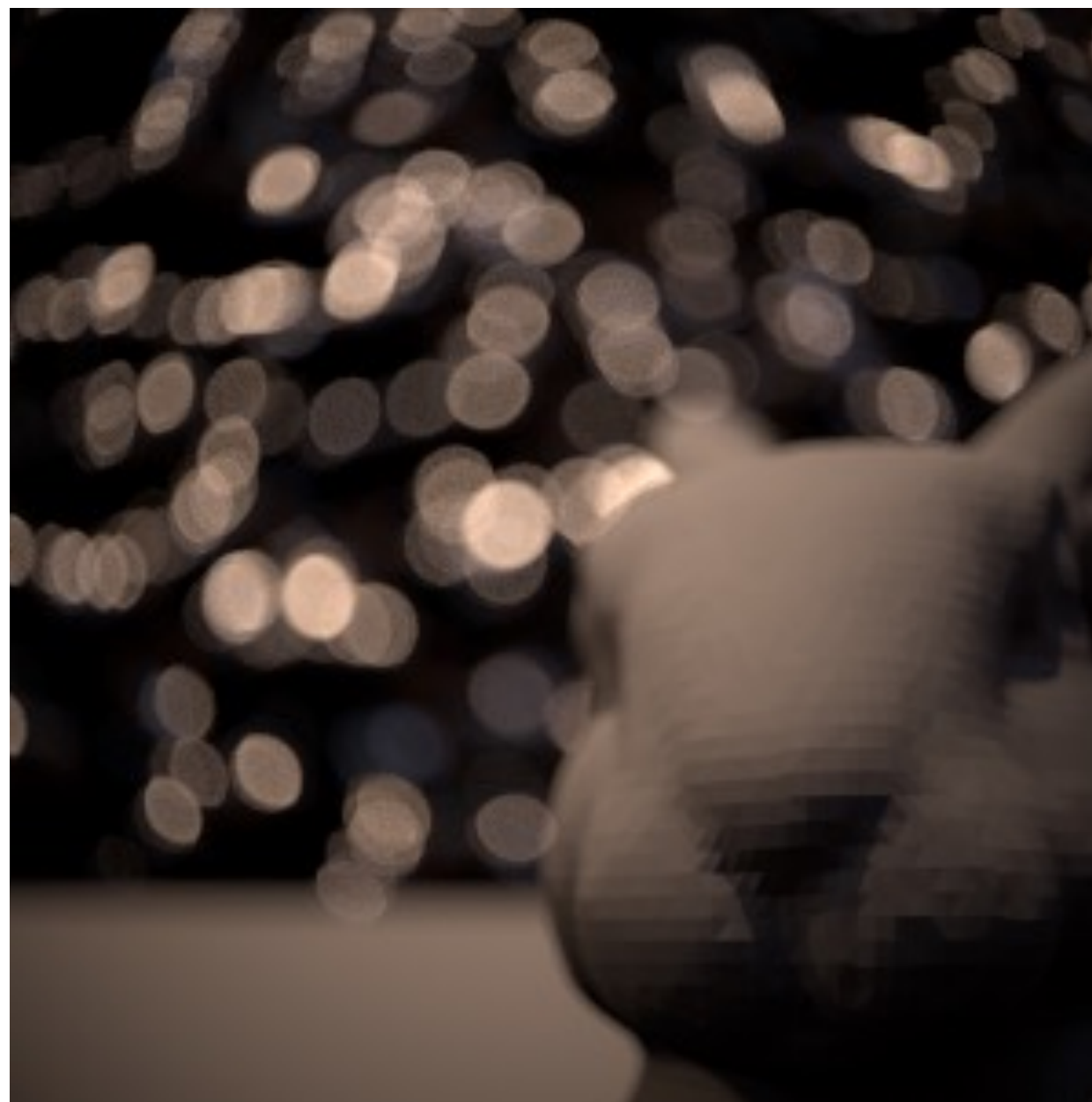
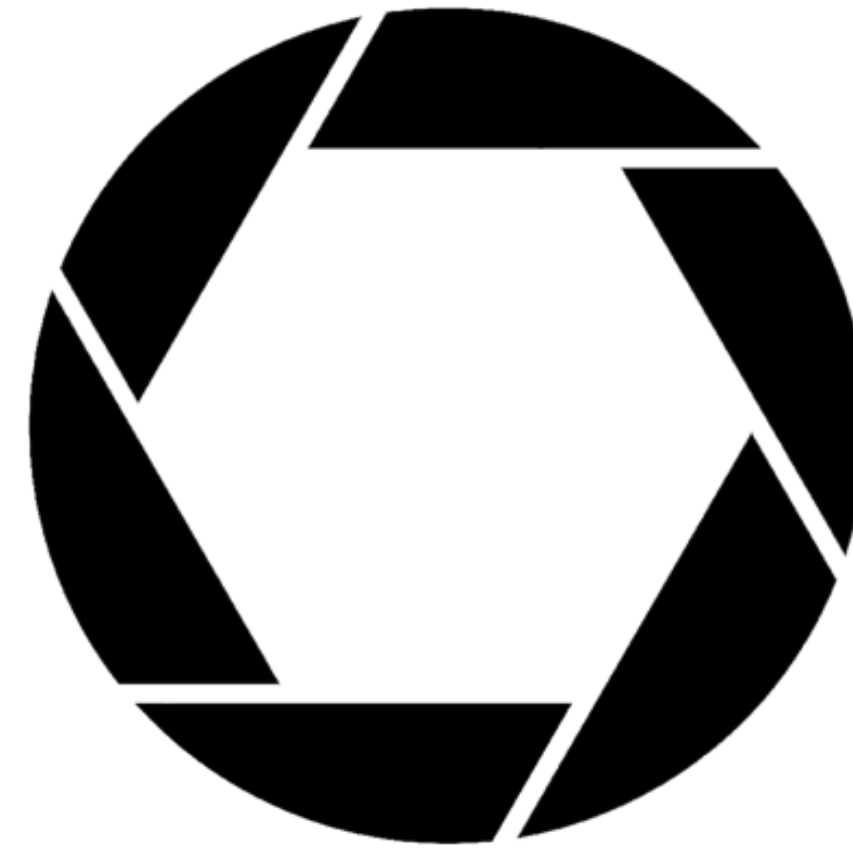


# Bokeh

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Photo credit: Wikimedia's The Photographer



# Bokeh

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**Bokeh is the shape and quality of out-of-focus blur**

- **For small, out-of-focus lights, bokeh takes on the shape of the lens aperture**



M Yashna, flickr, 40mm f/3.0

# Bokeh

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Dino Quinzani, Leica Noctilux 50mm, f/0.95

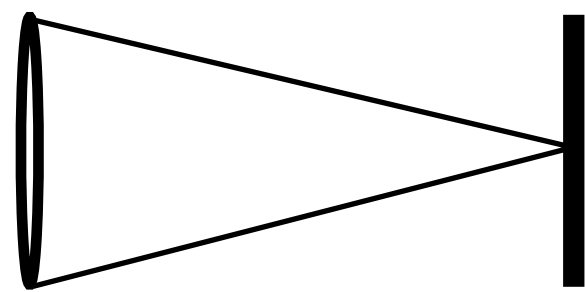
Why does the bokeh vary across the image?

# F Number

---

**A lens' F-number is the ratio of focal length ( $f$ ) to the maximum aperture diameter ( $A$ ) of the lens**

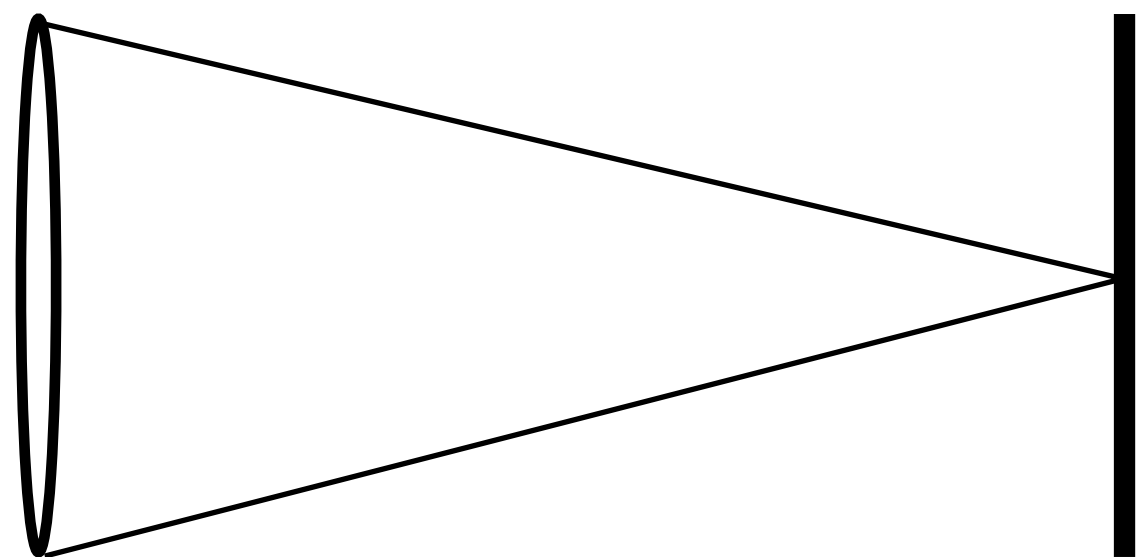
**Example: two lenses with the same F-number (Denoted as  $F/2$  or  $F:2$ )**



$$A = 50 \text{ mm}$$

$$f = 100 \text{ mm}$$

$$N = f/A = 2$$



$$A = 100 \text{ mm}$$

$$f = 200 \text{ mm}$$

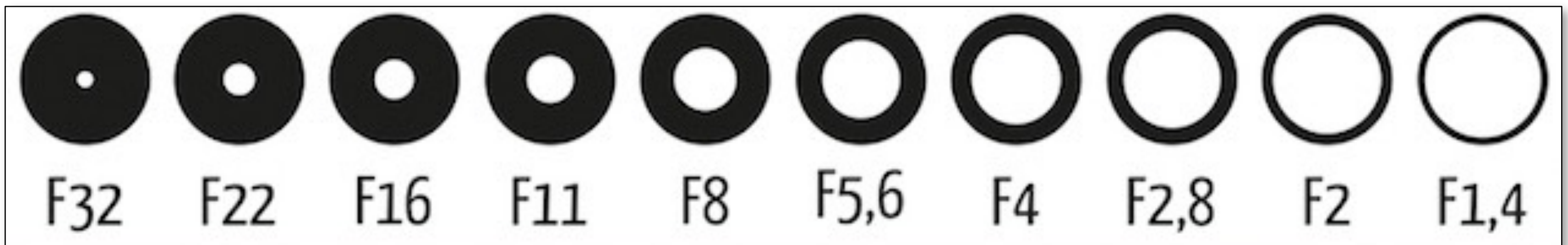
$$N = f/A = 2$$

# Lens's F-Number vs F-Number for Photo

---

But for an individual photo, the lens aperture may be “stopped down” to a smaller size

- E.g. 50 mm F/1.4 lens stopped down to F/4
- Aperture is closed down with an iris to  $50/4 = 12.5$  mm



# Size of Circle of Confusion is Inversely Proportional to F-Number for Photo



R. Berdan, [canadiannaturephotographer.com](http://canadiannaturephotographer.com)

$$C = A \frac{|z_s - z_i|}{z_i} = \frac{f}{N} \frac{|z_s - z_i|}{z_i}$$

# Ray Tracing Ideal Thin Lenses

# Rendering with Lens Focus

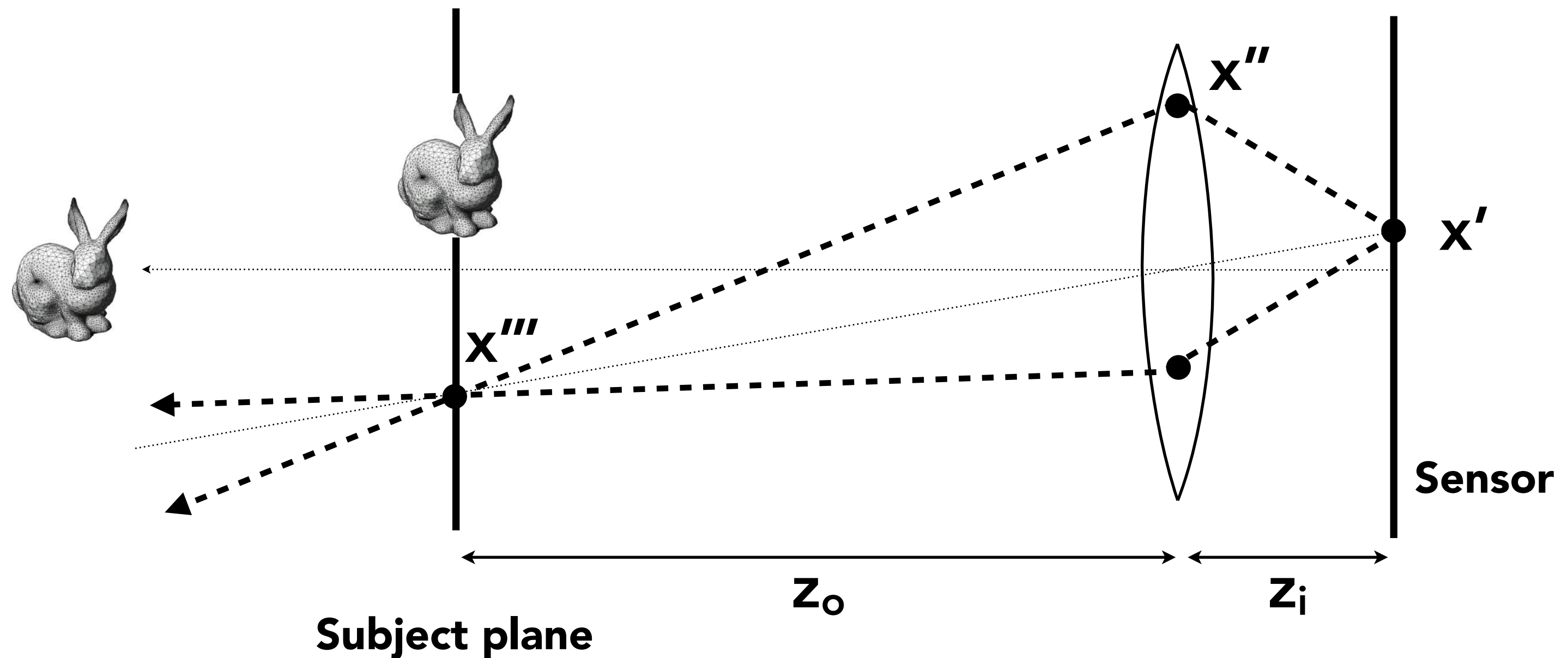
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Pharr and Humphreys



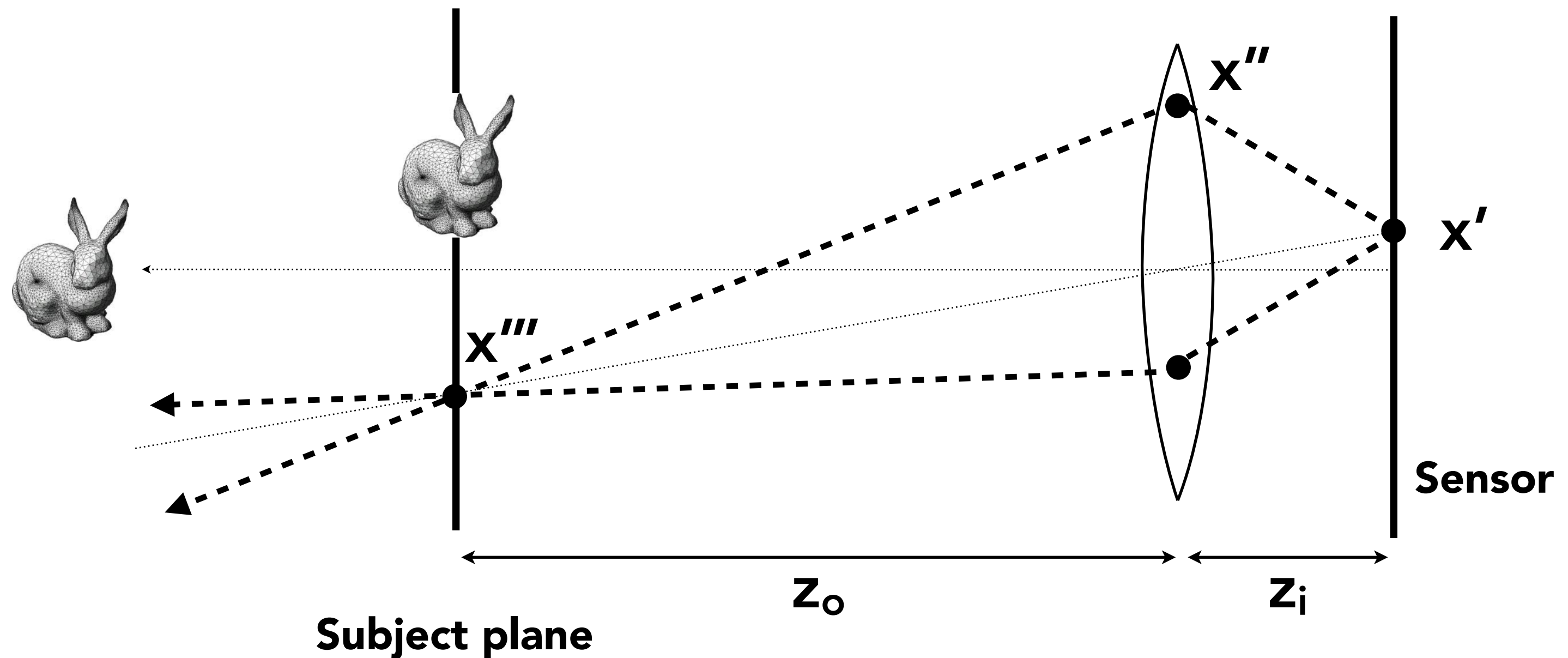
# Ray Tracing for Defocus Blur (Thin Lens)



## Setup:

- Choose sensor size, lens focal length and aperture size
- Choose depth of subject of interest  $z_o$ .
- Calculate corresponding depth of sensor  $z_i$  from thin lens equation (focusing)

# Ray Tracing for Defocus Blur (Thin Lens)



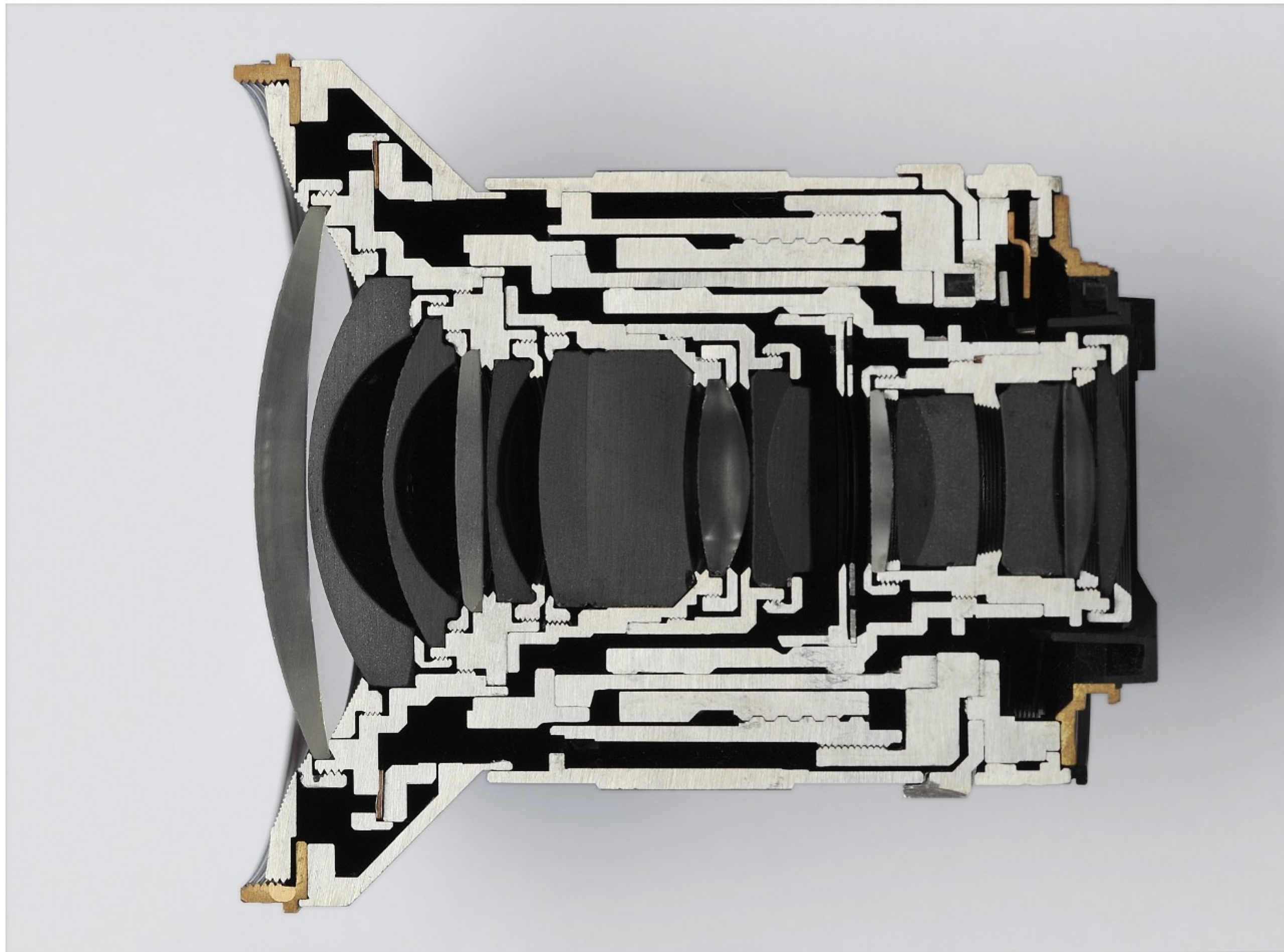
**To compute value of pixel at position  $x'$  by Monte Carlo integration:**

- Select random points  $x''$  on lens plane
- Rays pass from point  $x'$  on image plane  $z_i$  through points  $x''$  on lens
- Each ray passes through conjugate point  $x'''$  on the plane of focus  $z_o$ 
  - Can determine  $x'''$  from Gauss' ray diagram
  - So just trace ray from  $x''$  to  $x'''$
- Estimate radiance on rays using path-tracing, and sum over all points  $x''$

# **Real Compound Lenses**

# Modern Lens Designs Are Complex

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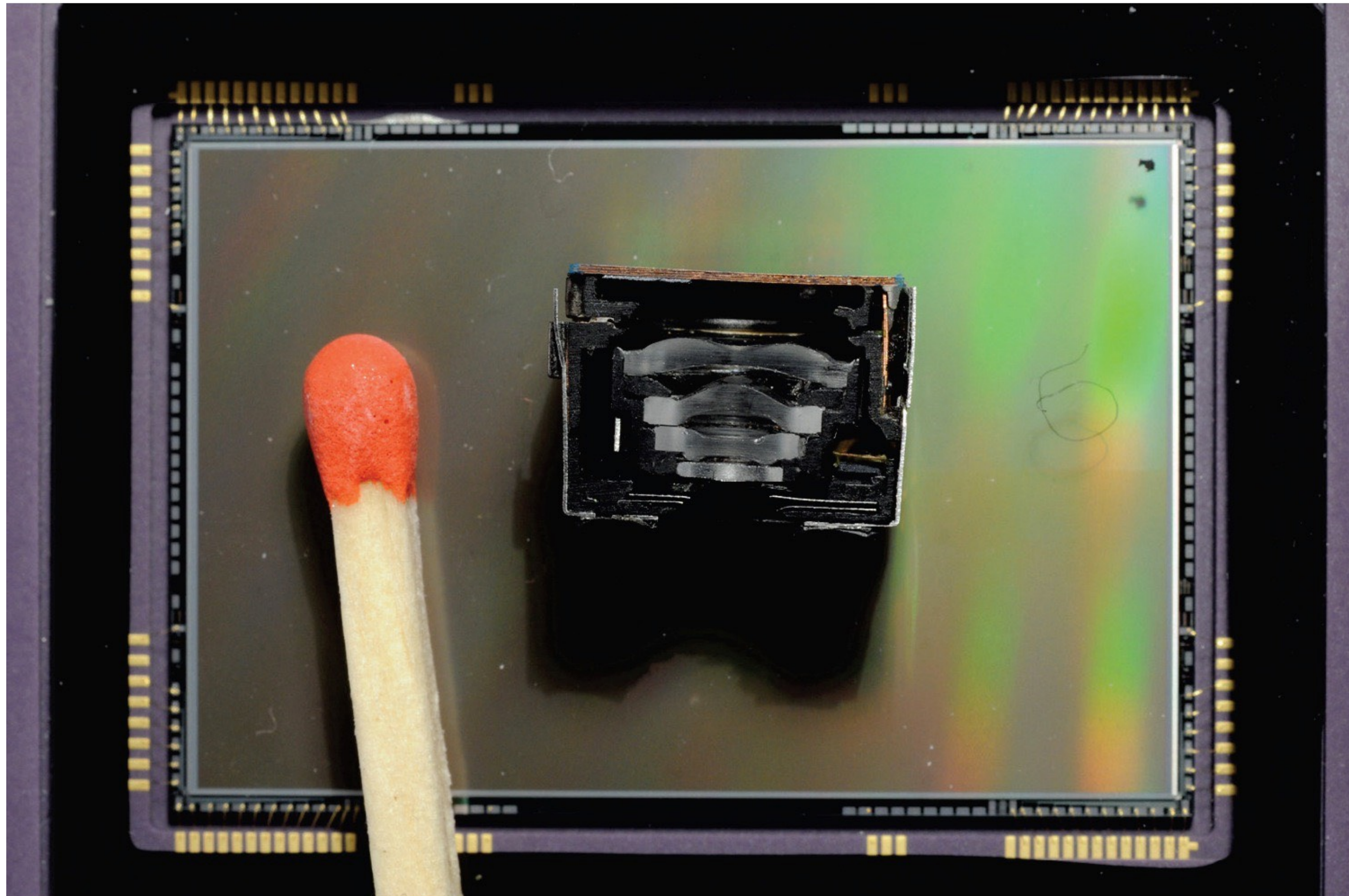


ilovephotography.com

**Photographic lens cross section**

# Modern Lens Designs Are Complex

---

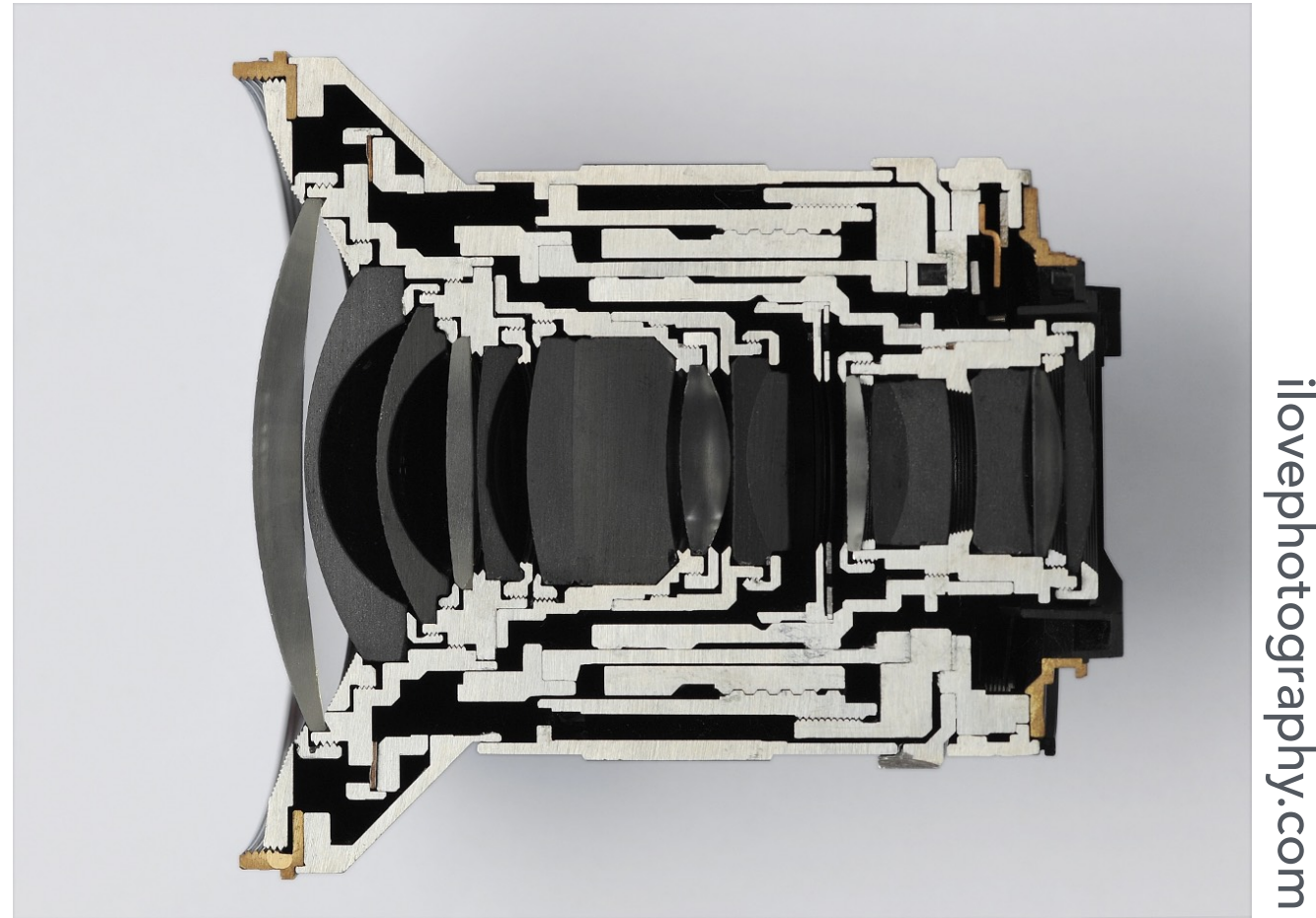


ilovehatephoto.com

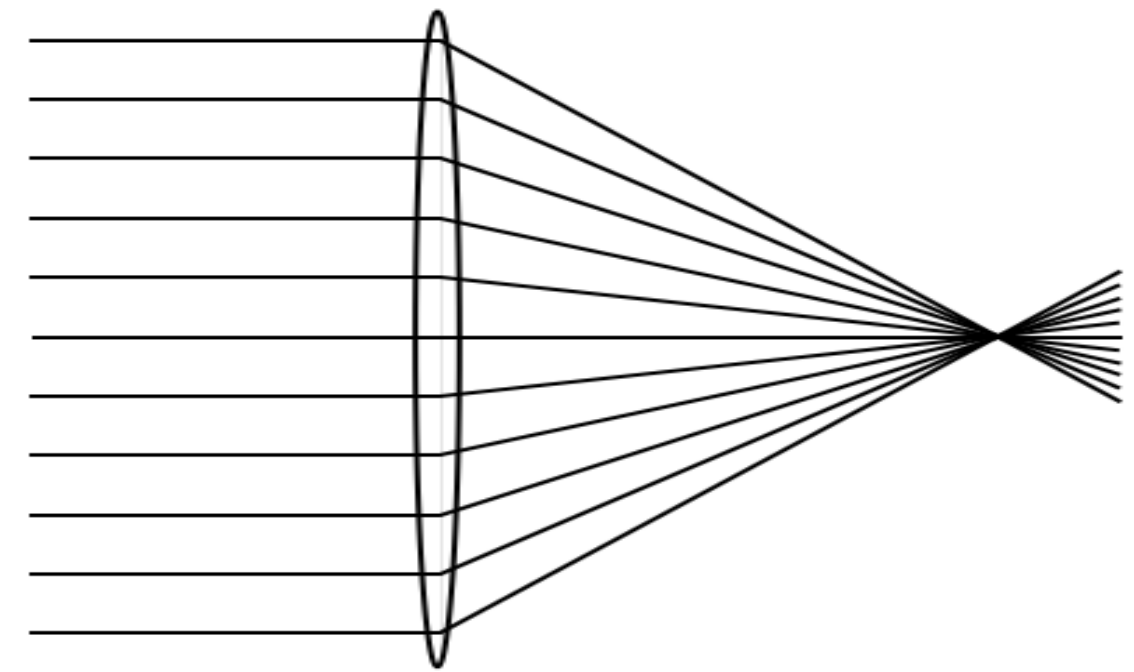
**4 element mobile phone lens (on 24x36mm sensor)**

# Real Lenses vs Ideal Thin Lenses

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- Real optical system
- Multiple physical elements in compound design
- Optical aberrations prevent rays from converging perfectly

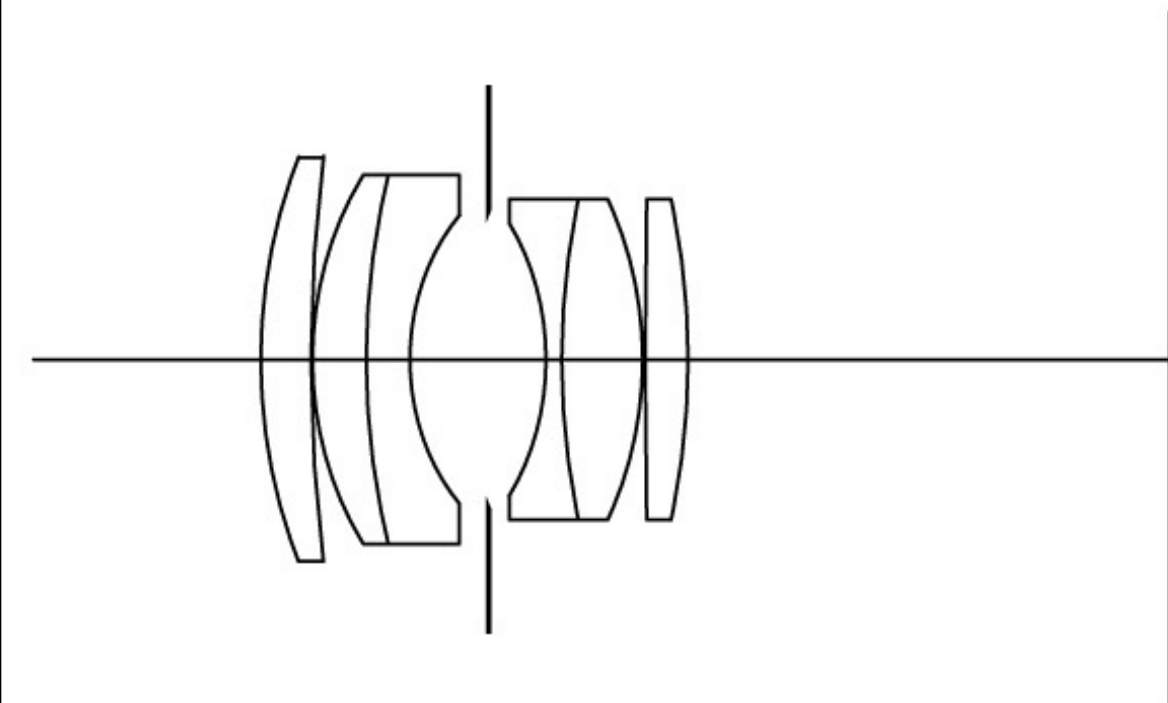


- Theoretical abstraction
- Assume all rays refract at a plane & converge to a point
- Quick and intuitive calculation of main imaging effects

# Double Gauss

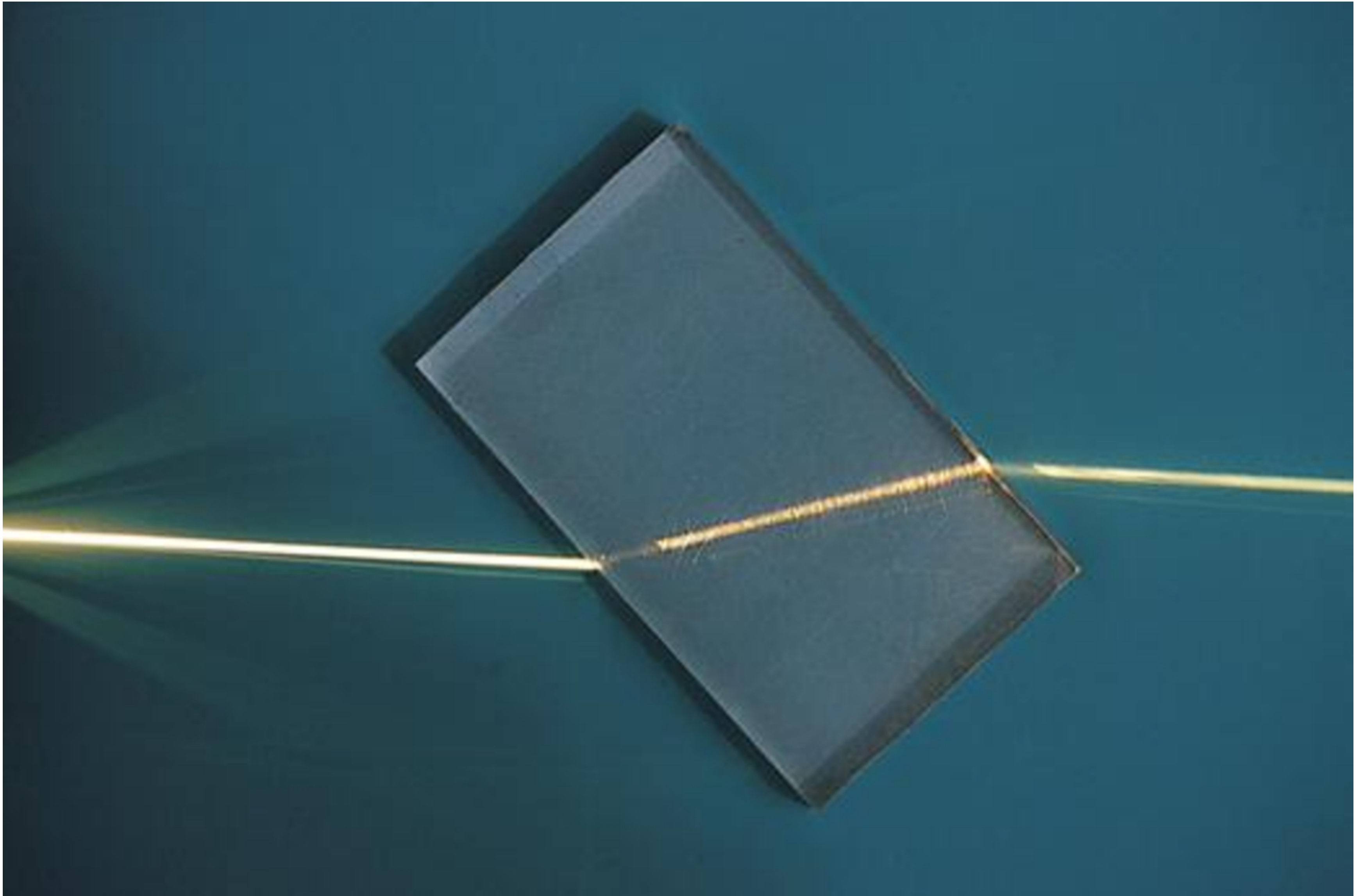
Data from W. Smith,  
Modern Lens Design, p 312

Radius	Thick	nd	V-no	aperture
58.950	7.520	1.670	47.1	50.4
169.660	0.240			50.4
38.550	8.050	1.670	47.1	46.0
81.540	6.550	1.699	30.1	46.0
25.500	11.410			36.0
	9.000			34.2
-28.990	2.360	1.603	38.0	34.0
81.540	12.130	1.658	57.3	40.0
-40.770	0.380			40.0
874.130	6.440	1.717	48.0	40.0
-79.460	72.228			40.0



# Refraction

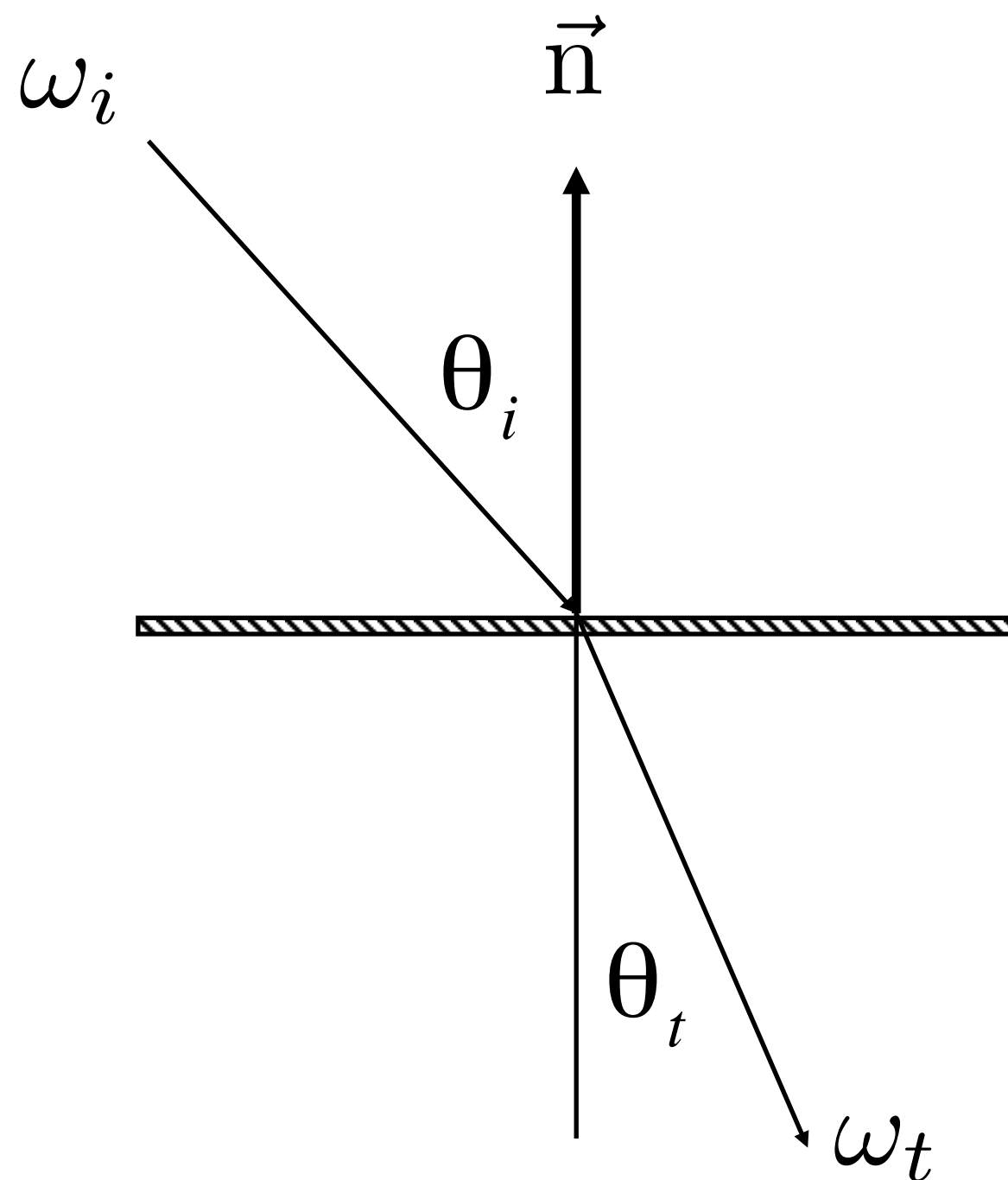
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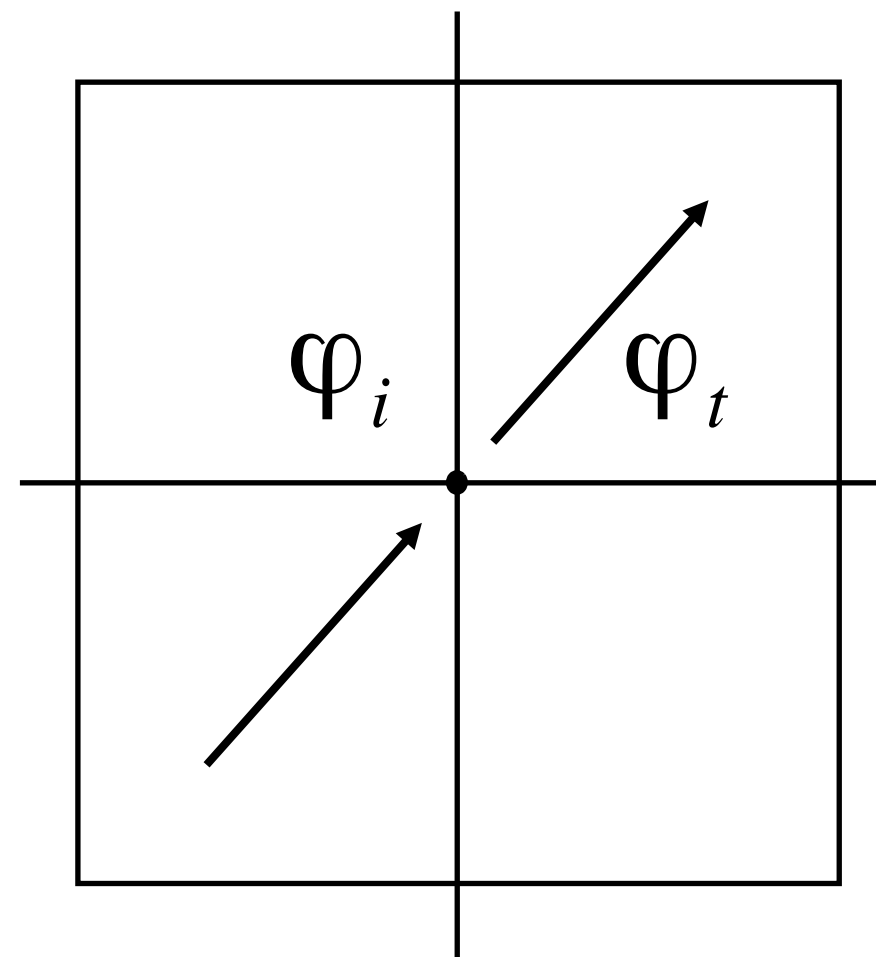


# Snell's Law

Transmitted angle depends on index of refraction of medium incident ray is in and index of refraction of medium light is entering.



$$\eta_i \sin \theta_i = \eta_t \sin \theta_t$$



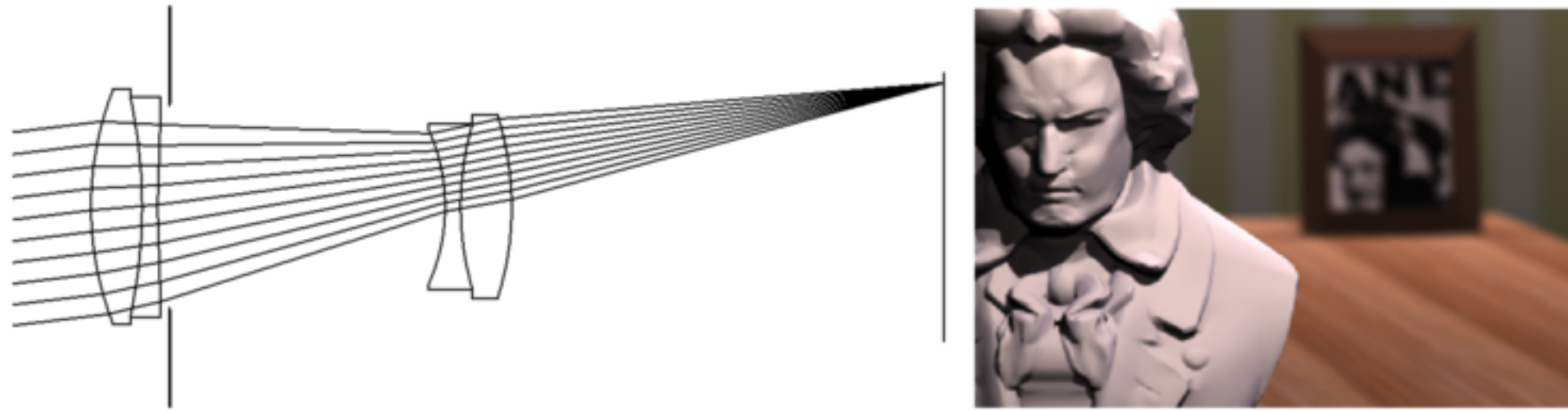
$$\varphi_t = \varphi_i \pm \pi$$

Medium	$\eta^*$
Vacuum	1.0
Air (sea level)	1.0002
Water (20 °C)	9
Glass	1.333
Diamond	1.5-1.6
	2.42

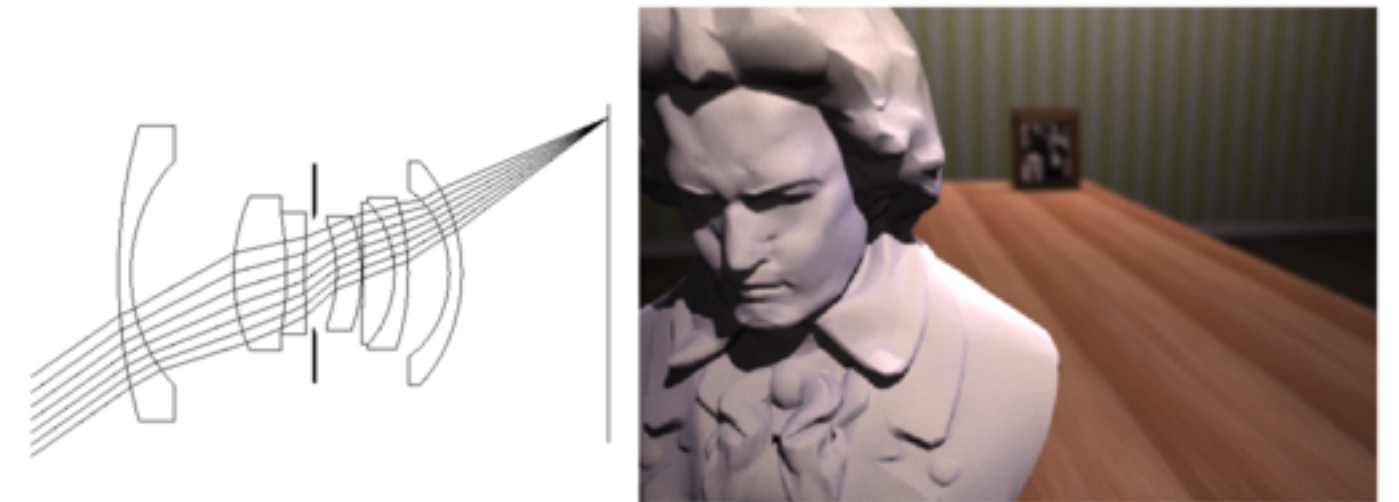
\* index of refraction is wavelength dependent (these are averages)

# Ray Tracing Through Lenses

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**200 mm telephoto**



**35 mm wide-angle**



**50 mm double-gauss**



**16 mm fisheye**

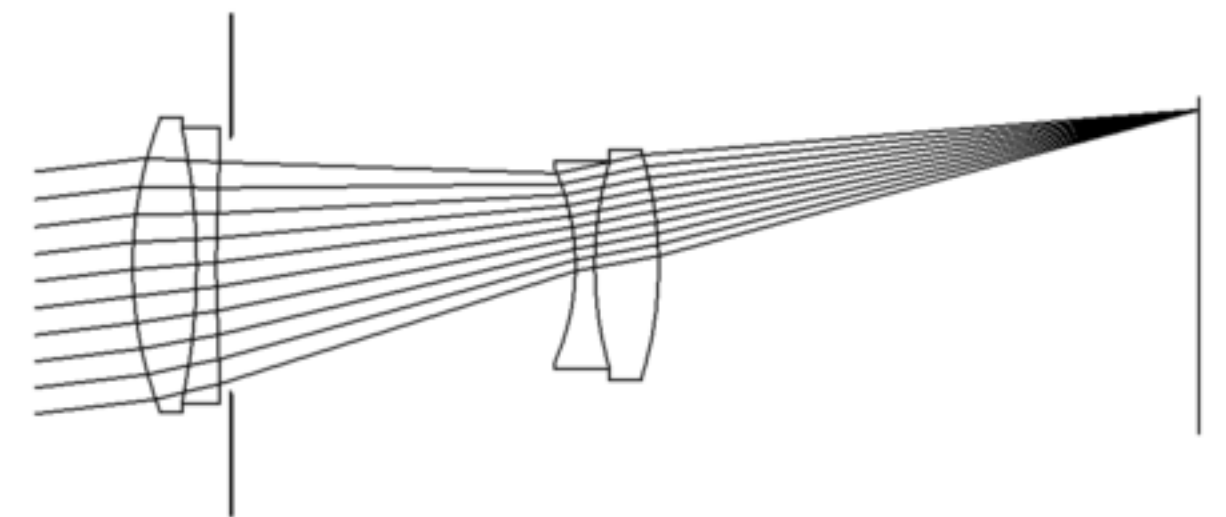
**From Kolb, Mitchell and Hanrahan (1995)**

# Ray Tracing Through Real Lens Designs

---



**200 mm telephoto**



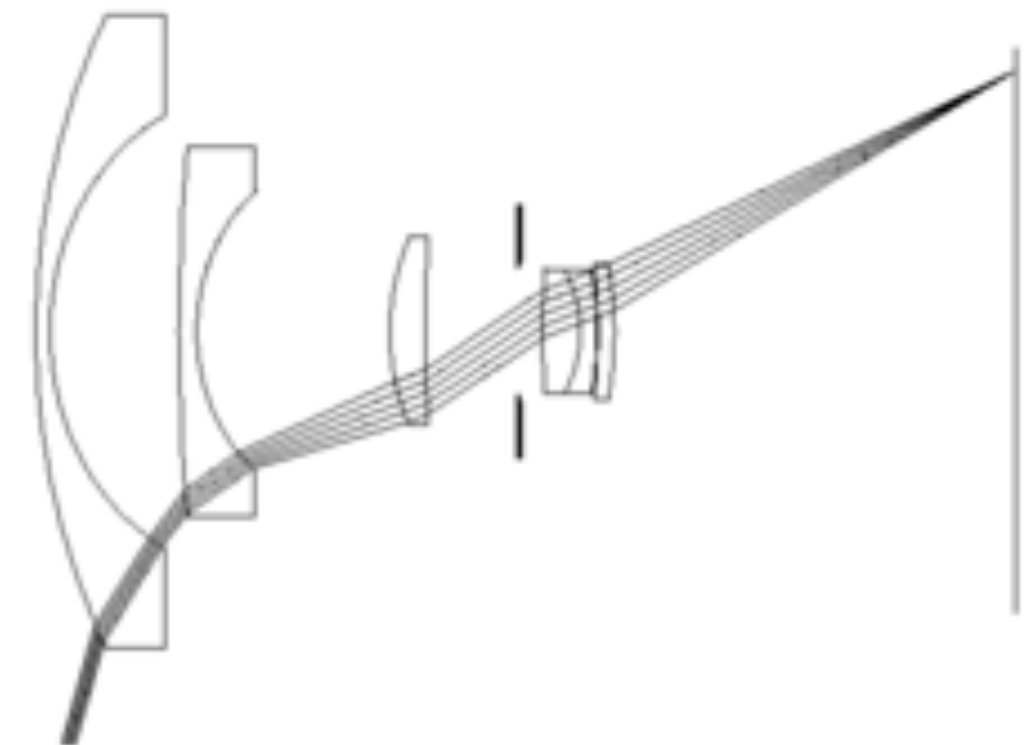
**Notice shallow depth of field (out of focus background)**

# Ray Tracing Through Real Lens Designs

---



**16 mm fisheye**



**Notice distortion in the corners (straight lines become curved)**

# Ray Tracing Through Real Lens Designs

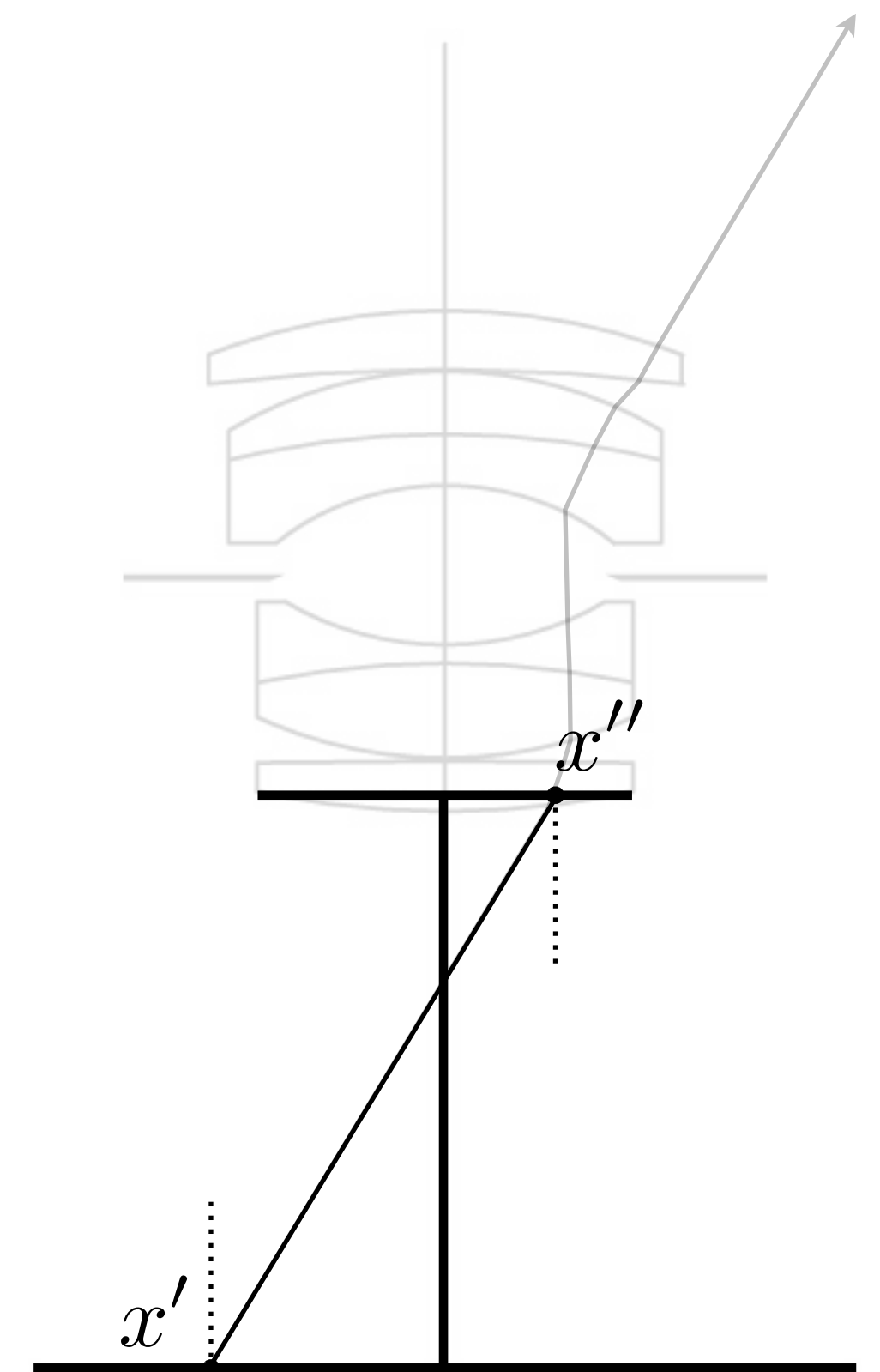
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## Monte Carlo approach

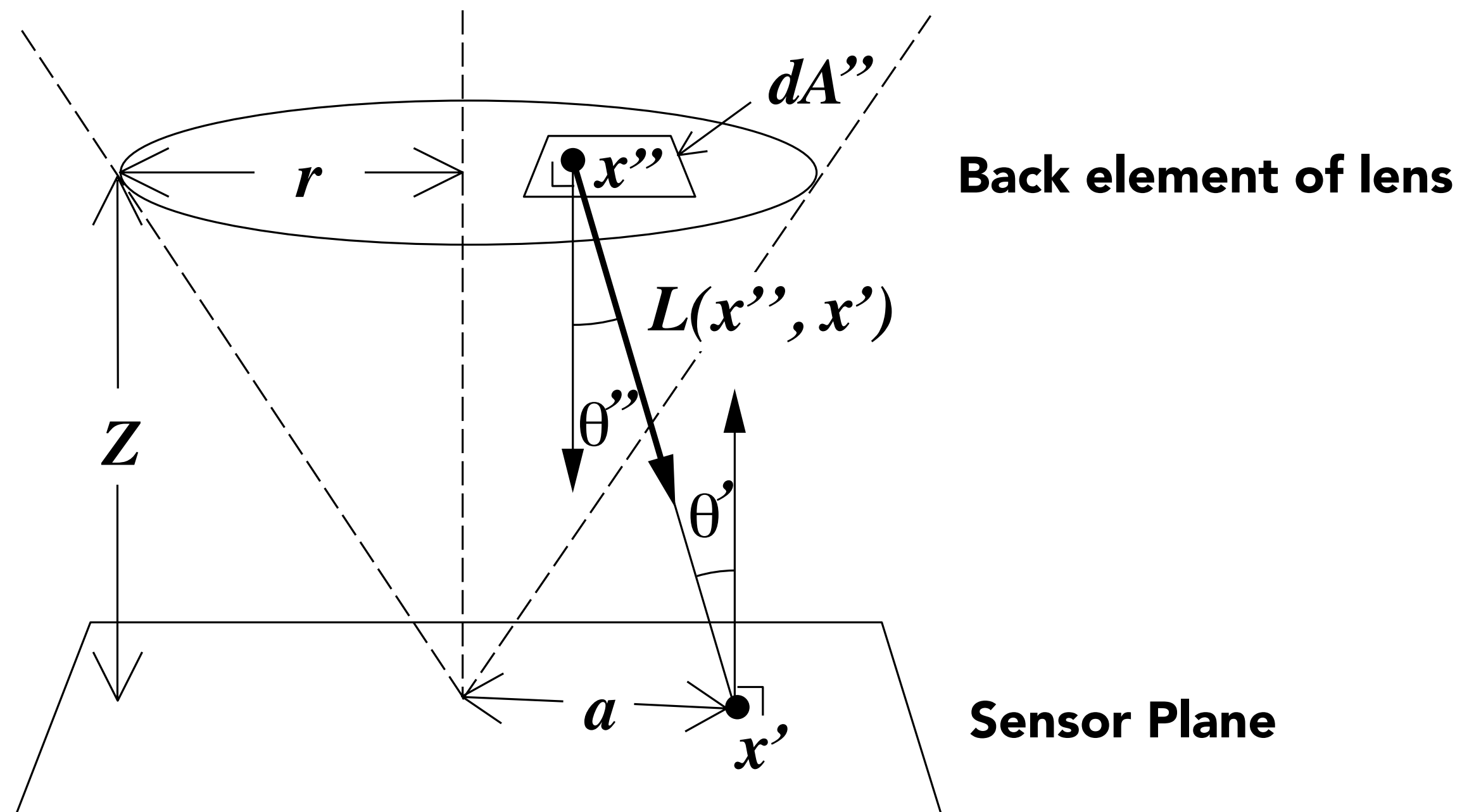
- **At every sensor pixel, compute integral of rays incident on pixel area arriving from all paths through the lens**

## Algorithm (for a pixel)

- **Choose  $N$  random positions in pixel**
- **For each position  $x'$ , choose a random position on the back element of the lens  $x''$**
- **Trace a ray through from  $x'$  to  $x''$ , trace refractions through lens elements until it misses the next element (kill ray) or exits the lens (path trace through the scene)**
- **Weight each ray according to radiometric calculation on next slide to estimate irradiance  $E(x')$**



# Radiometry for Tracing Lens Designs

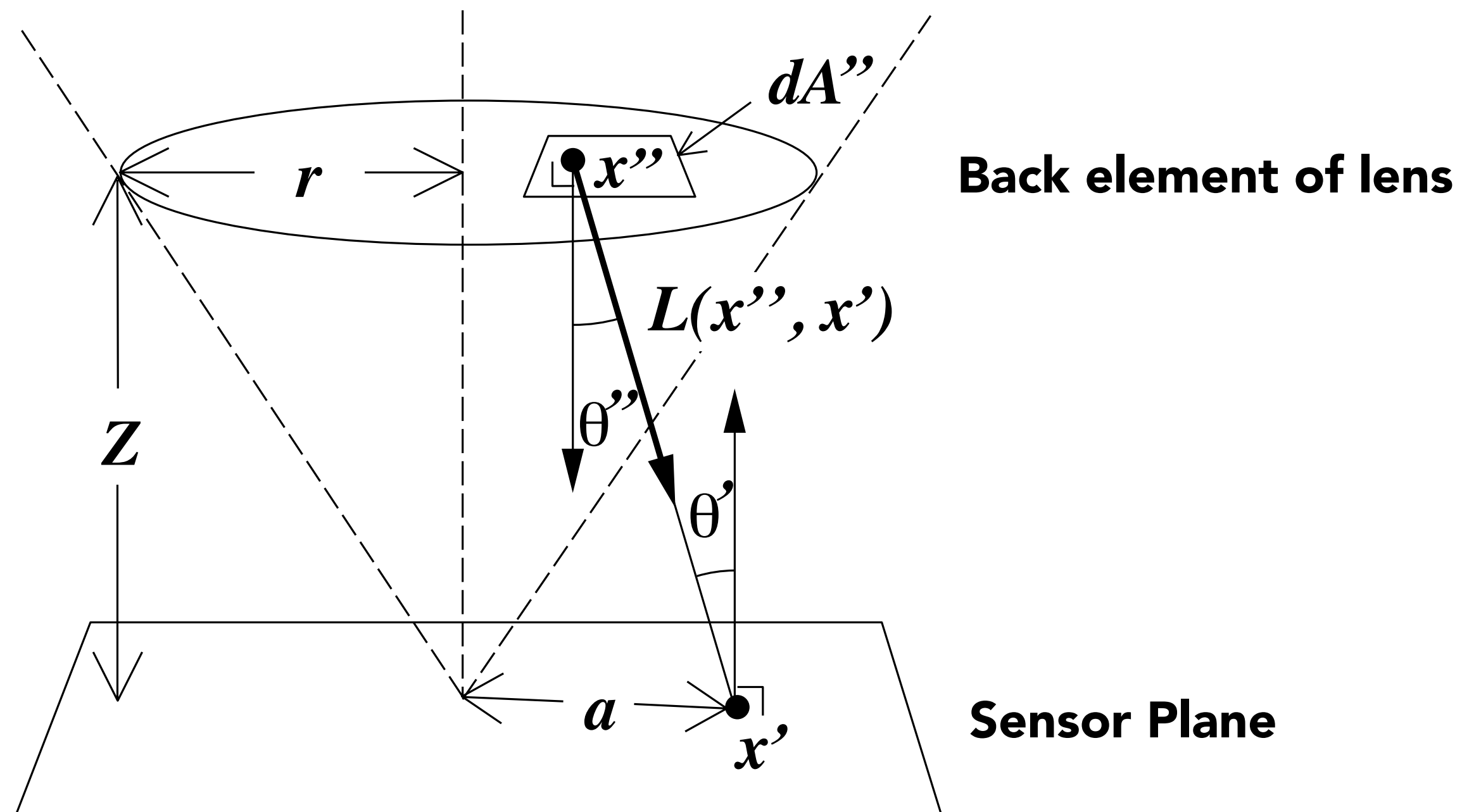


$$E(x') = \int_{x'' \in D} L(x'' \rightarrow x') \frac{\cos \theta' \cos \theta''}{\|x'' - x'\|^2} dA''$$

$$= \frac{1}{Z^2} \int_{x'' \in D} L(x'' \rightarrow x') \cos^4 \theta dA''$$

**D = region of lens aperture**

# Real sensor: pixel measurement integrates irradiance over area of pixel



$$E(\text{pixel}) = \int_{x' \in P} \int_{x'' \in D} L(x'' \rightarrow x') \frac{\cos \theta' \cos \theta''}{\|x'' - x'\|^2} dA'' dA'$$

**P** = region of pixel

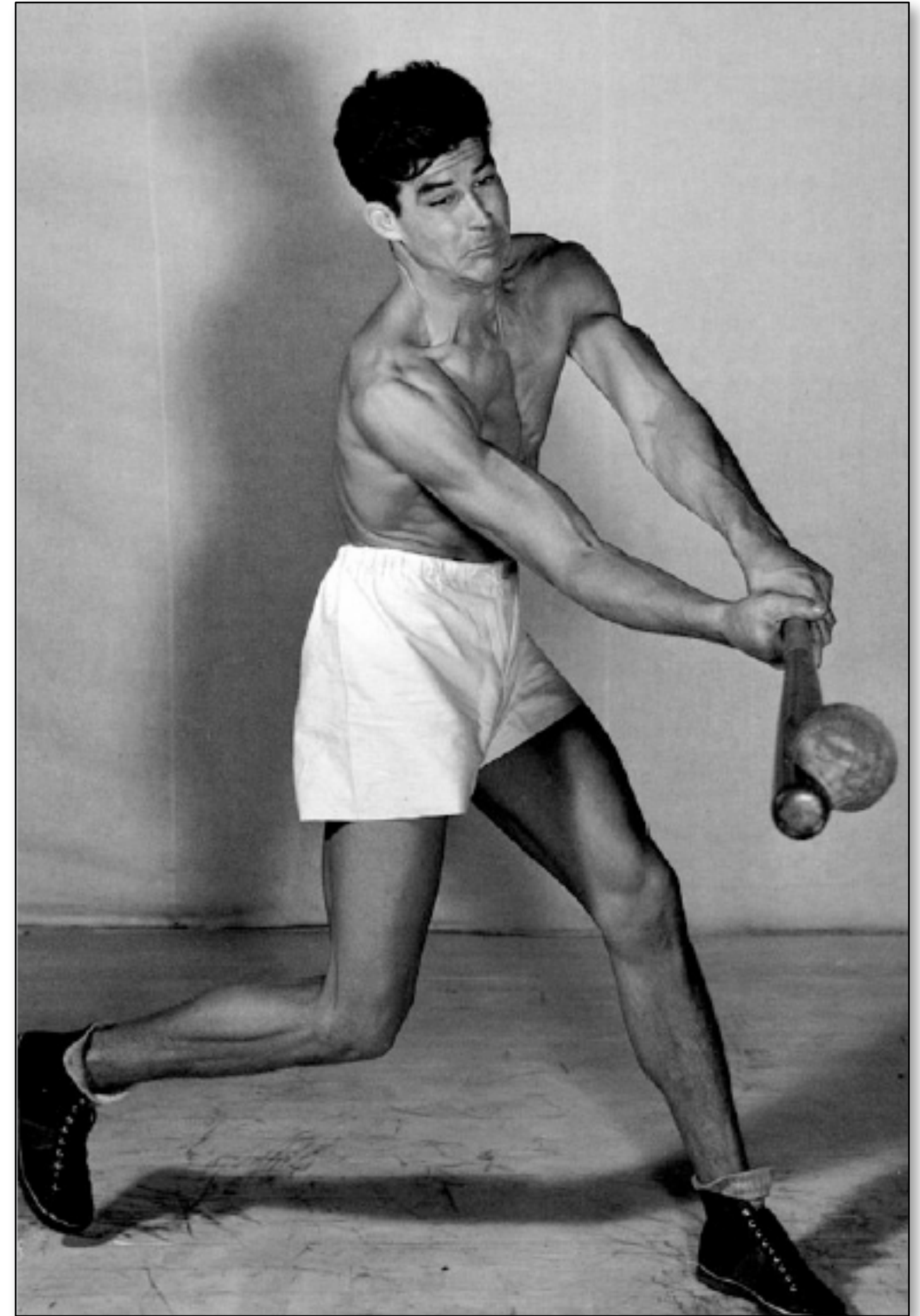
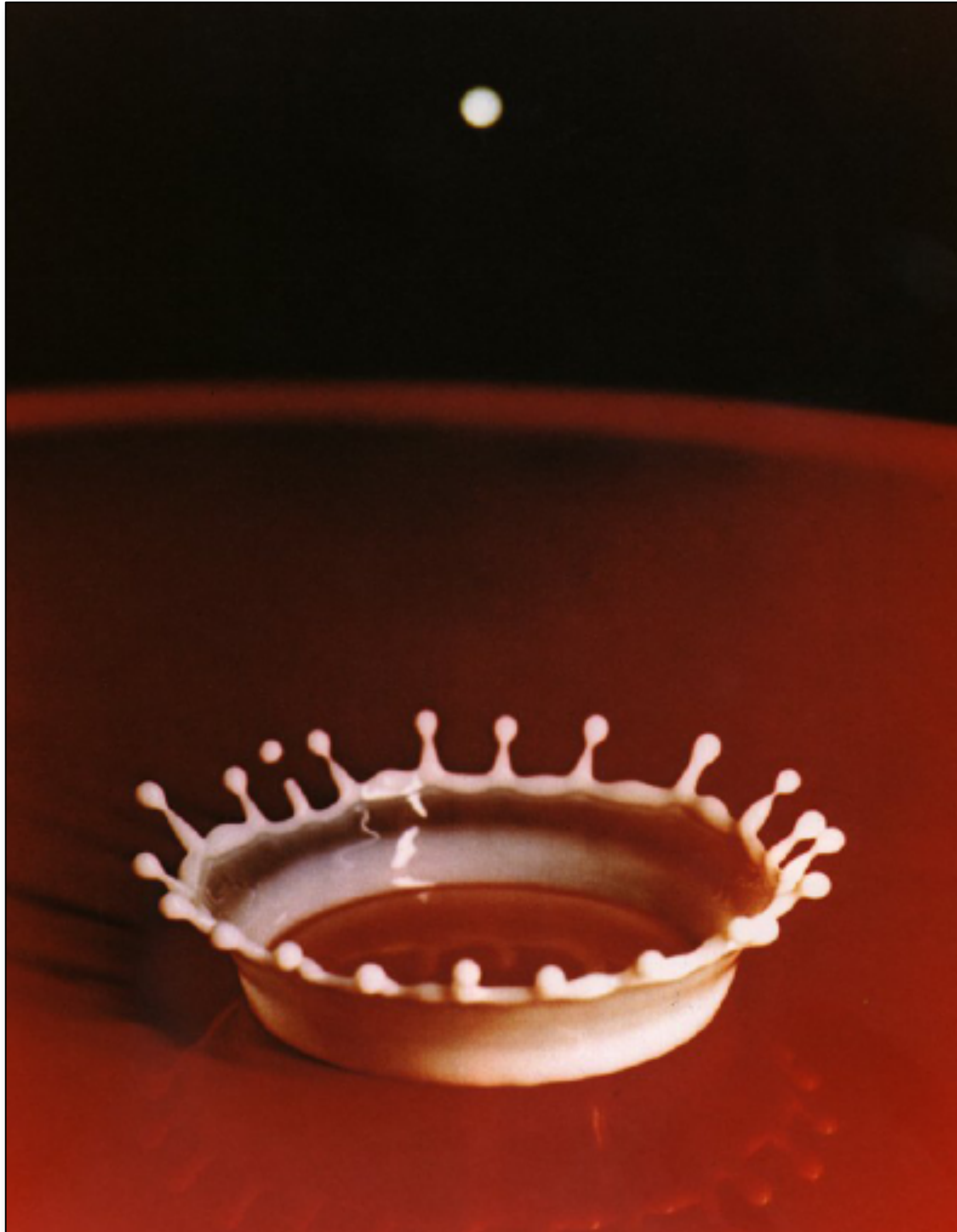
**D** = region of lens aperture

# Exposure



# High-Speed Photography (short exposure)

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# Long exposure

(a bad photo by Kayvon)

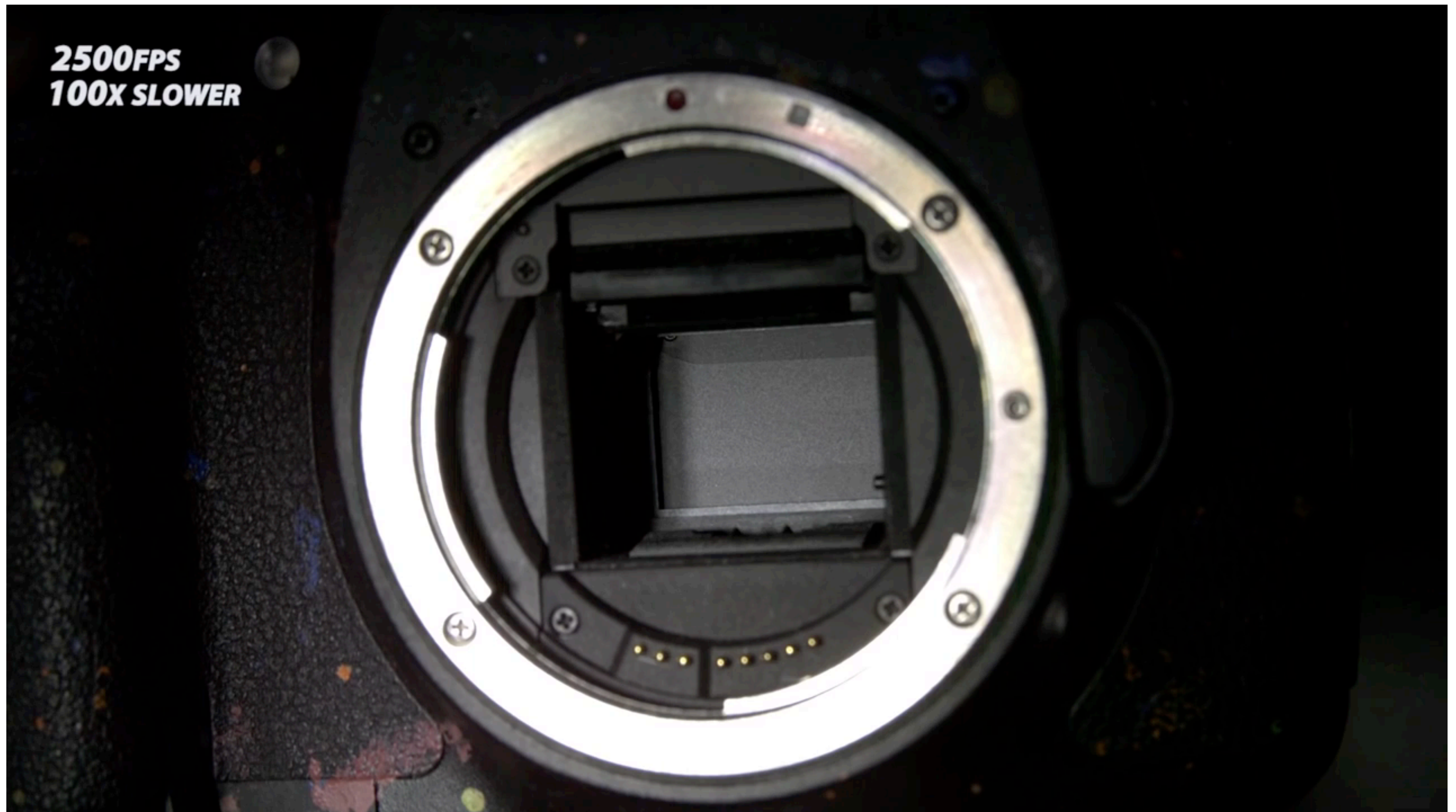


# Long exposure

(intentional for artistic effect)

# Physical Shutter (1/25 Sec Exposure)

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The Slow Mo Guys, <https://youtu.be/CmjeCchGRQo>

# Main Side Effect of Shutter Speed

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**Motion blur: handshake, subject movement**

**Doubling shutter time doubles motion blur**

Slow shutter speed



Fast shutter speed



London

# Electronic (Rolling) Shutter

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- **Pixel is electronically reset to start exposure**
- **Fills with photoelectrons as light falls on sensor**
- **Reading out pixel electronically “ends” exposure**
- **Problem: most sensors read out pixels sequentially, takes time (e.g. 1/30 sec) to read entire sensor**
  - **If reset all pixels at the same time, last pixel read out will have longer exposure**
  - **So, usually stagger reset of pixels to ensure uniform exposure time**
  - **Problem: rolling shutter artifact**

# Electronic Rolling Shutter

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Can you explain these images?



Credit: David Adler, B&H Photo Video

<https://www.bhphotovideo.com/explora/video/tips-and-solutions/rolling-shutter-versus-global-shutter>



Credit: Soren Ragsdale

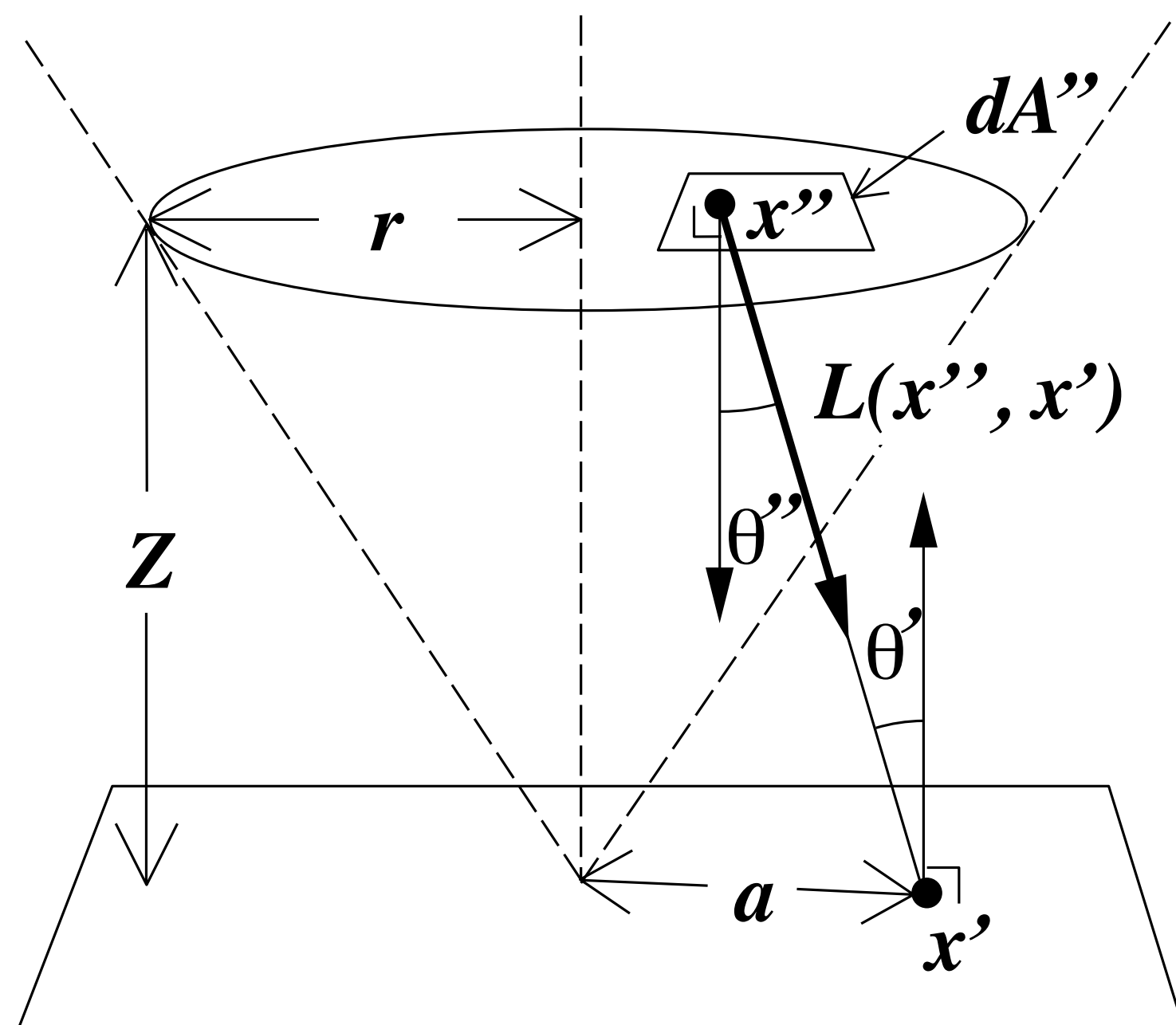
<https://flic.kr/p/5S6rKw>

# Exposure (Q)

**Pixels integrate (time varying) irradiance over time  
(5D integral)**

$$Q(\text{pixel}) = \int_{t \in T} E(\text{pixel}, t) dt$$

$$Q(\text{pixel}) = \int_{t \in T} \int_{x' \in P} \int_{x'' \in D} L(x'' \rightarrow x', t) \frac{\cos \theta' \cos \theta''}{\|x'' - x'\|^2} dA'' dA' dt$$





# Exposure

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- **Exposure (Q) is an integral of irradiance over time**
- **Exposure time (T)**
  - **Controlled by shutter**
- **Irradiance (E)**
  - **Controlled by lens aperture**
- **Implication: can increase exposure by increasing exposure time or by increasing aperture**
  - **Aperture: f-stop - 1 "stop" doubles Q**
    - Note: Also decreases depth of field**
  - **Shutter: Doubling the open time doubles Q**
    - Note: Increases motion blur**

# Aperture vs Shutter

Constant Exposure



**f/16**  
**1/8s**



**f/4**  
**1/125s**

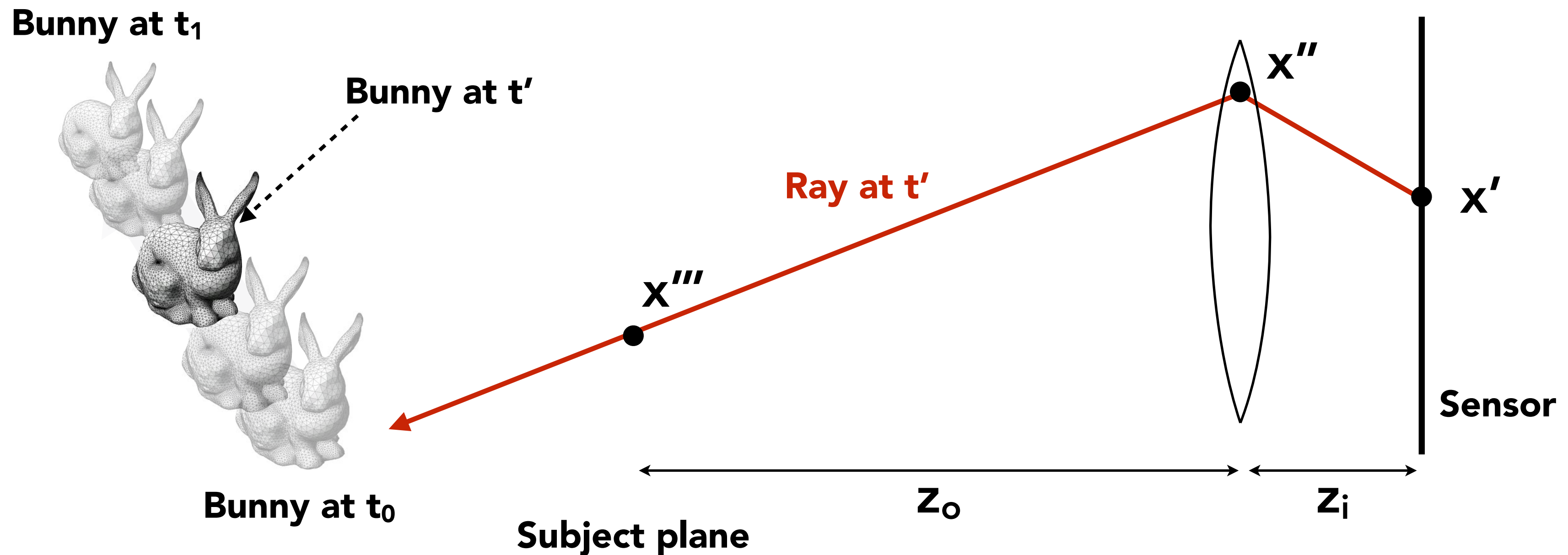


**f/2**  
**1/500s**

**From London and Upton**

# Ray tracing with motion blur

# Ray Tracing for Defocus Blur (Thin Lens)



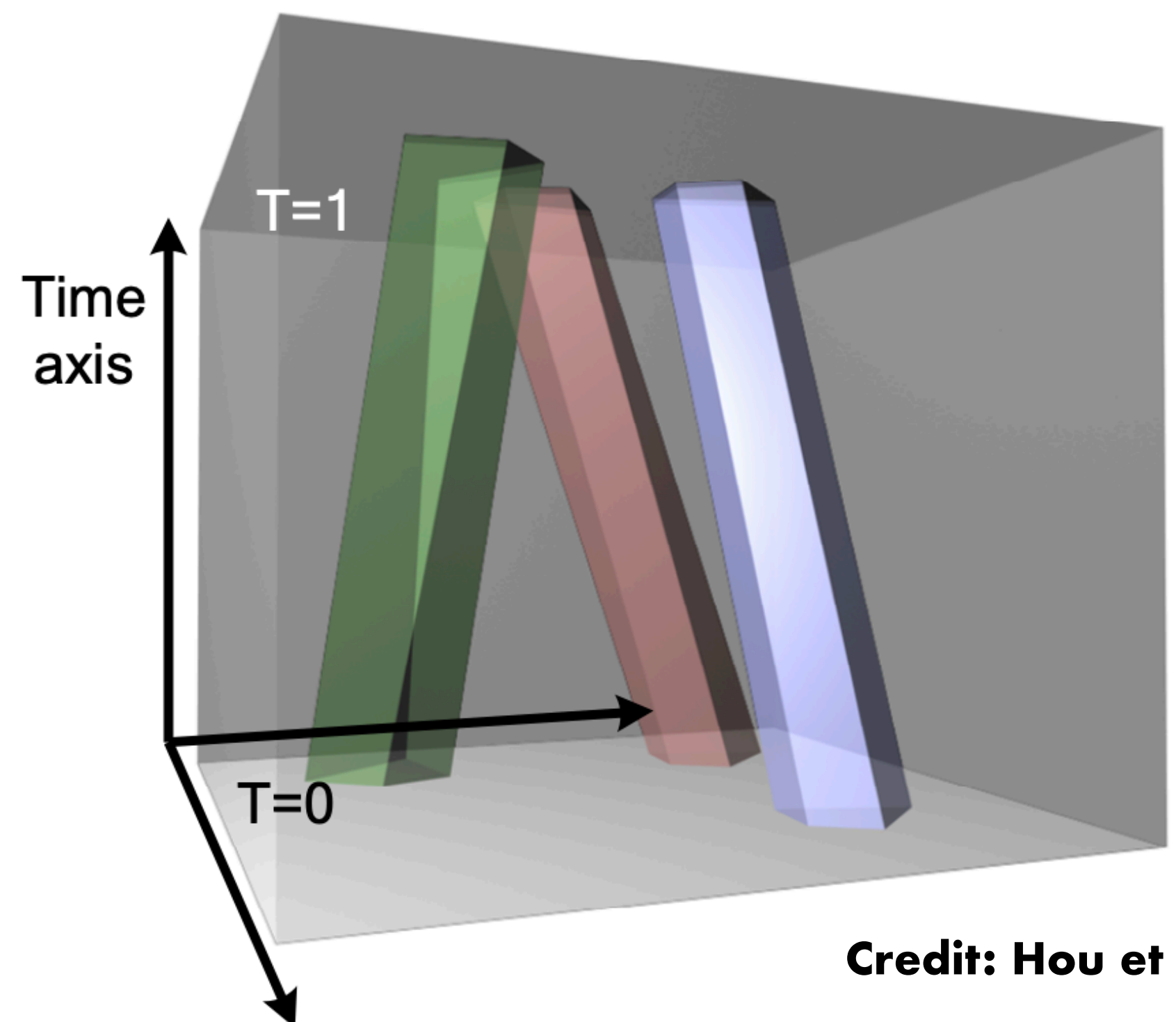
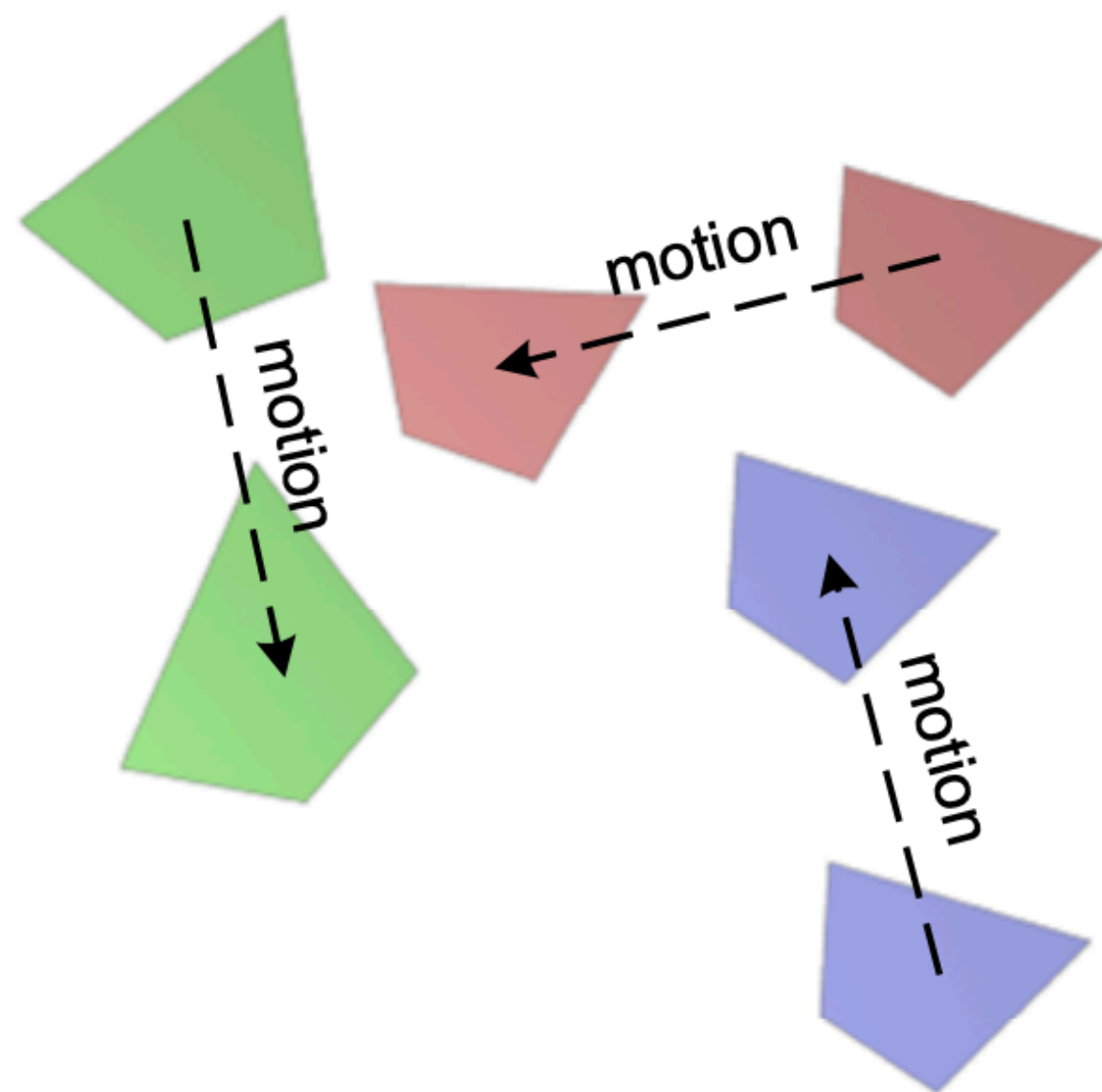
**To compute value of pixel at position  $x'$  by Monte Carlo integration:**

- **Select random time  $t'$  for ray (in addition to  $x''$  on lens aperture)**
- **Trace ray through lens system (or use thin lens approximation)**
- **Update scene geometry to its position at  $t'$**
- **Ray trace through BVH of geometry at  $t'$**

# BVH traversal with motion blur

**Assume: all primitives provide vertex positions at  $t_0$  (open shutter time) and  $t_1$  (close shutter time)**

**Assume vertices move linearly during shutter interval**



Credit: Hou et al.

# BVH traversal with motion blur

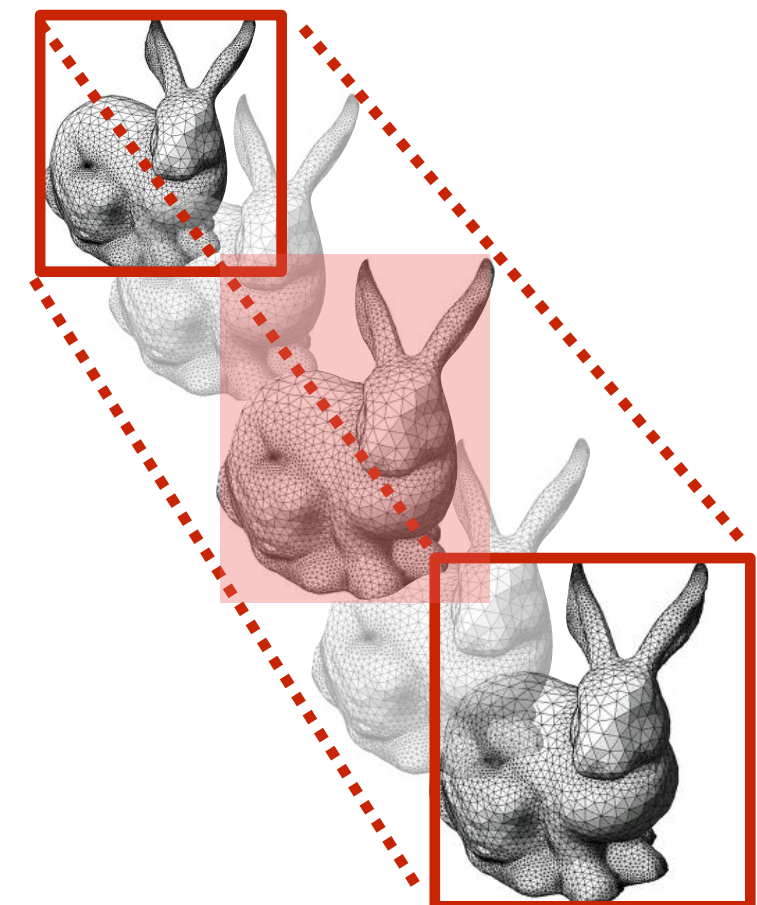
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**BVH construction: compute triangle bbox for  $t_0$  and  $t_1$ . Use  $\text{union}(\text{bbox}_{t_0}, \text{bbox}_{t_1})$  as the triangle's bbox during regular SAH-based BVH construction.**

**Each BVH node stores its  $\text{bbox}_{t_0}$  and  $\text{bbox}_{t_1}$ .**

**During traversal: given ray at time  $t$ :**

- **Compute  $\text{bbox}(n)_t$  for node  $n$  at time  $t$  via linear interpolation of  $\text{bbox}(n)_{t_0}$  and  $\text{bbox}(n)_{t_1}$ .**
- **Intersect ray with  $\text{bbox}(n)_t$  as normal**



# Challenges

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**Linear motion over a frame may be insufficient to capture fast non-linear motions. (e.g, walk cycles, rotating wheels)**



Credit: Houdini docs

1 linear segment

4 segments

9 segments

**Solution: piecewise linear motion approximation — store multiple sets of vertex positions over shutter interval**

**Memory cost: must store many bboxes for each node in BVH**

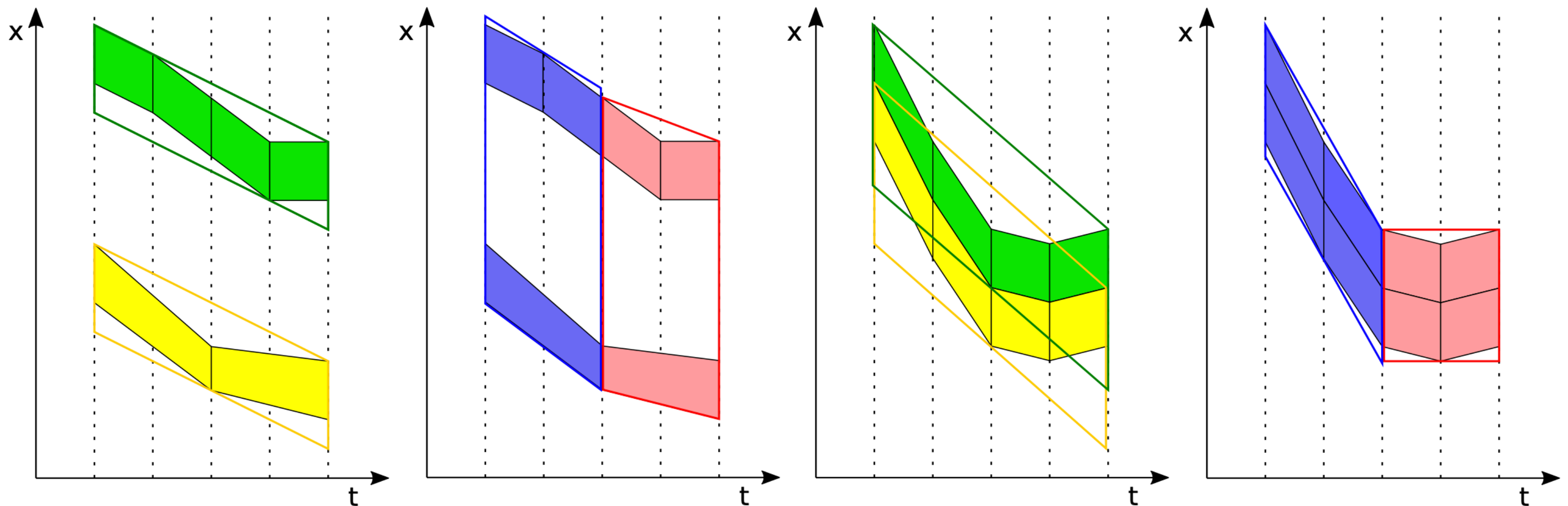
# Challenges

**Fast motion can significantly bloat primitive bounds used for SAH, resulting in inefficient BVH trees**

**Idea: enhance splitting algorithm to partition time as well as objects**

**BVH nodes now have both space and time bounds.**

**(Ray misses box if ray's  $t$  does not overlap box's time bound)**



(a) Example 1: Object partitioning

(b) Example 1: Temporal partitioning

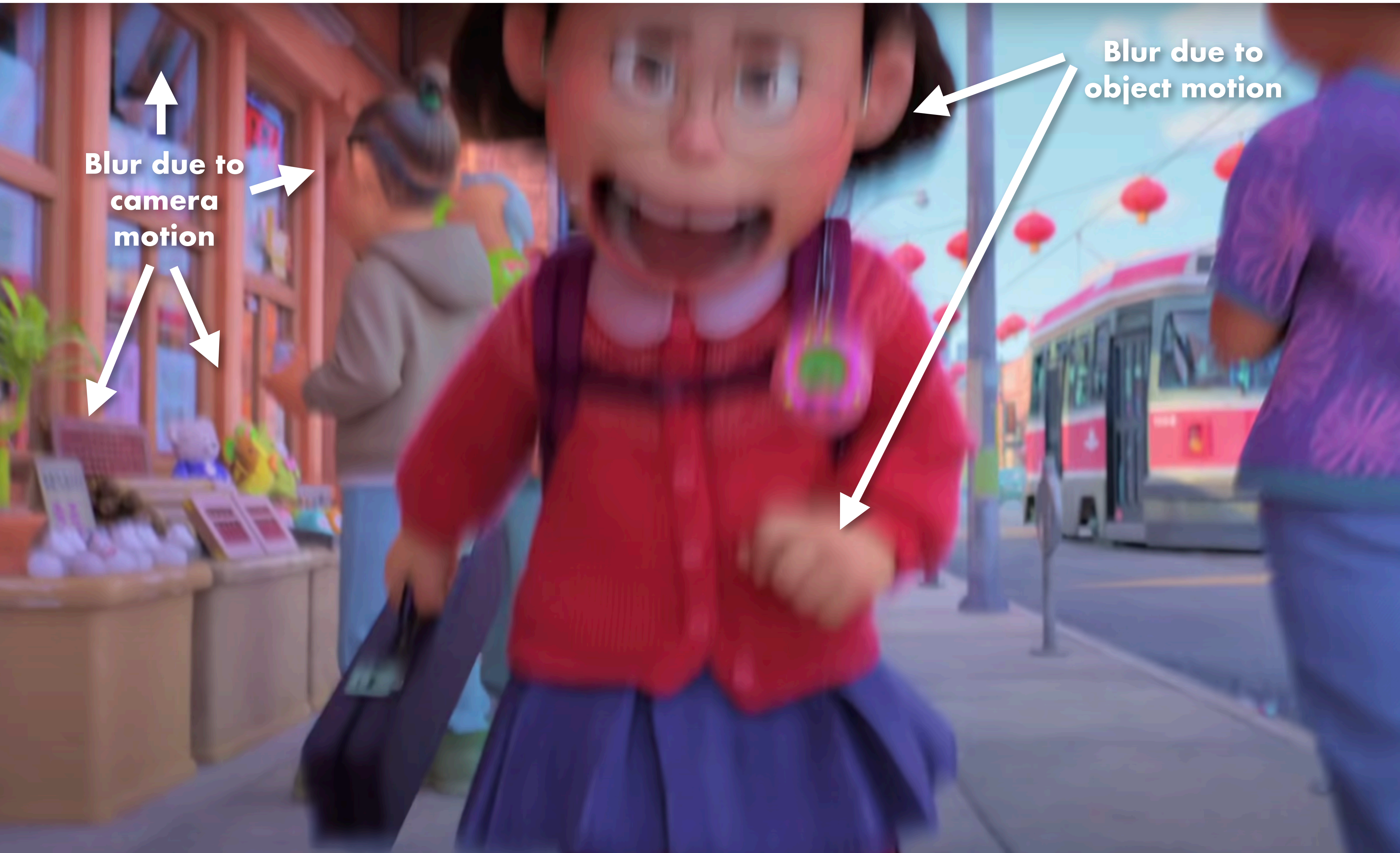
(c) Example 2: Object partitioning

(d) Example 2: Temporal partitioning

**See Woop et al. 2017 (STBVH)**



# Frame from "Turning Red" trailer



# Light Field Cameras

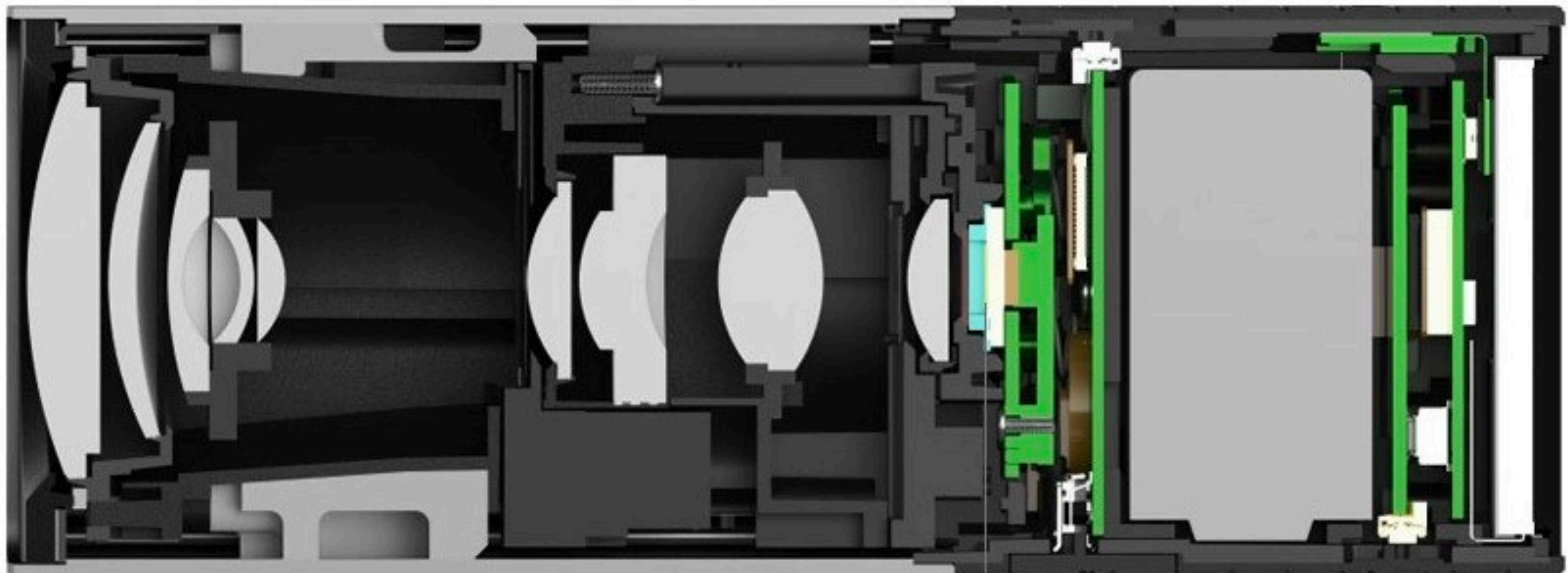
### Lens

The Lytro Light Field Camera starts with an 8X optical zoom, f/2 aperture lens. The aperture is constant across the zoom range allowing for unheard of light capture.

### Light Field Engine 1.0

The Light Field Engine replaces the supercomputer from the lab and processes the light ray data captured by the sensor.

The Light Field Engine travels with every living picture as it is shared, letting you refocus pictures right on the camera, on your desktop and online.

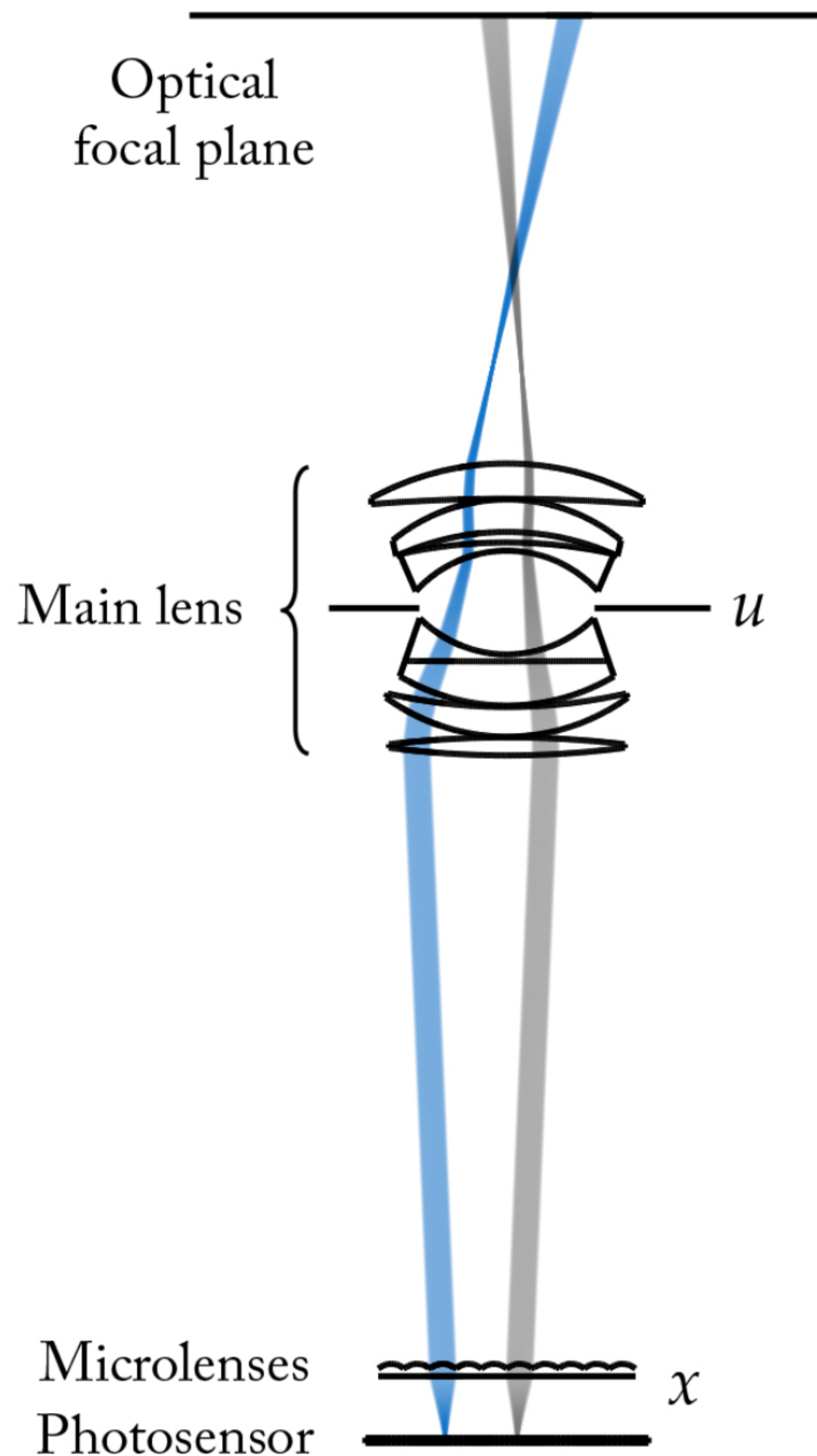


### Light Field Sensor

From a roomful of cameras to a micro-lens array specially adhered to a standard sensor, the Lytro's Light Field Sensor captures 11 million light rays.

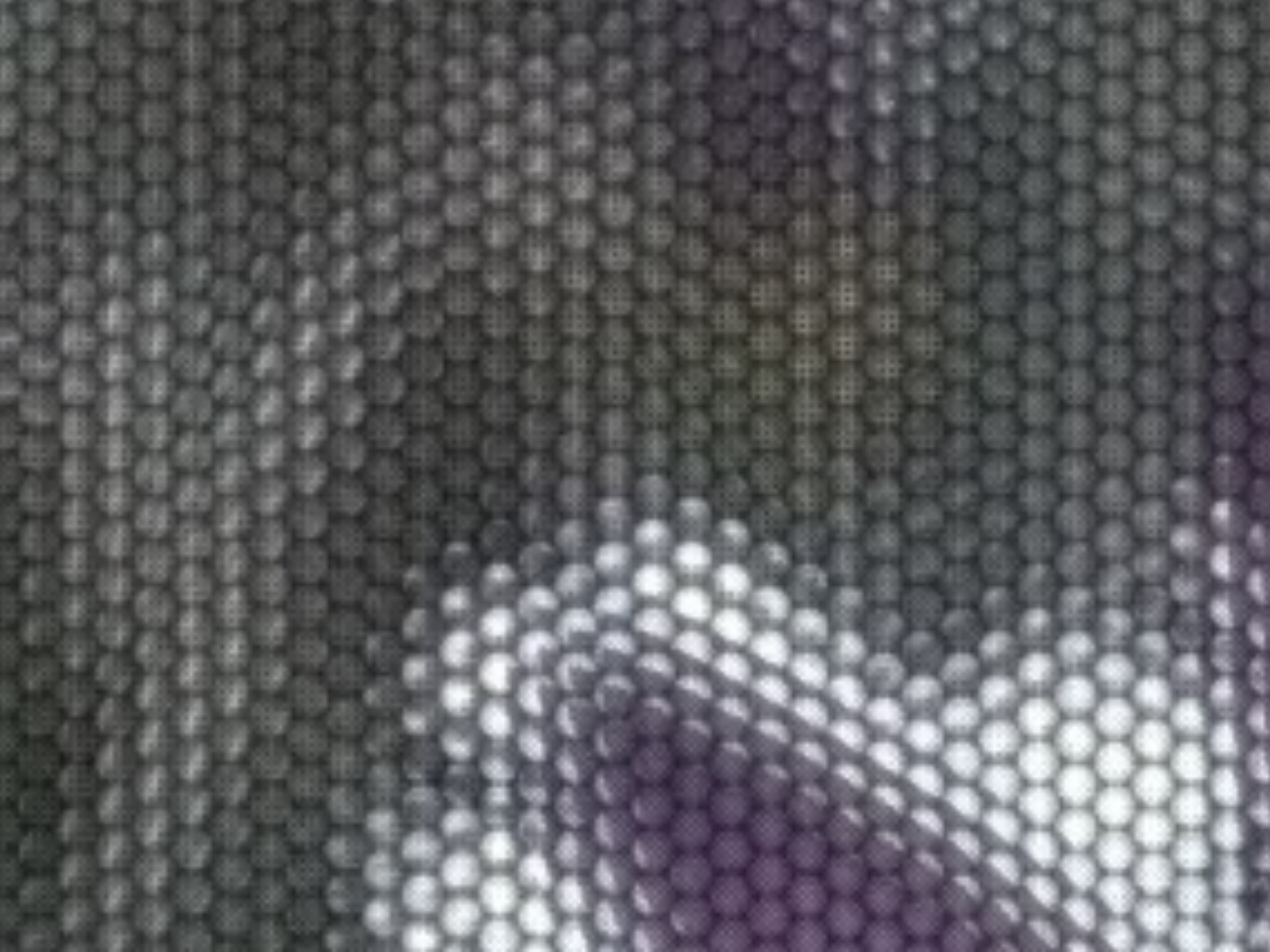
# PIXAR Super Lightfield Lens





**Each microlens (and the pixels underneath it) form a “mini” camera taking a picture of the back of the main lens**





# Stanford camera array





# Assignment 3

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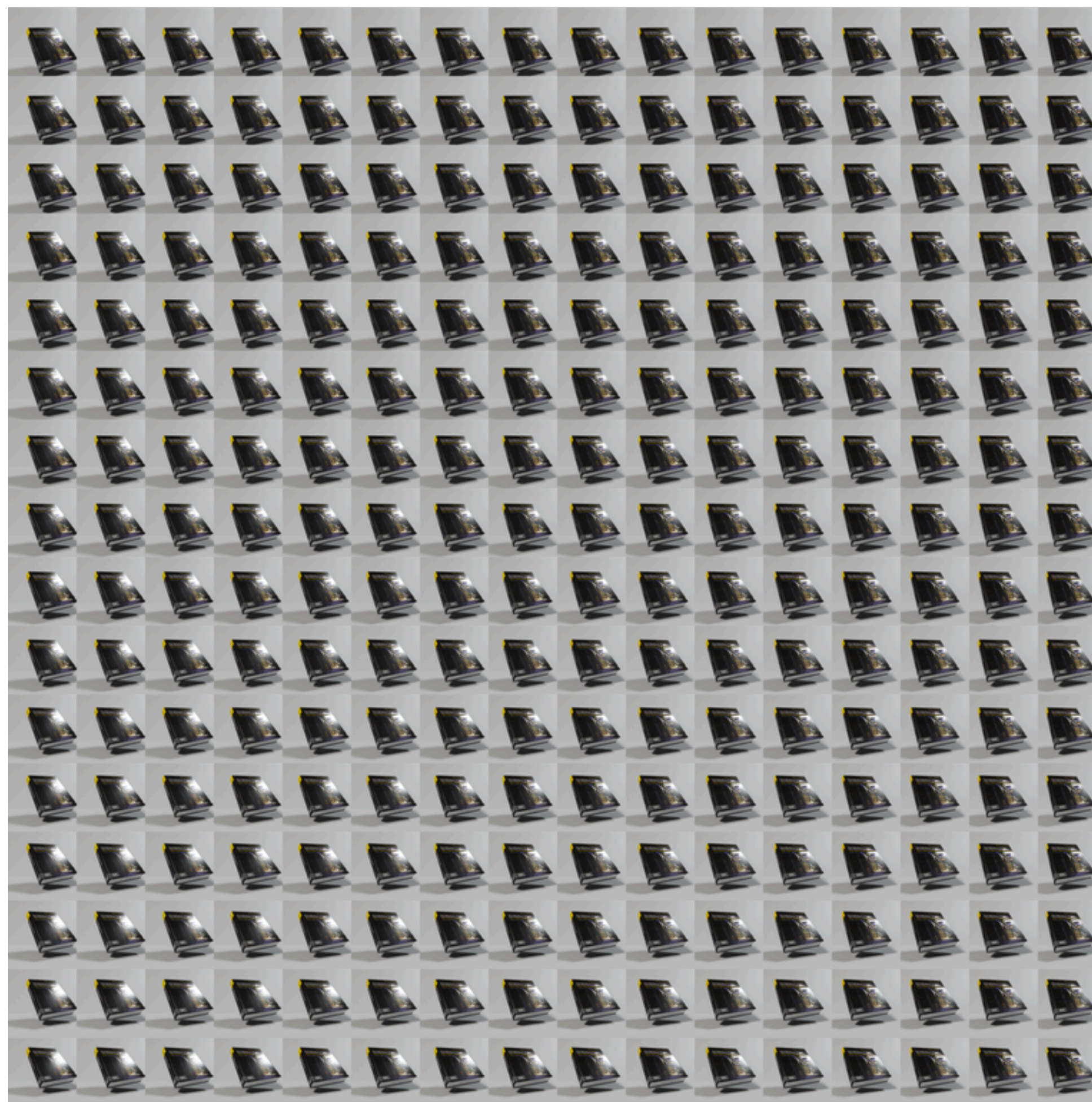
## Part 1. Create light field image using pbrt



# Assignment 3

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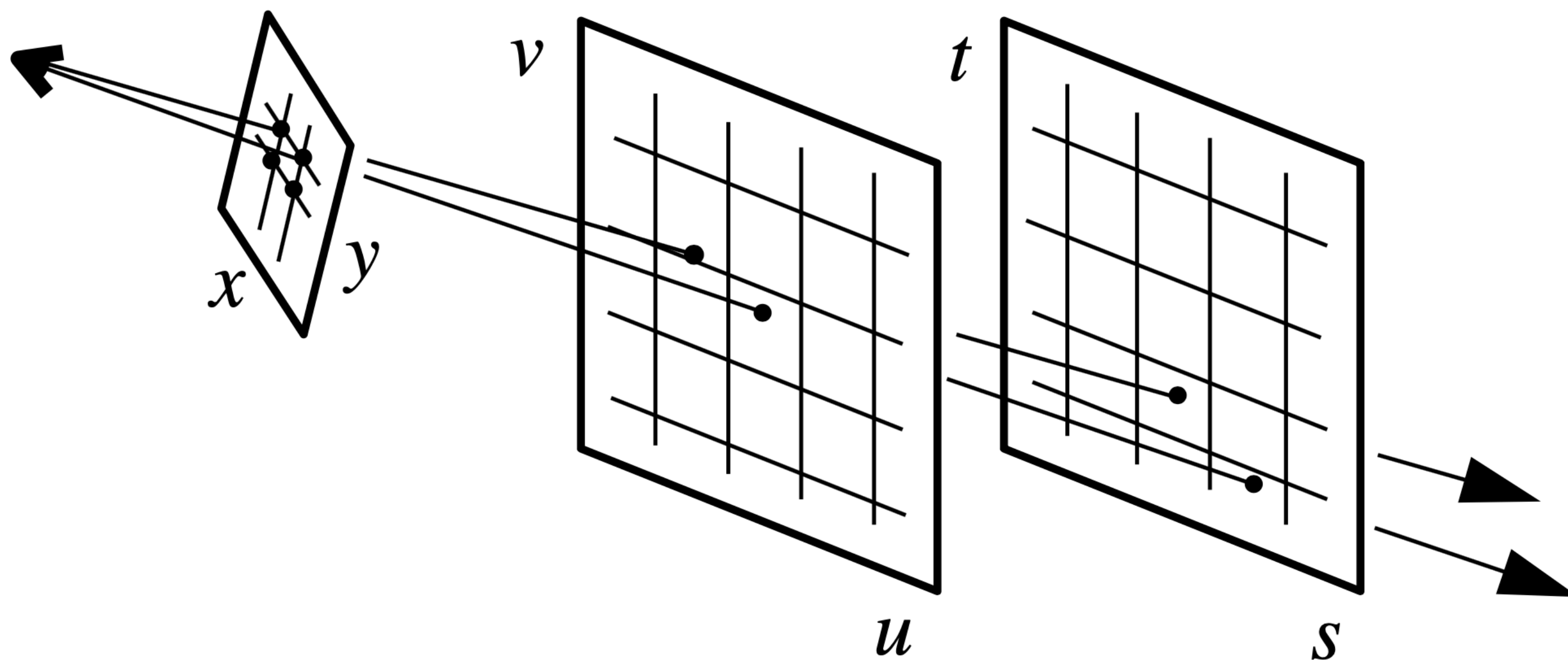
## Part 1. Create light field image using pbrt



# Assignment 3

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**Part 2. Compute image  $I(x,y)$  from another viewpoint using the light field image**



# Acknowledgments

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**Many thanks to Marc Levoy, Pat Hanrahan,  
and Ren Ng**